

----- (Phenomenology session of WG2) -----
Wednesday (3 July, 2002)

~~10:00~~²² - ~~10:30~~⁵² S. Choubey
Global analysis of solar neutrinos
~~10:30~~⁴⁸ - ~~11:00~~¹⁸ K. Kimura
EXACT FORMULA OF PROBABILITY AND CP VIOLATION
FOR NEUTRINO OSCILLATIONS IN MATTER

~~11:30~~⁴⁵ - ~~12:00~~¹⁵ H. Minakata
METHOD FOR DETERMINATION OF $|U(E3)|$ IN
NEUTRINO OSCILLATION APPEARANCE EXPERIMENTS
~~12:00~~¹⁵ - ~~12:30~~⁴⁵ K. Whisnant
BREAKING EIGHT FOLD DEGENERACIES IN NEUTRINO
CP VIOLATION, MIXING, AND MASS HIERARCHY
~~12:30~~⁴⁵ - ~~13:00~~¹⁵ O. Mena
Resolving degeneracies between CP- δ and
 θ_{13}

~~13:55~~^{14:10} - ~~14:30~~⁴⁵ P. Huber
CP, T & CPT violation at future LBL experiments
~~14:30~~ - ~~15:00~~ Y.Y. Wong
T-violation tests for relativity principles
~~15:00~~ - ~~15:30~~ M. Campanelli
Effects of new physics in Oscillations in matter
~~15:30~~ - ~~16:00~~ D. Meloni
The $\nu_e \rightarrow \nu_\tau$ channel as a tool to improve
the leptonic CP violation measurement

~~16:30~~^{16:00} - ~~17:00~~³⁰ T. Ota
Matter profile effect in neutrino factory
~~17:00~~ - ~~17:30~~ W. Winter
The effects of matter density uncertainties
on neutrino oscillations in the Earth

----- (Theory session of WG2) -----
~~17:30~~ - ~~18:00~~ T. Morozumi
LEPTOGENESIS AND LOW ENERGY CP VIOLATION
~~18:00~~ - ~~18:30~~ A. Ibarra
Leptogenesis and low energy phases

not covered in this Summary

(Theory session of WG2)

Tuesday (2 July, 2002)

16:30-17:00 Q. Shafi Neutrino mass in extra dimensions
 17:00-17:30 T. Blazek GUT models
 17:30-18:15 J.W.F. Valle ^{std} Non-standard interpretations

not covered in this Summary

(Joint theory session with WG4)

Thursday (4 July, 2002)

14:15 ⁴⁵
 14:00-14:30 Y. Shimizu Theories of lepton flavor violation
 14:30-15:00 N. Shimoyama Neutrino Bimaximal Texture in MSSM with Right-handed Neutrino and Lepton Flavor Violation
 15:00-15:30 M. Koike Calculation of μ -e conversion
 15:30-16:00 J. Sato OSCILLATION ENHANCED SEARCH FOR NEW INTERACTION WITH NEUTRINOS
 16:00 ³⁰

Break

16:30-17:10 K. Babu LEPTON NUMBER VIOLATING MUON DECAY AND THE LSND NEUTRINO ANOMALY

anomalies in ν physics

$$\nu_0 \quad \Delta m_0^2 \sim O(10^{-5} \text{eV}^2) \quad \sin^2 2\theta_0 \sim 0.8 \quad \text{LMA}$$

$$\nu_{\text{atm}} \quad \Delta m_{\text{atm}}^2 \sim O(10^{-3} \text{eV}^2) \quad \sin^2 2\theta_{\text{atm}} \sim 1.0$$

$$\text{LSND} \quad \Delta m_{\text{LSND}}^2 \sim O(1 \text{eV}^2) \quad \sin^2 2\theta_{\text{LSND}} \sim O(10^{-3} - 10^{-2})$$

$$(\beta\beta)_{0\nu} \quad 0.11 \text{eV} \lesssim m_\nu \lesssim 0.58 \text{eV}$$

(not discussed here)

→ Phenomenologists can always assume

Majorana mass term and can shift m_ν ,
so no problem arises.

framework	ν_0	ν_{atm}	LSND	comments
$N_\nu=3$	✓(ν -osc)	✓(ν -osc)	X	Perfect except for LSND.
$N_\nu=4$	(2+2)	Δ (tension between ν_0 & ν_{atm})	✓(ν -osc)	Both schemes have tension, so this doesn't work well.
	(3+1)	✓(ν -osc) ✓(ν -osc)	Δ (tension w/ Bugey, CDHSW, KARMEN2)	
Babu-Pakvasa	✓(ν -osc)	✓(ν -osc)	✓(LFV)	Phenomenologically perfect.
CPT w/ $N_\nu=3$	✓(ν -osc)	✓(ν -osc)	✓(ν -osc)	Lorentz inv. is broken. (to be killed by KamLAND)

$N_\nu=3$ — main subject @ WG2

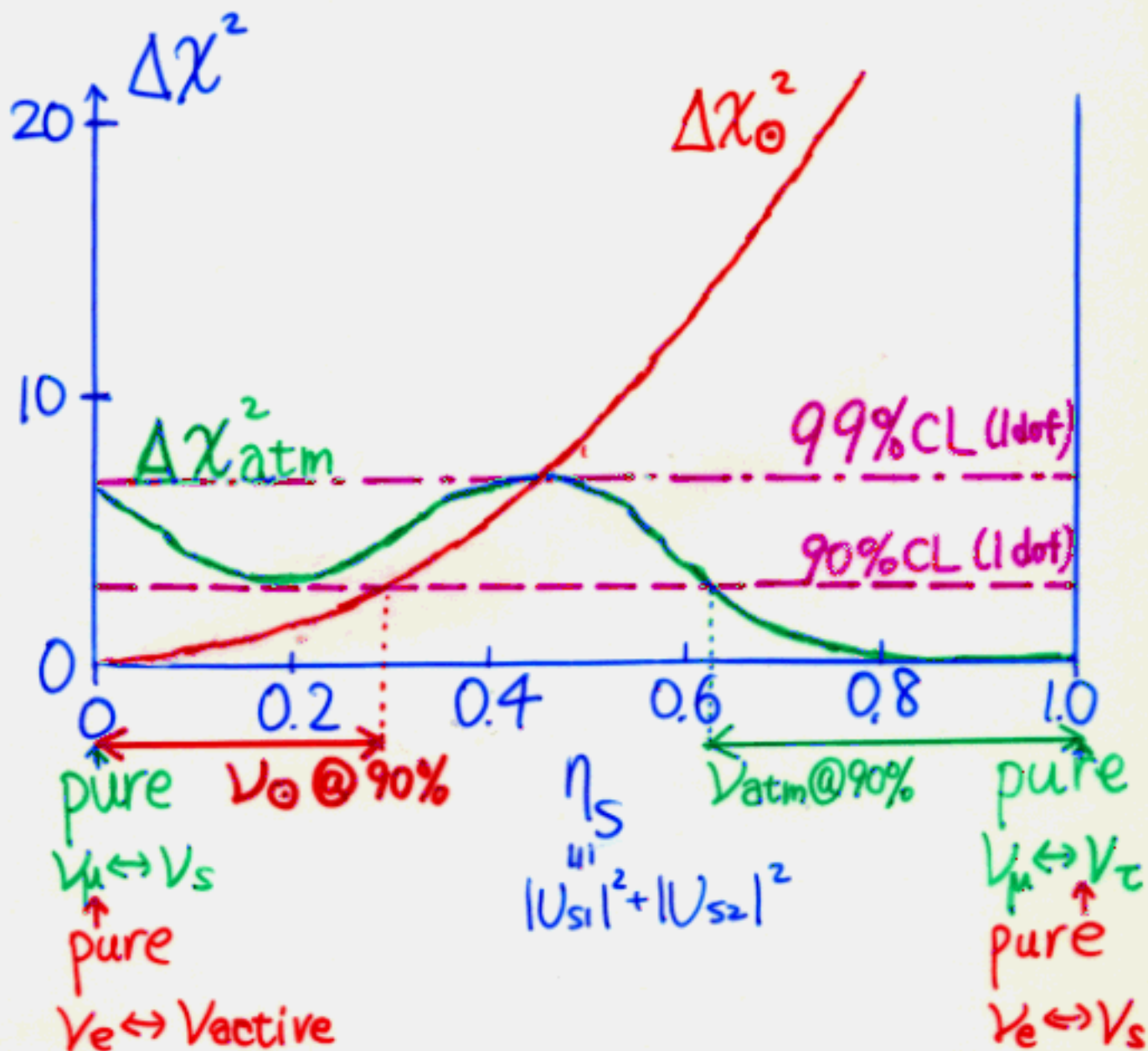
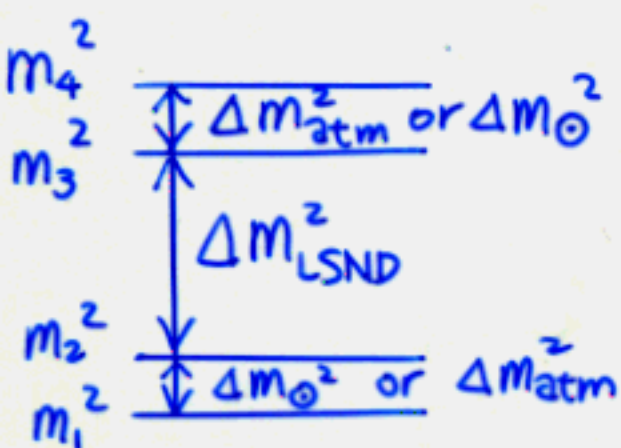
$N_\nu=4$ — not discussed

Babu-Pakvasa — discussed @ joint WG2+WG4

4ν scenarios have tension w/ data

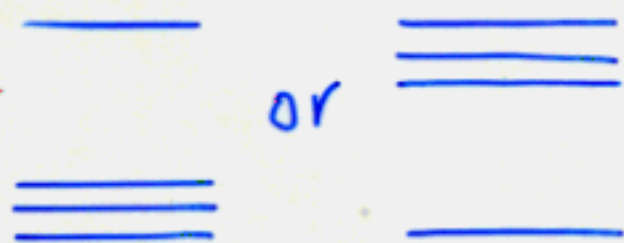
J.W.F. Valle

(2+2)-scheme



no overlap of 90% CL allowed regions of ν_{atm} & $\nu_{\odot}$

(3+1)-scheme



Bugey ($\bar{\nu}_e \rightarrow \bar{\nu}_e$):

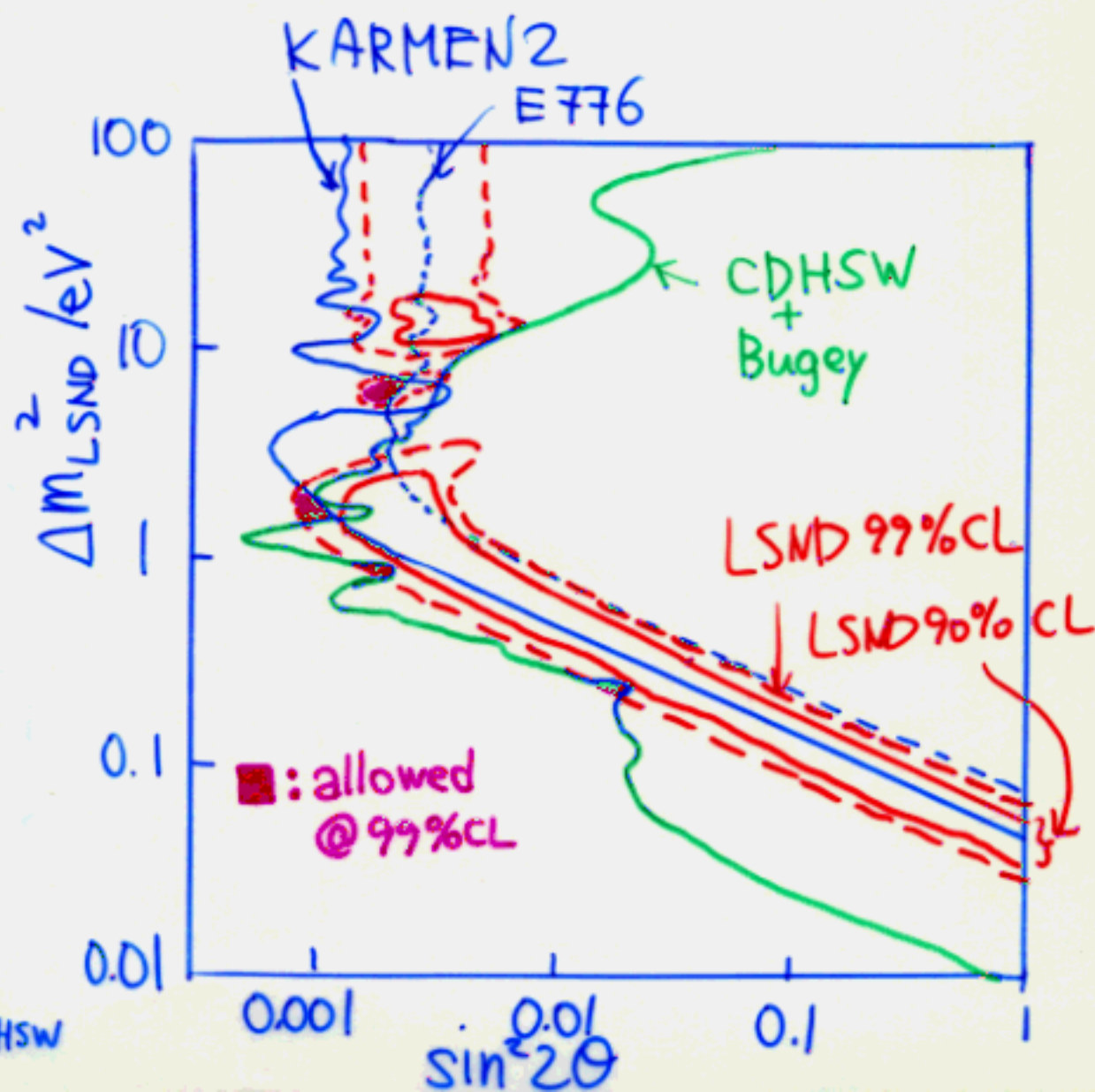
$$4|U_{e4}|^2 \leq \sin^2 2\theta_{Bugey}$$

CDHSW ($\nu_{\mu} \rightarrow \nu_{\mu}$):

$$4|U_{\mu 4}|^2 \leq \sin^2 2\theta_{CDHSW}$$

LSND in (3+1)-scheme

$$\sin^2 2\theta_{LSND} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \leq \frac{1}{4} \sin^2 2\theta_{Bugey} \sin^2 2\theta_{CDHSW}$$



• Lepton # violation in μ -decay

K.S. Babu

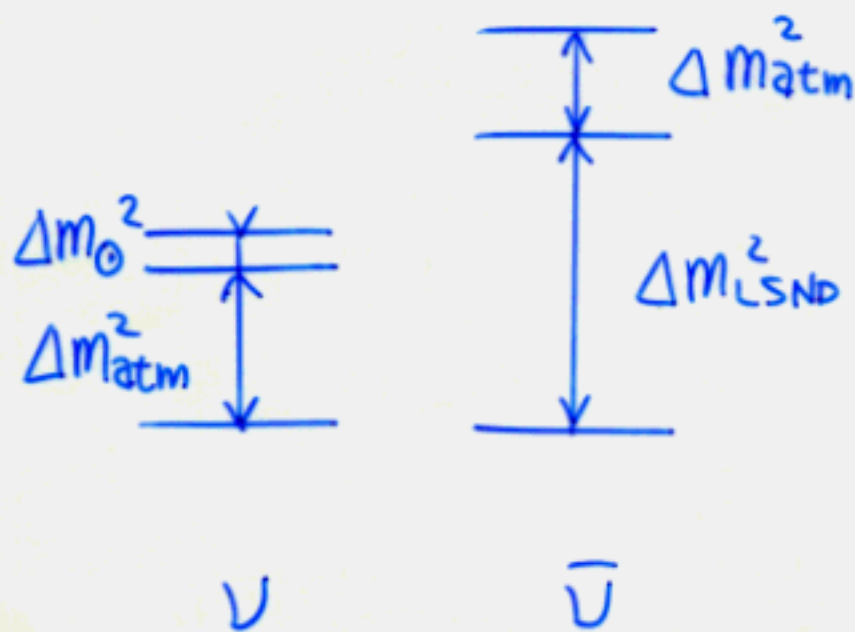
$$\mu^+ \rightarrow e^+ + \bar{\nu}_e + \bar{\nu}_i \quad (i = e, \mu, \tau)$$

$\Delta L = 2$ process explains LSND

NB Mini-Boone will see nothing.
(π -decay)

• CPT violation

Murayama-Yanagida '01



If Δm_{ij}^2 is different for ν & $\bar{\nu}$

then $N_\nu = 3$ is enough to explain

LSND. : no $\bar{\nu}_e \leftrightarrow \bar{\nu}_e$ for $\Delta m_{ij}^2 = \Delta m_0^2$

⇒ If Kamland sees deficit in $\bar{\nu}_e \leftrightarrow \bar{\nu}_e$
for $\Delta m^2 = \Delta m_0^2$ (LMA) then this scenario
will be excluded.

Subjects discussed @ WG2 (phenomenology)

6

$N_\nu = 3$

$(\Delta m_{21}^2, \theta_{12})$, $(\Delta m_{32}^2, \theta_{23})$,

↑

ν_0

S. Choubey

J.W.F. Valle

↑

ν_{atm}

θ_{13} , $\text{sign}(\Delta m_{32}^2)$, δ

↑

to be measured by future
long baseline experiments

main motivation

- exact formula for $P(\nu_\alpha \rightarrow \nu_\beta)$ in matter
with constant density

K. Kimura

- degeneracy in parameter space

- (δ, θ_{13})

H. Minakata

- $\pm \Delta m_{32}^2$

K. Whisnant

- $(\theta_{23}, \frac{\pi}{2} - \theta_{23})$

O. Mena

D. Meloni

- determination of $N_e(\vec{r})$ from LBL exp.

T. Ota

W. Winter

- exotic scenarios

P. Huber

CPT as well as CP, τ

Y. Y. Y. Wong

violation of equivalence principle

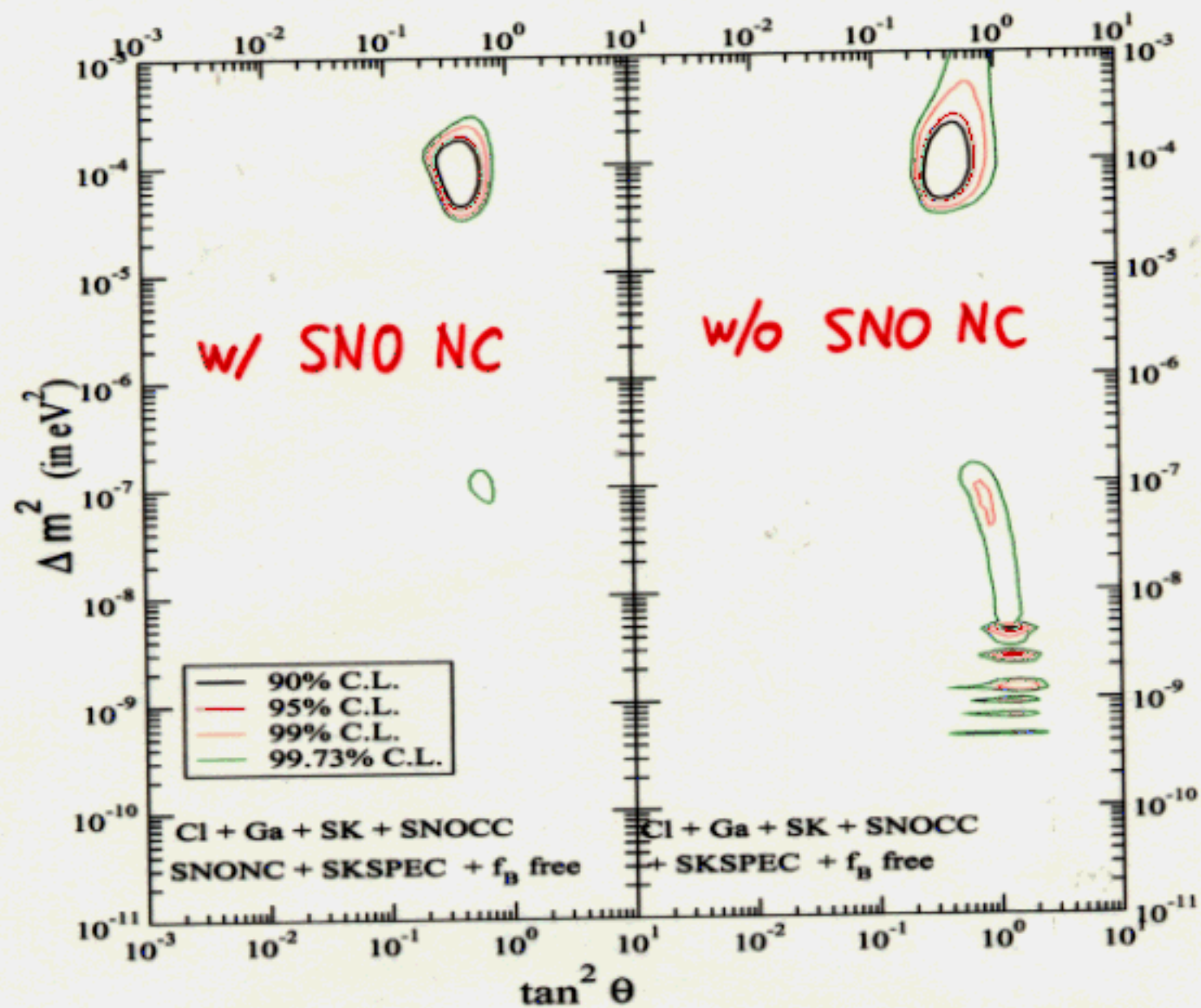
M. Campanelli

} new exotic interactions

J. Sato

Impact of SNO NC on Parameter Space

S. Choubey (सिद्धा जाँब)



- LOW appears only at 3σ
- Values of Δm^2 above 3×10^{-4} disfavored
- VO-QVO and Just-So not allowed at 3σ
- Maximal Mixing is disfavored at 3σ
- SMA further disfavored
- Dark Side solutions are gone $\Rightarrow \Delta m^2 > 0$

2 K. Kimura Exact formula of $P(\nu_\alpha \rightarrow \nu_\beta)$ in matter w/ const. density

(木村恵一)

$$P(\nu_\alpha \rightarrow \nu_\beta)_{\text{in matter}} = \delta_{\alpha\beta} - 4 \sum_{j < k} \text{Re}(\tilde{X}_j^{\alpha\beta} \tilde{X}_k^{\alpha\beta*}) \sin^2\left(\frac{\Delta \tilde{E}_{jk} L}{2}\right) + 2 \sum_{j < k} \text{Im}(\tilde{X}_j^{\alpha\beta} \tilde{X}_k^{\alpha\beta*}) \sin(\Delta \tilde{E}_{jk} L)$$

$$\begin{pmatrix} \tilde{X}_1^{\alpha\beta} \\ \tilde{X}_2^{\alpha\beta} \\ \tilde{X}_3^{\alpha\beta} \end{pmatrix} = \begin{pmatrix} \frac{1}{\Delta \tilde{E}_{21} \Delta \tilde{E}_{32}} & \begin{pmatrix} \tilde{E}_2 \tilde{E}_3 & -(\tilde{E}_2 + \tilde{E}_3) & 1 \end{pmatrix} \\ \frac{1}{\Delta \tilde{E}_{21} \Delta \tilde{E}_{32}} & \begin{pmatrix} -\tilde{E}_1 \tilde{E}_3 & \tilde{E}_1 + \tilde{E}_3 & -1 \end{pmatrix} \\ \frac{1}{\Delta \tilde{E}_{32} \Delta \tilde{E}_{31}} & \begin{pmatrix} \tilde{E}_1 \tilde{E}_2 & -(\tilde{E}_1 + \tilde{E}_2) & 1 \end{pmatrix} \end{pmatrix} \begin{pmatrix} \delta^{\alpha\beta} \\ \sum_j \tilde{E}_j X_j^{\alpha\beta} \\ \sum_j \tilde{E}_j^2 X_j^{\alpha\beta} + \delta^{\alpha e} A \sum_j \tilde{E}_j X_j^{\alpha\beta} + \delta^{\beta e} A \sum_j \tilde{E}_j X_j^{\alpha e} \end{pmatrix}$$

where $U \text{diag}(E_1, E_2, E_3) U^{-1} + \text{diag}(A, 0, 0) = \tilde{U} \text{diag}(\tilde{E}_1, \tilde{E}_2, \tilde{E}_3) \tilde{U}^{-1}$

$$\begin{cases} \alpha, \beta = e, \mu, \tau, & E_j \equiv \sqrt{\vec{p}^2 + m_j^2} \\ X_j^{\alpha\beta} \equiv U_{\alpha j} U_{\beta j}^* & \text{(in vacuum)} \\ \tilde{X}_j^{\alpha\beta} \equiv \tilde{U}_{\alpha j} \tilde{U}_{\beta j}^* & \text{(in matter)} \end{cases}$$

K. Kimura showed for $N_\nu = 3$

① $\tilde{X}_j^{\alpha\beta}$ can be explicitly expressed in terms of $X_j^{\alpha\beta}$, $\tilde{E}_j$ and E_j (**linear** in $X_j^{\alpha\beta}$).

② $P(\nu_\mu \rightarrow \nu_e) = A \cos \delta + B \sin \delta + C$
where A, B, C are functions of E_j & θ_{ij} .

His results are more useful than previous works (e.g. Zaglauer - Schwarzer '88) because

i) the expression does not use particular parametrization for $U_{\alpha j}$.

ii) it is relatively easy to see under what condition enhancement occurs.

$$\Delta_{13} \equiv \frac{\Delta m_{13}^2 L}{2E}$$

$$Q \equiv \frac{1}{4} \sin 2\theta_{12} \sin 2\theta_{23} \sin \frac{\Delta_{13}}{2} \frac{\Delta m_{12}^2 L}{2E}$$

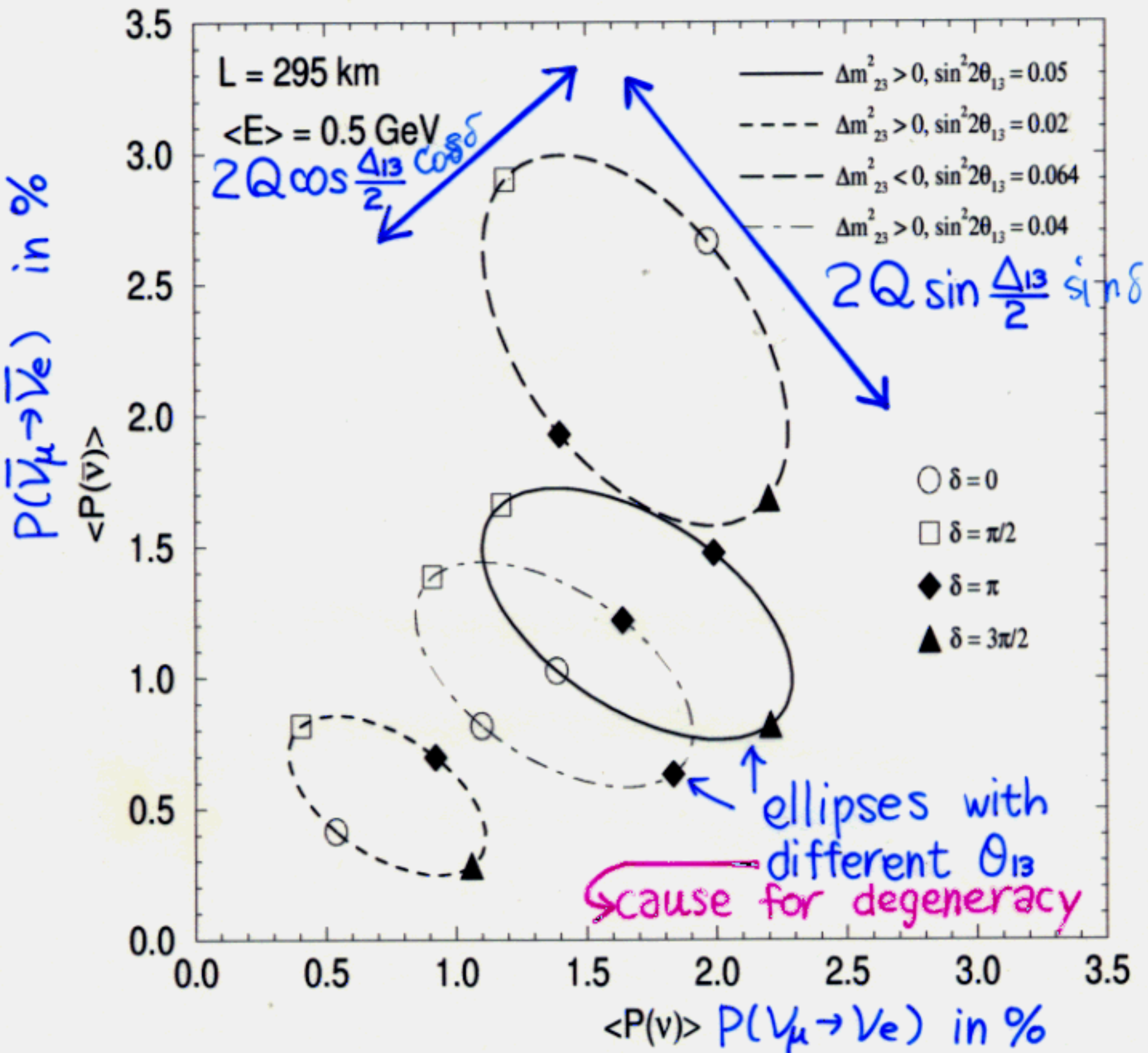


FIG. 1. CP trajectory diagrams showing the contours of $\langle P(\nu) \rangle \equiv \langle P(\nu_\mu \rightarrow \nu_e) \rangle$ and $\langle P(\bar{\nu}) \rangle \equiv \langle P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \rangle$ as a function of δ . The Gaussian energy distribution of neutrino beam with $\langle E \rangle = 0.5 \text{ GeV}$ with width $\sigma = 0.1 \text{ GeV}$ is assumed and the baseline length is taken as $L = 295 \text{ km}$. The mixing parameters are fixed to be $\Delta m_{23}^2 = \pm 3 \times 10^{-3} \text{ eV}^2$, $\sin^2 2\theta_{23} = 1.0$, $\Delta m_{12}^2 = 6.2 \times 10^{-5} \text{ eV}^2$, $\tan^2 \theta_{12} = 0.35$. We take the matter density as $\rho = 2.8 \text{ g/cm}^3$ and the electron fraction as $Y_e = 0.5$.

Tune (E, L) such that $\frac{\Delta m_{13}^2 L}{2E} = \pi$.

Then the ellipsis becomes thin and the degeneracy in (δ, θ_{13}) is reduced.

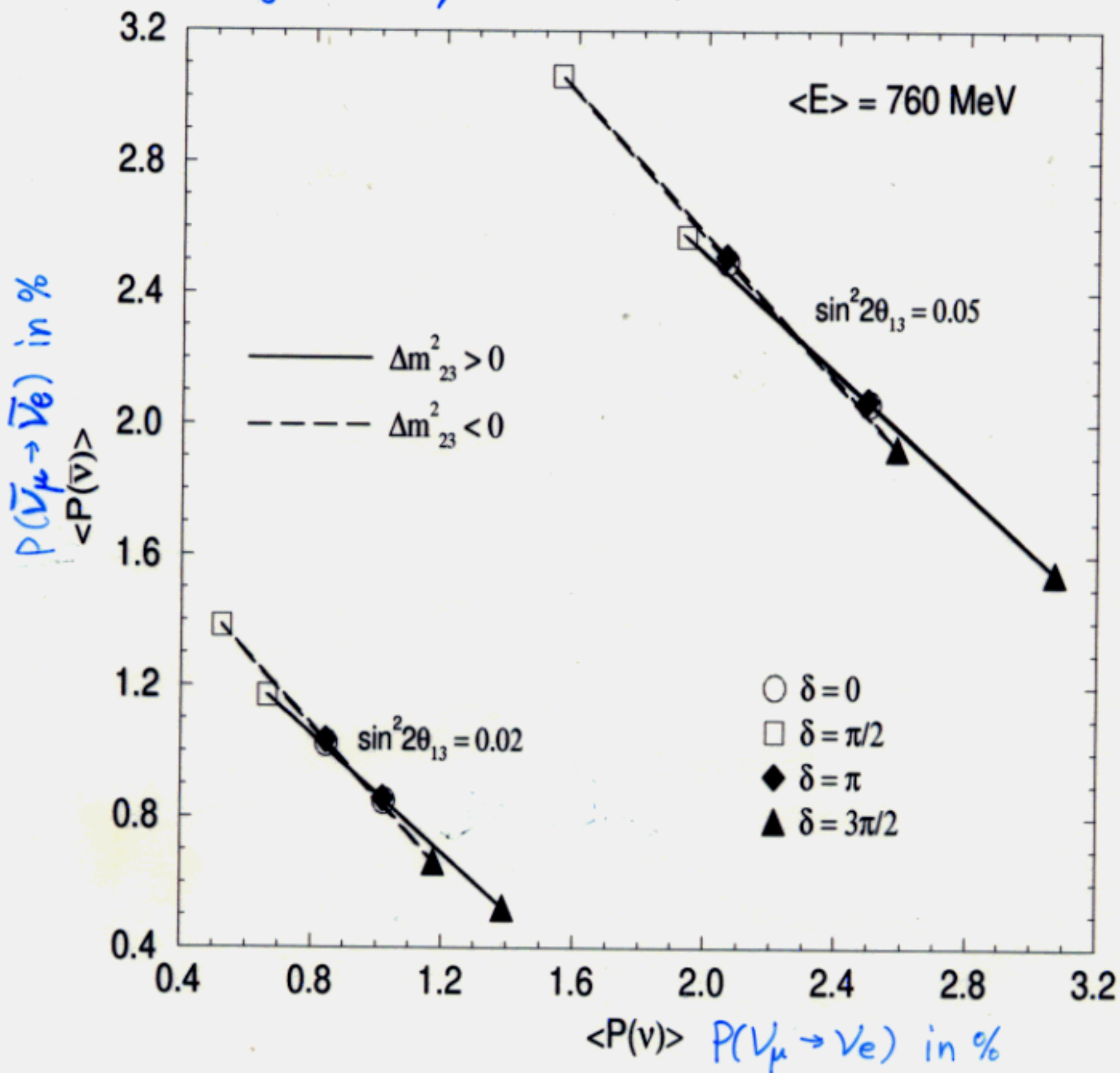


FIG. 3. The thinnest CP trajectories for a tuned peak energy for $\sin^2 2\theta_{13} = 0.05$ and 0.02 .

The beam profile, the mixing parameters and the matter density are taken as in Fig. 1.

K. Whisnant

Breaking 2^3 -fold degeneracy ¹²

(δ, θ_{13})
ambiguity

Burguet-Castel
et al.

NPB608 ('01)301

sign (Δm_{32}^2)
ambiguity

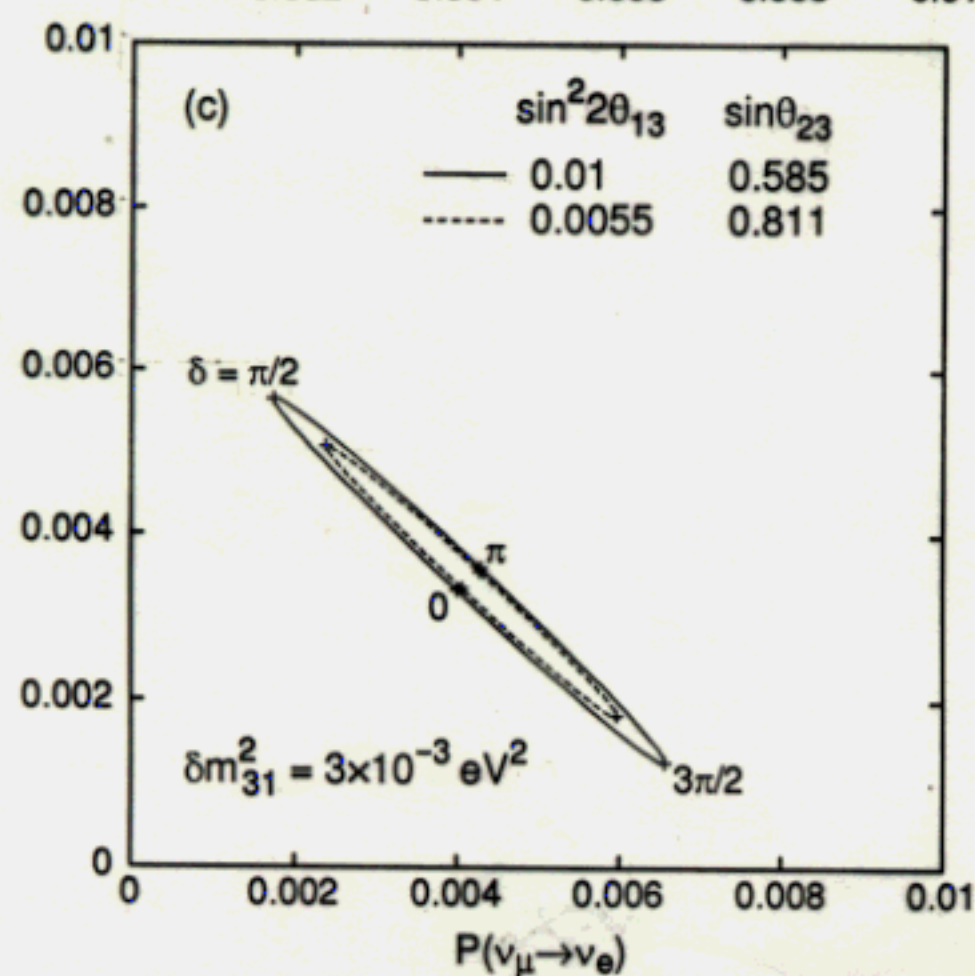
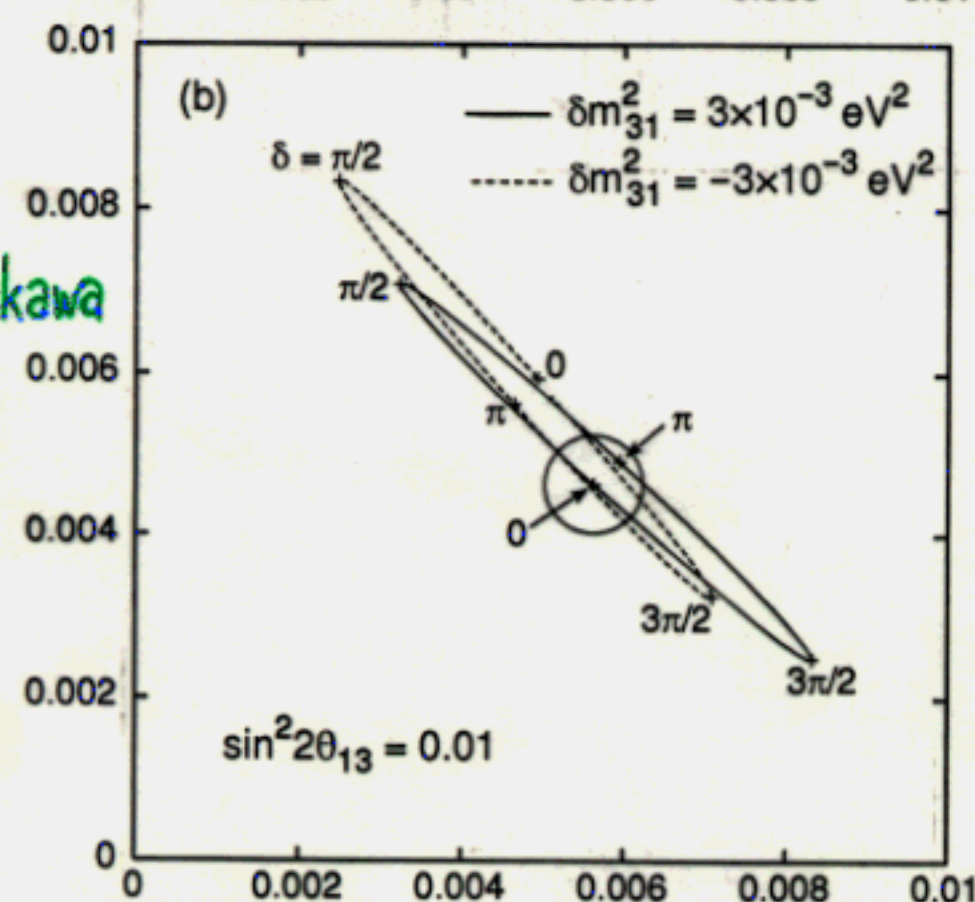
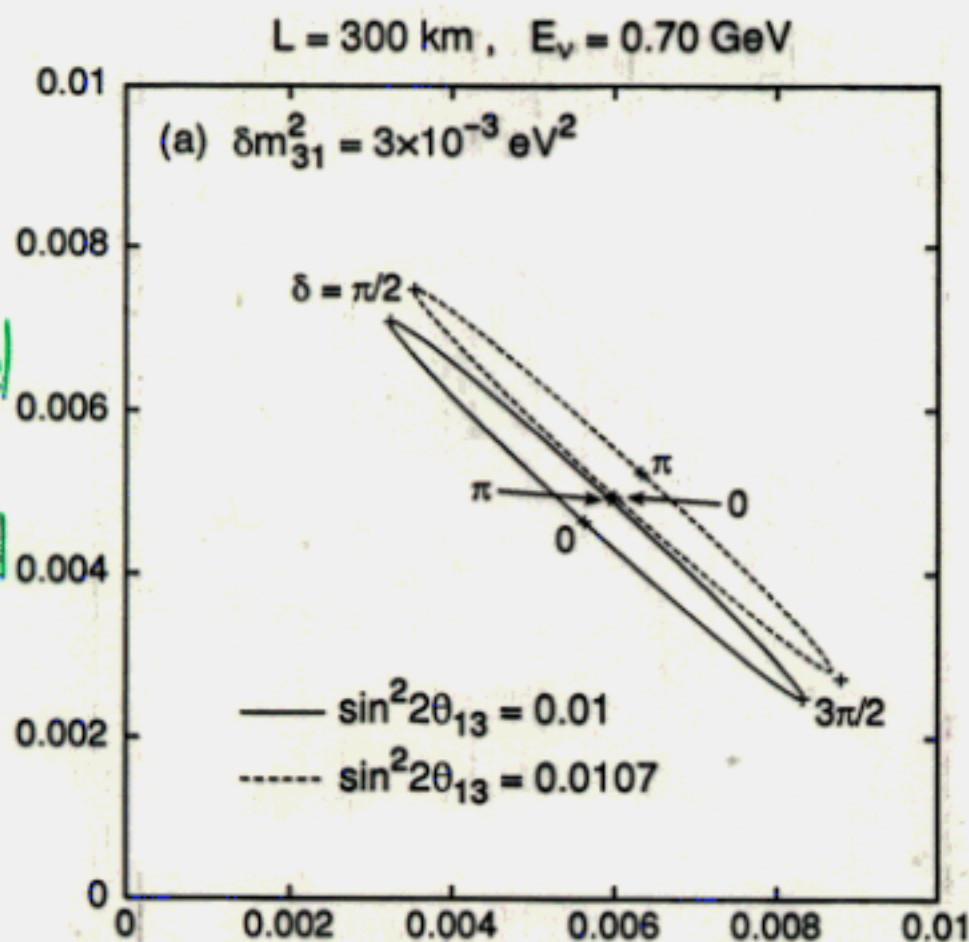
Minakata-Nunokawa

JHEP 0110
('01)001

$(\theta_{23}, \frac{\pi}{2} - \theta_{23})$
ambiguity

Barger et al.

PRD65 ('02)
073023



Measurements at
two baselines
lift these
ambiguities

→ Measurement of
 $\nu_e \rightarrow \nu_\tau$ at a
 ν factory lifts
this degeneracy

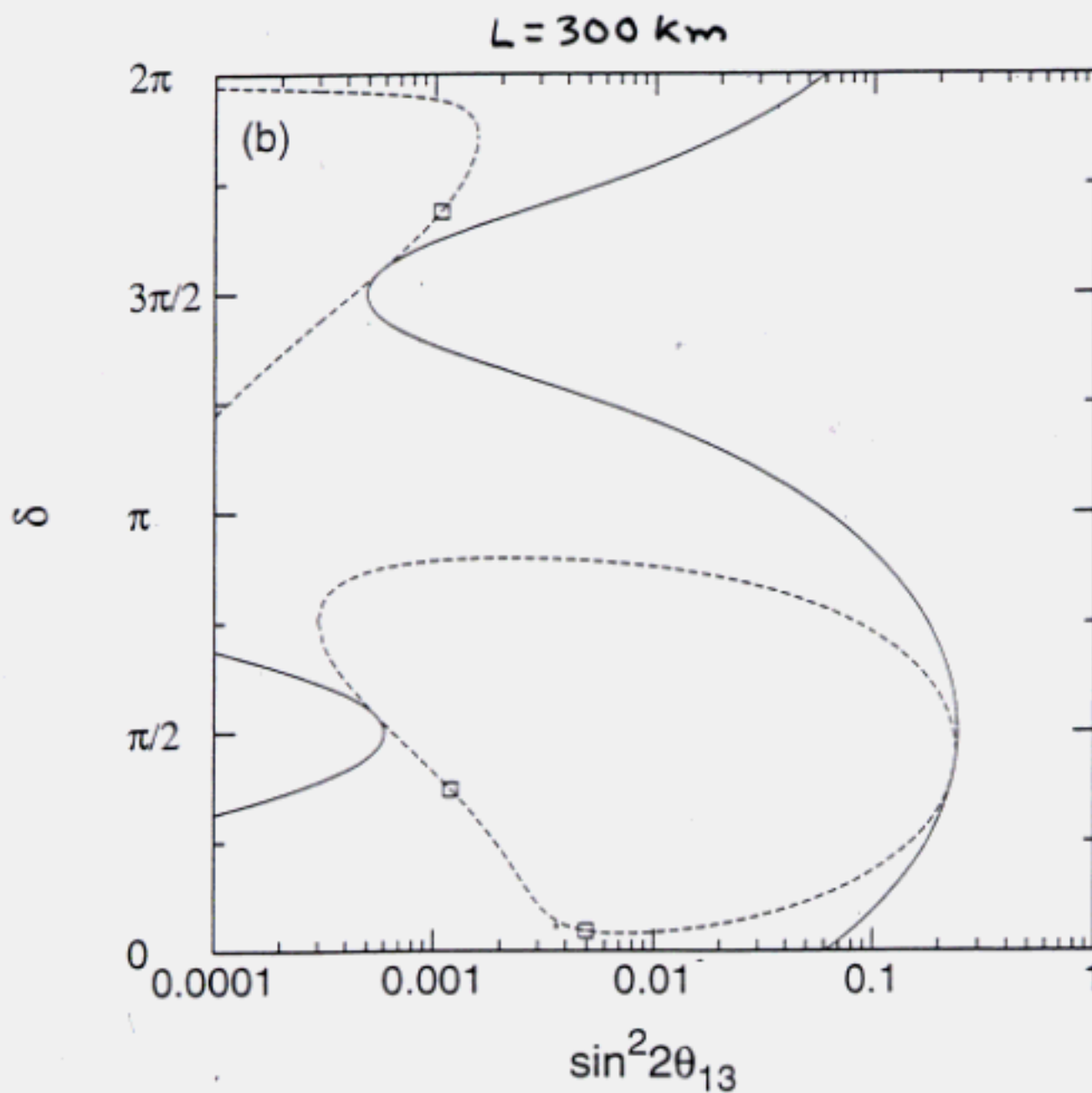
cf. in vacuum

$$P(\nu_e \rightarrow \nu_\mu) = S_{23}^2 \sin^2 2\theta_{13} \Delta$$

$$P(\nu_e \rightarrow \nu_\tau) = C_{23}^2 \sin^2 2\theta_{13} \Delta$$

$$\Delta \equiv \sin^2(\Delta m_{32}^2 L / 4E)$$

Adding a 4th measurement reduces regions with degeneracies to isolated points in (δ, θ_{13}) space



Measurements

$$\nu, \bar{\nu} @ \Delta = \frac{\pi}{2}$$

$$\text{add } \nu @ \Delta = \frac{\pi}{3}$$

$$\text{add } \bar{\nu} @ \Delta = \frac{\pi}{3}$$

Region with degeneracies

between solid lines

along dashed curves

boxes only

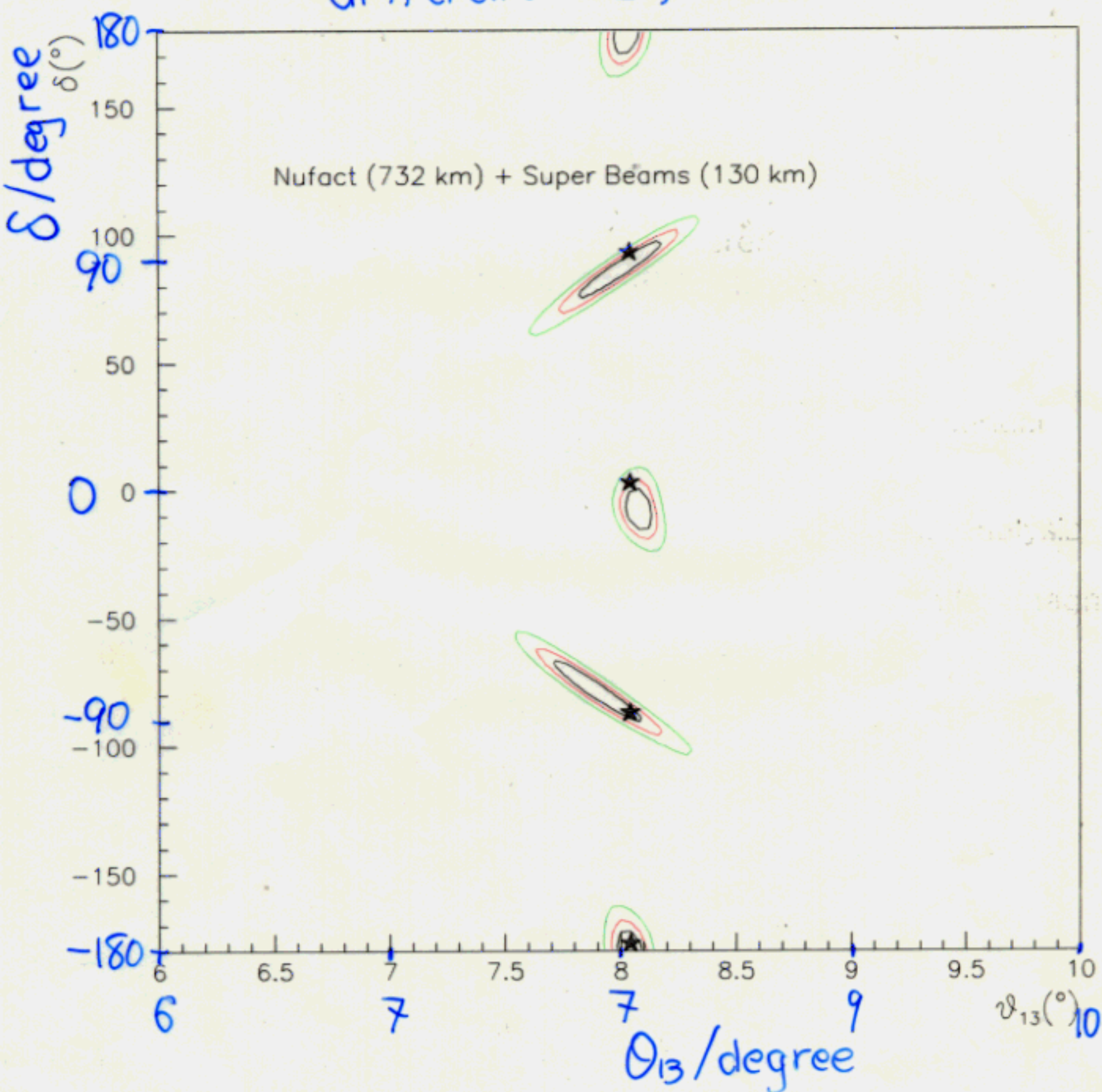
Degeneracies do not have to be removed completely;

they are not a problem if they occur at

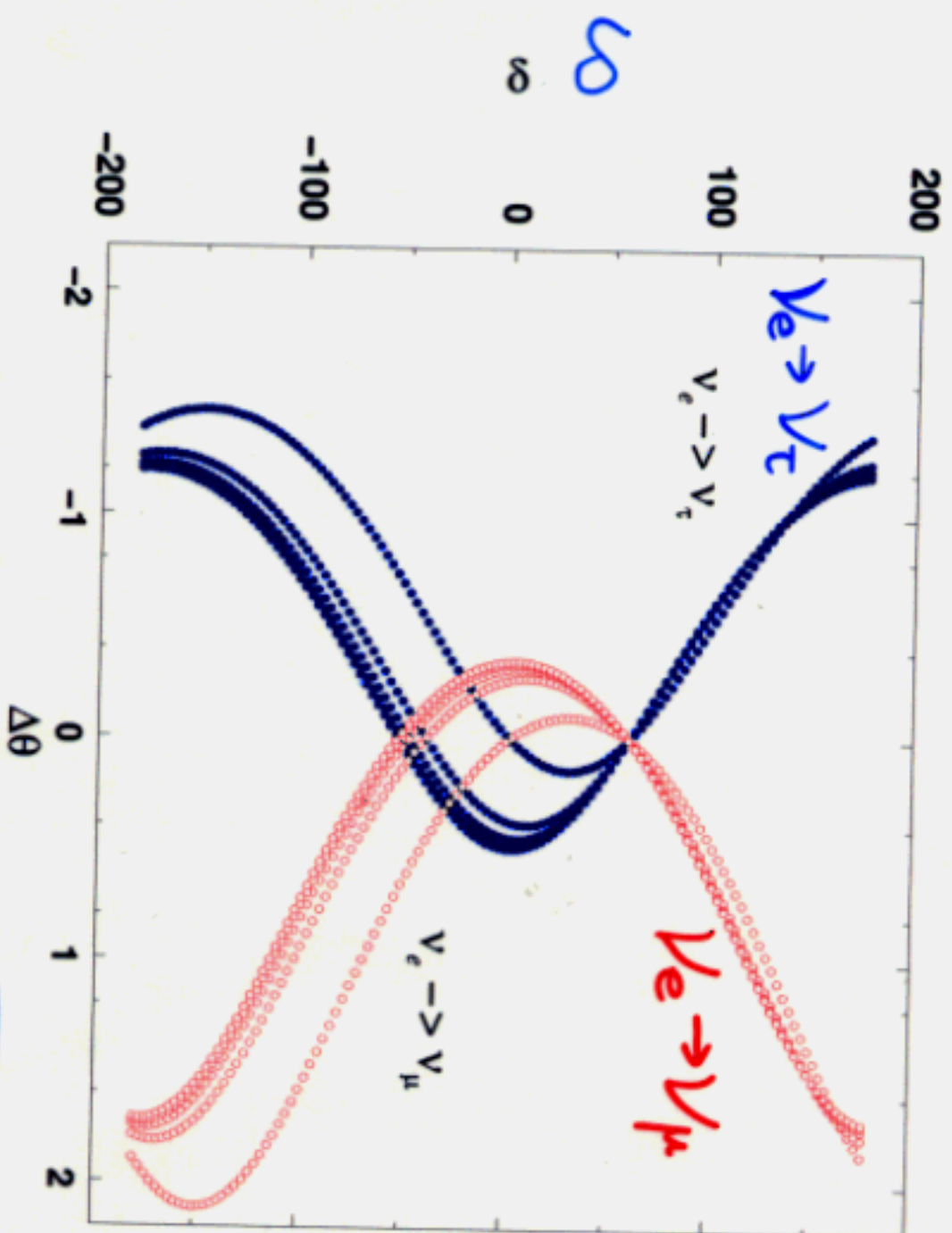
$\sin^2 2\theta_{13}$ below the reach of the experiment

O. Mena

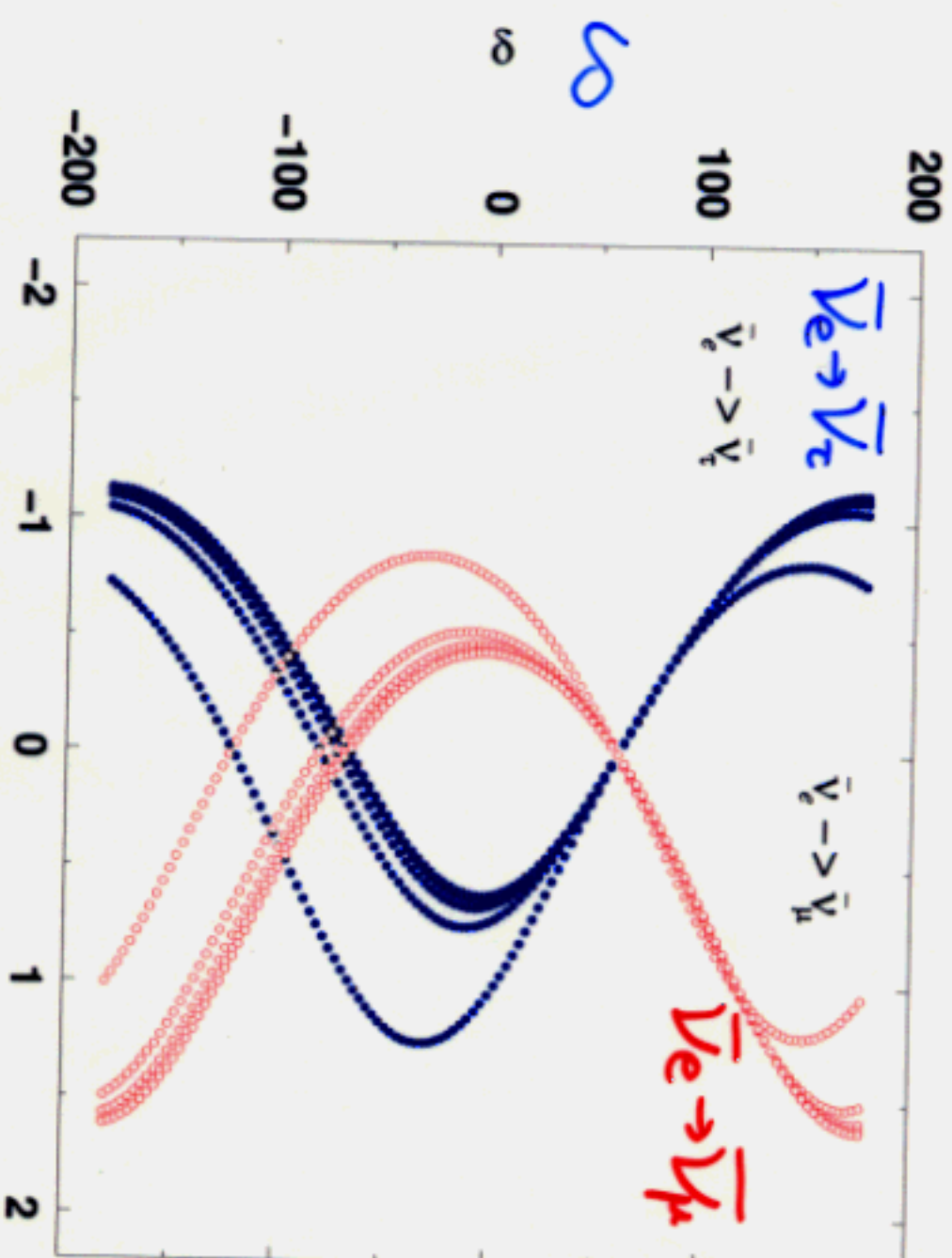
ν fact (732 km) + super beam (130 km)
different E, L



D. Meloni $\nu_e \rightarrow \nu_\tau$ channel : silver
 $\nu_e \rightarrow \nu_\mu$ channel : golden



$$\Delta\theta \equiv \theta_{13} - \theta_{13}^{\text{fake}}$$



$$\Delta\theta \equiv \theta_{13} - \bar{\theta}_{13}$$

Figure 7: Equiprobability curves in the $(\Delta\theta, \delta)$ plane, for $\theta_{13} = 5^\circ$, $\bar{\delta} = 60^\circ$, $E_\nu \in [5, 50]$ GeV and $L = 732$ Km for the $\nu_e \rightarrow \nu_\mu$ and $\nu_e \rightarrow \nu_\tau$ oscillation (neutrinos on the left antineutrinos on the right).

D. Meloni

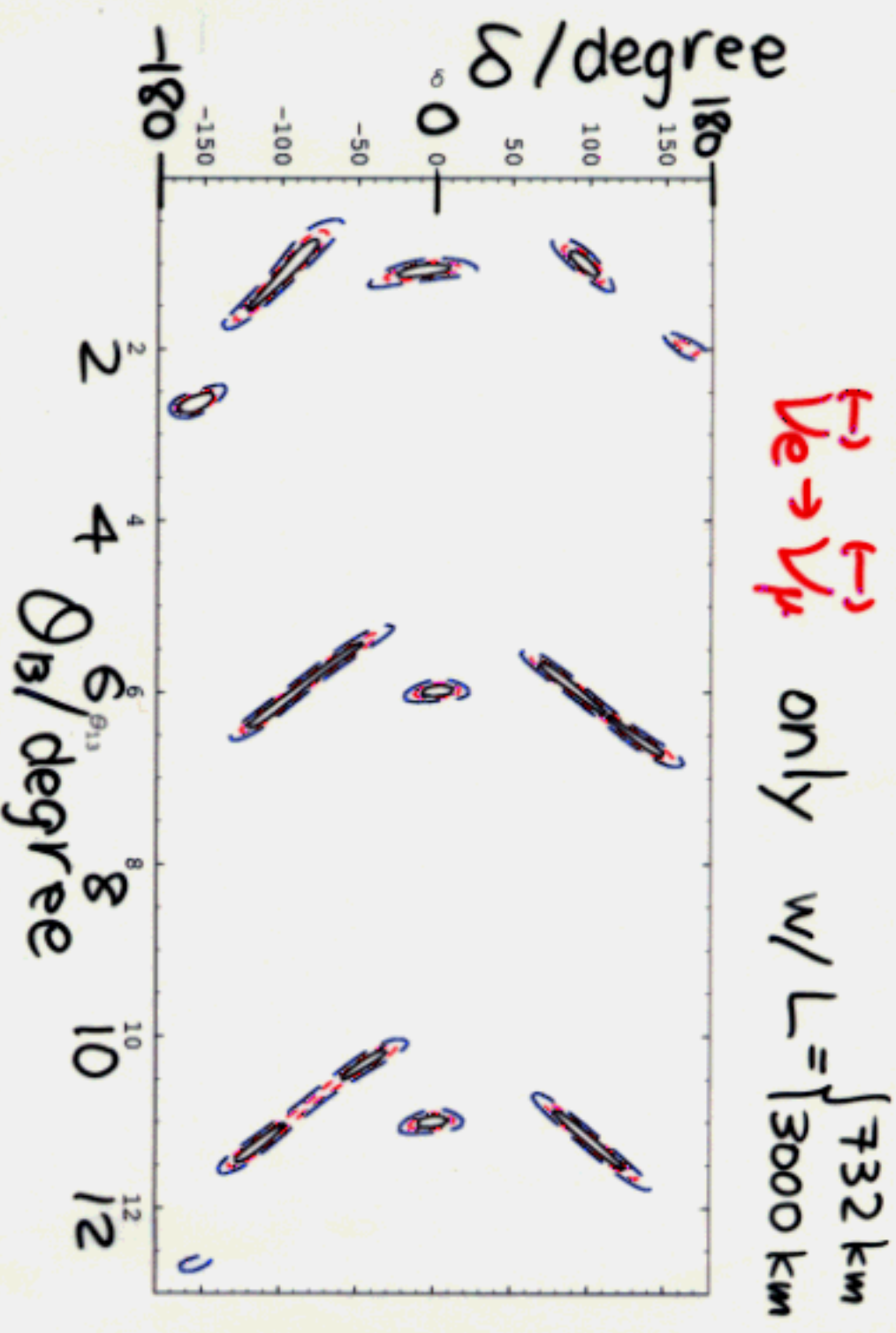
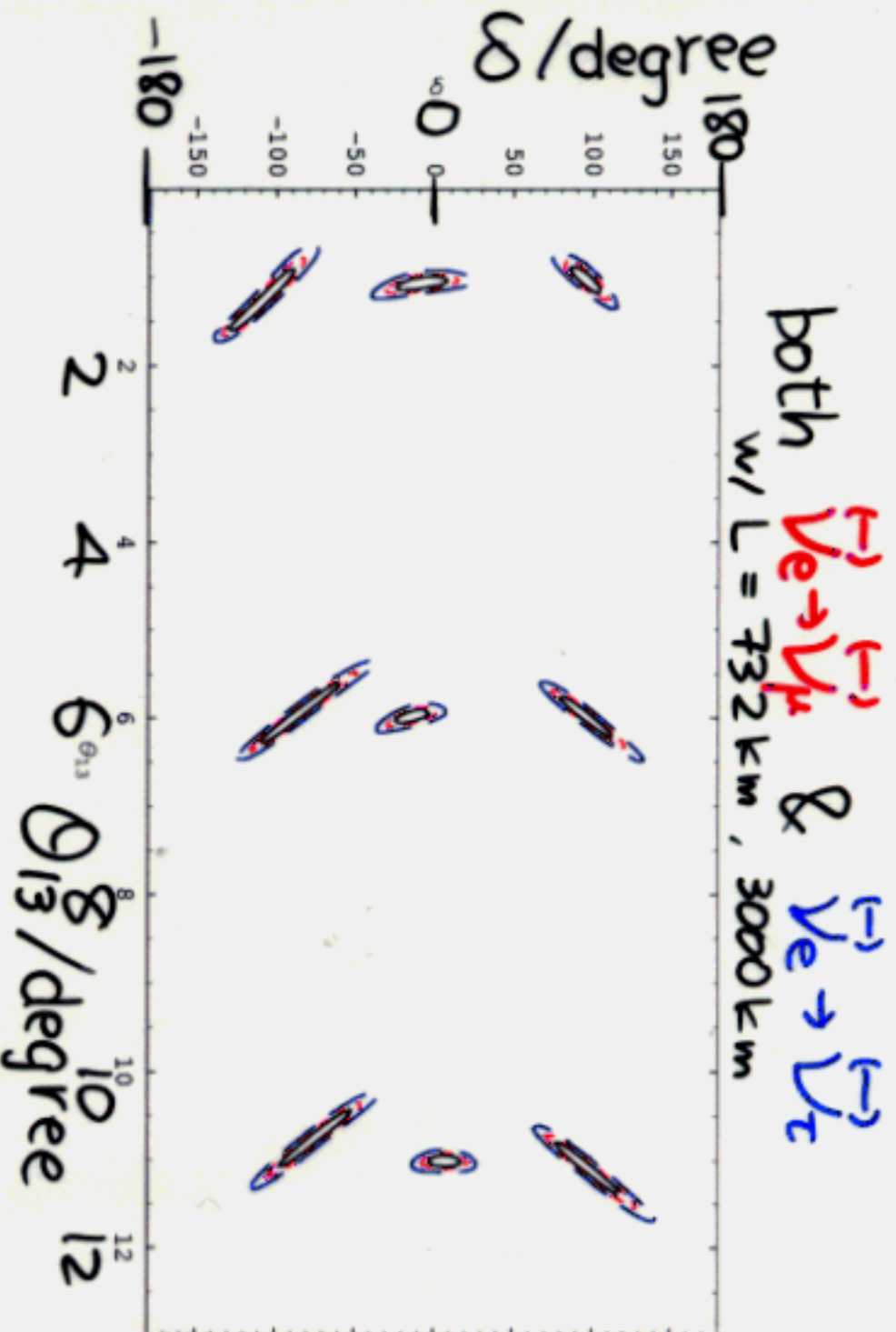


Figure 12: 68.5, 90 and 99 % C.L. contours resulting from a χ^2 fit of θ_{13} and δ , for $\theta_{13} = 1^\circ, 6^\circ$ and 11° , and $\delta = -90^\circ, 0^\circ$ and 90° , for the combination of an iron detector at $L = 3000 \text{ Km}$ and an emulsion detector at $L = 732 \text{ Km}$: (left) both “silver” and “golden” muon events are taken into account (same figure as in Fig. 11, lower right); (right) only “golden” muon events are taken into account. Five years of data taking for both polarities in the distant detector and only five years in the μ^+ polarity in the near detector have been considered.

With the silver channel, the errors are significantly reduced.

T. Ota
(太田俊彦)

Matter profile effect

$$A(x) \equiv \sqrt{2} G_F N_e(x) = \sum_{n=-\infty}^{\infty} a_n e^{-ip_n x}$$

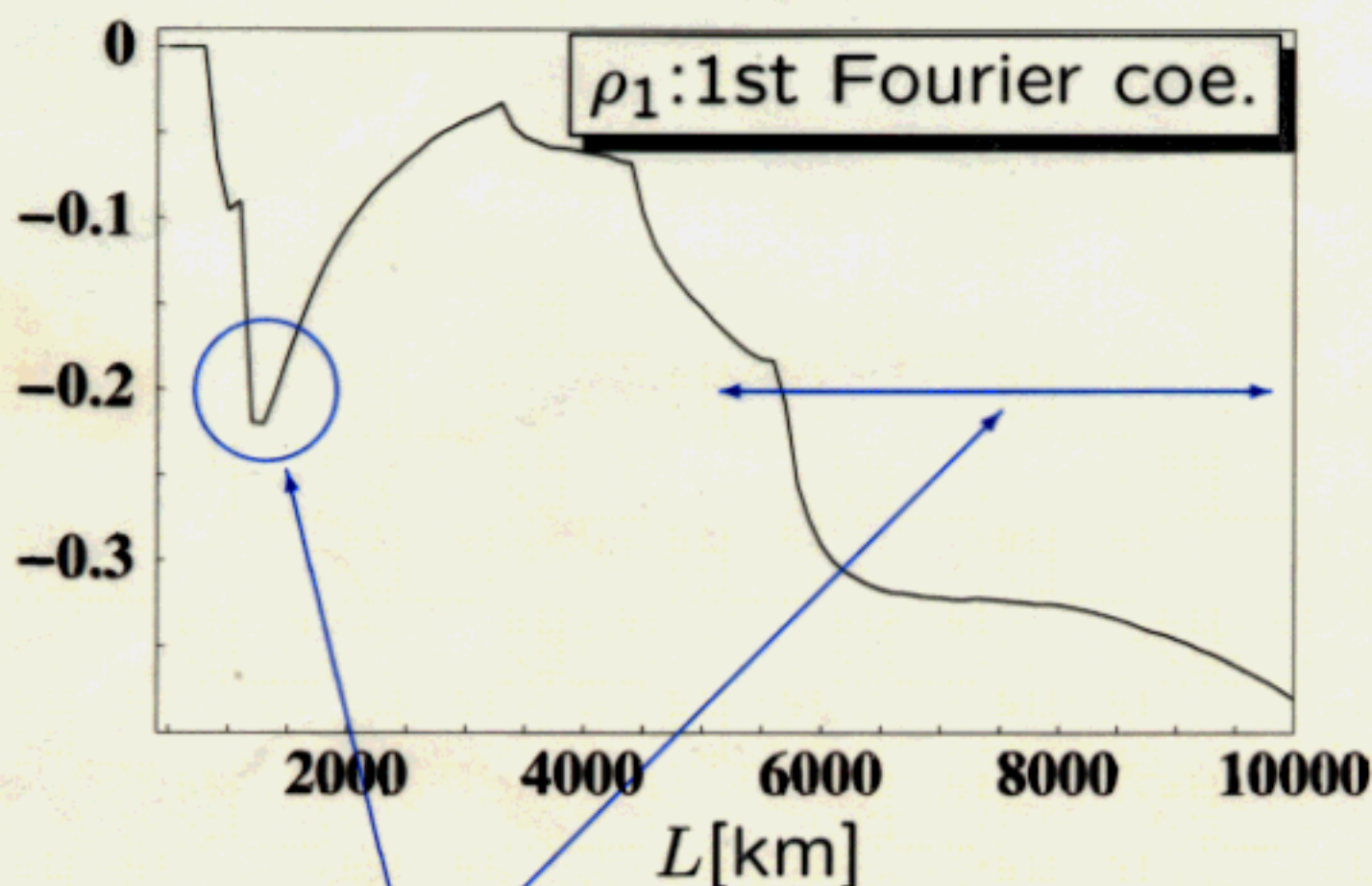
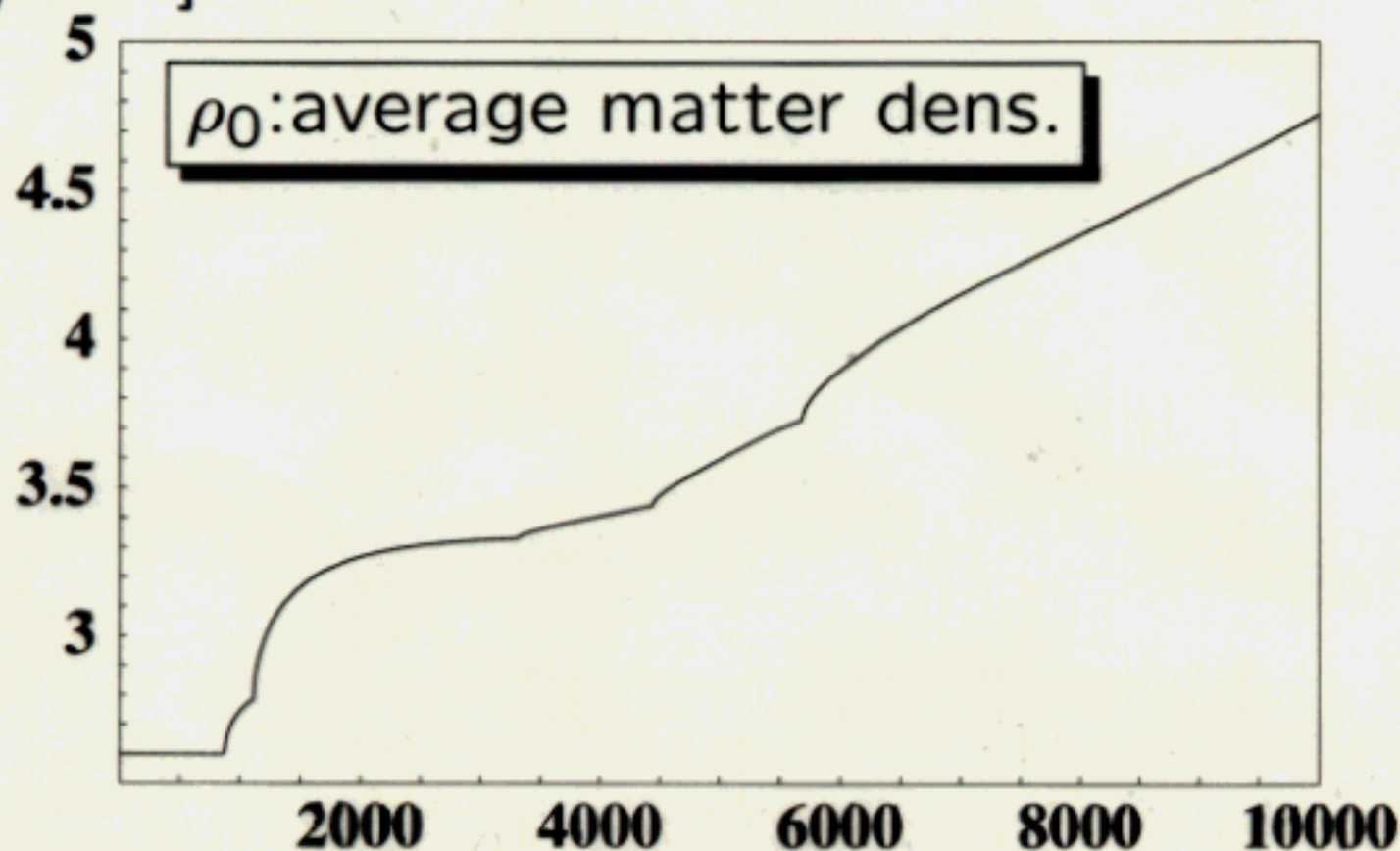
only a_0, a_1 are important

17

How large is the matter profile effect?

Based on PREM

$\rho [\text{g/cm}^3]$



In these regions, the matter profile effect is large in terms of the comparison with the average density.

■ Conclusion:

In $L \lesssim 10,000\text{km}$,

- ★ The profile including up to a_1 can reproduce the event number using PREM.
- ★ There is a strong correlation between a_0 and a_1 .
- To ignore the matter profile effect. $\stackrel{\star}{=} a_1 \rightarrow 0$.
- ★ $\stackrel{\star}{=} \text{To shift } a_0 \text{ from the average based on PREM.}$



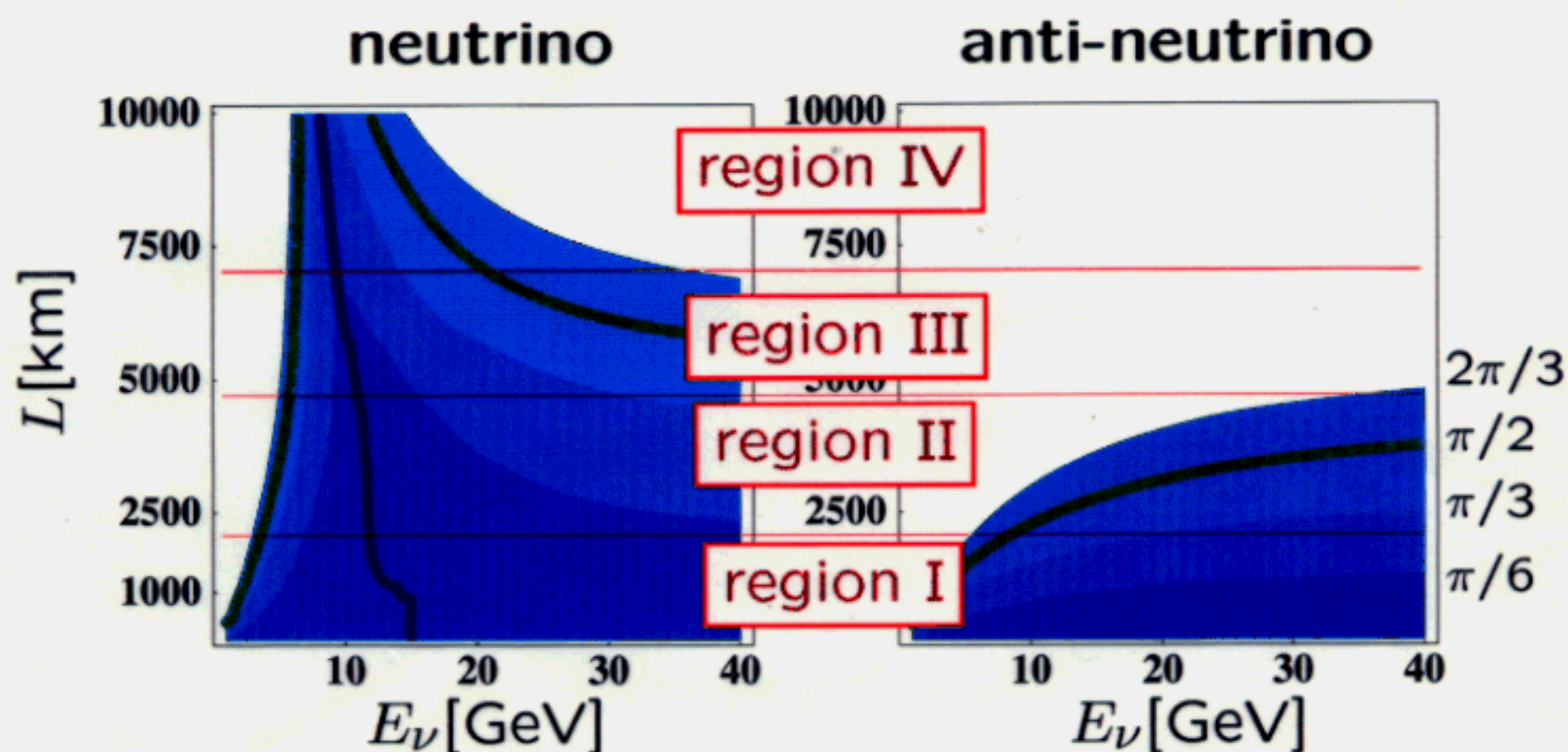
1. Even if we use the average density based on PREM, a disregard of the matter profile effect brings unexpected **extra uncertainty** ($\sim 5\%$) to a_0 in $5,000\text{km} \lesssim L \lesssim 10,000\text{km}$.

2. From the viewpoint that the analyses should be independent of the Earth model, the matter profile should be fitted in experiments. We recommend to introduce a_1 as a fitting parameter.

2'. We can deal with the change of the matter profile keeping average density value.

■ The region where the correlation exists

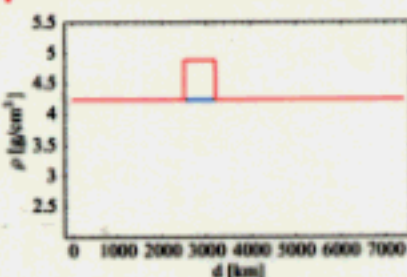
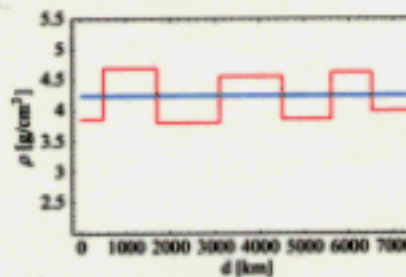
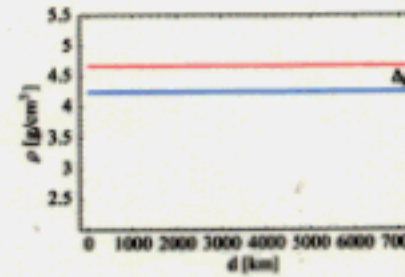
Contour plots of $\frac{\lambda_+ - \lambda_-}{4E_\nu} L$



	neutrino	anti-neutrino	correlation
region I	0	0	○
region II	0	$\pi/2$	○
region III	0, $\pi/2$	—	○
region IV	0, $\pi/2$...	—	—

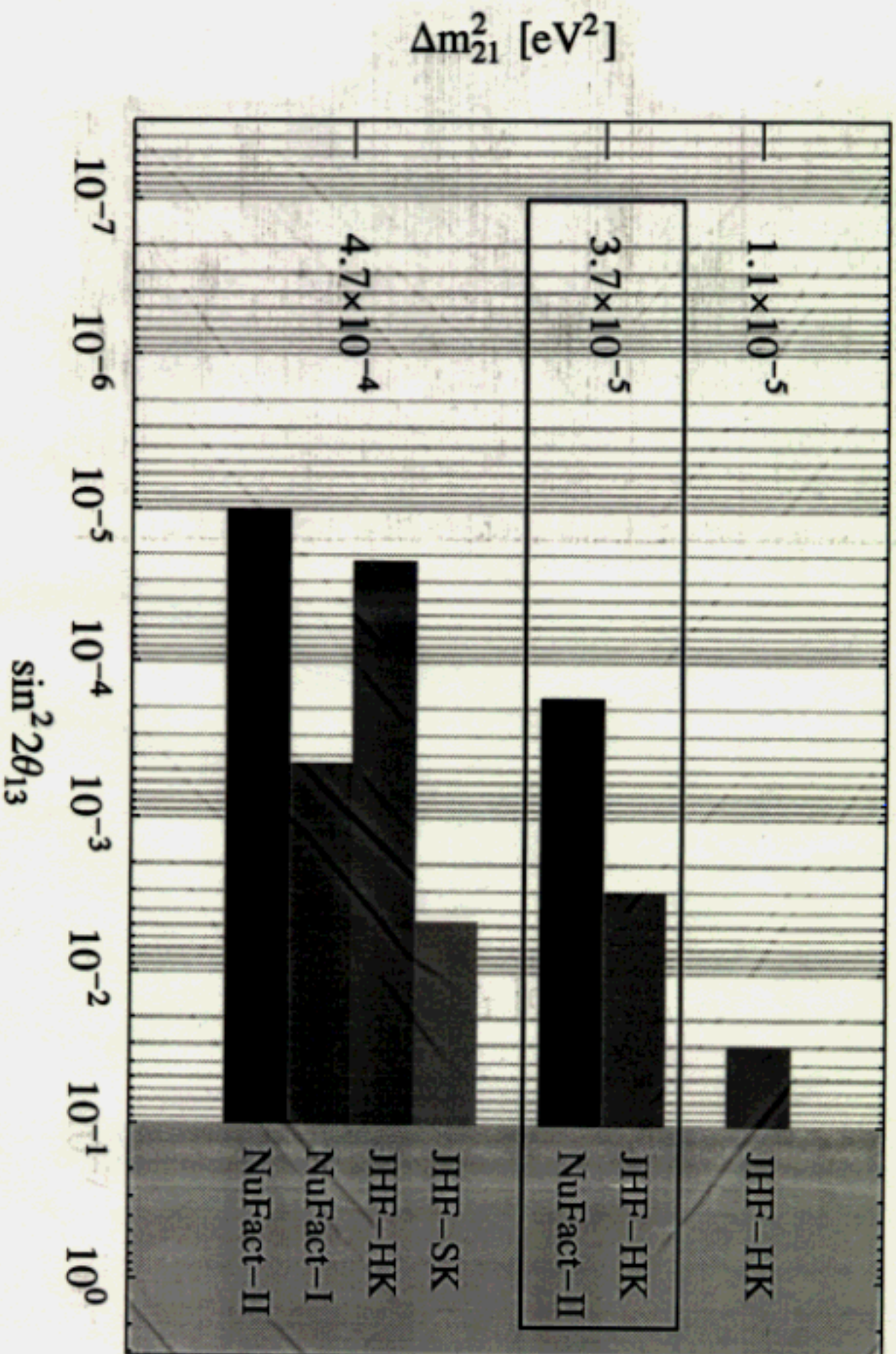
*In these regions, anti-neutrino events are not significant in statistical sense.

Summary: Comparison of models

Type	1. Single perturbation	2. Random fluctuations	3. Measured mean
			
Averaging	No	Yes	No
Dep. on	$\lambda \cdot \Delta\rho$	$\lambda \otimes \Delta\rho$ (Interference effects remaining)	$\Delta\rho$
Evaluation	Analytical	Numerical	Numerical
Level	Osc. probs.	Osc. probs.	Full analysis
Impact	Small lakes, etc.	for mines, For $\lambda \ll L$: small For $\lambda > L$: 3. good approximation	Similar magnitude as other error sources
Problem	Only limited applications	High computational effort	Conservative choice

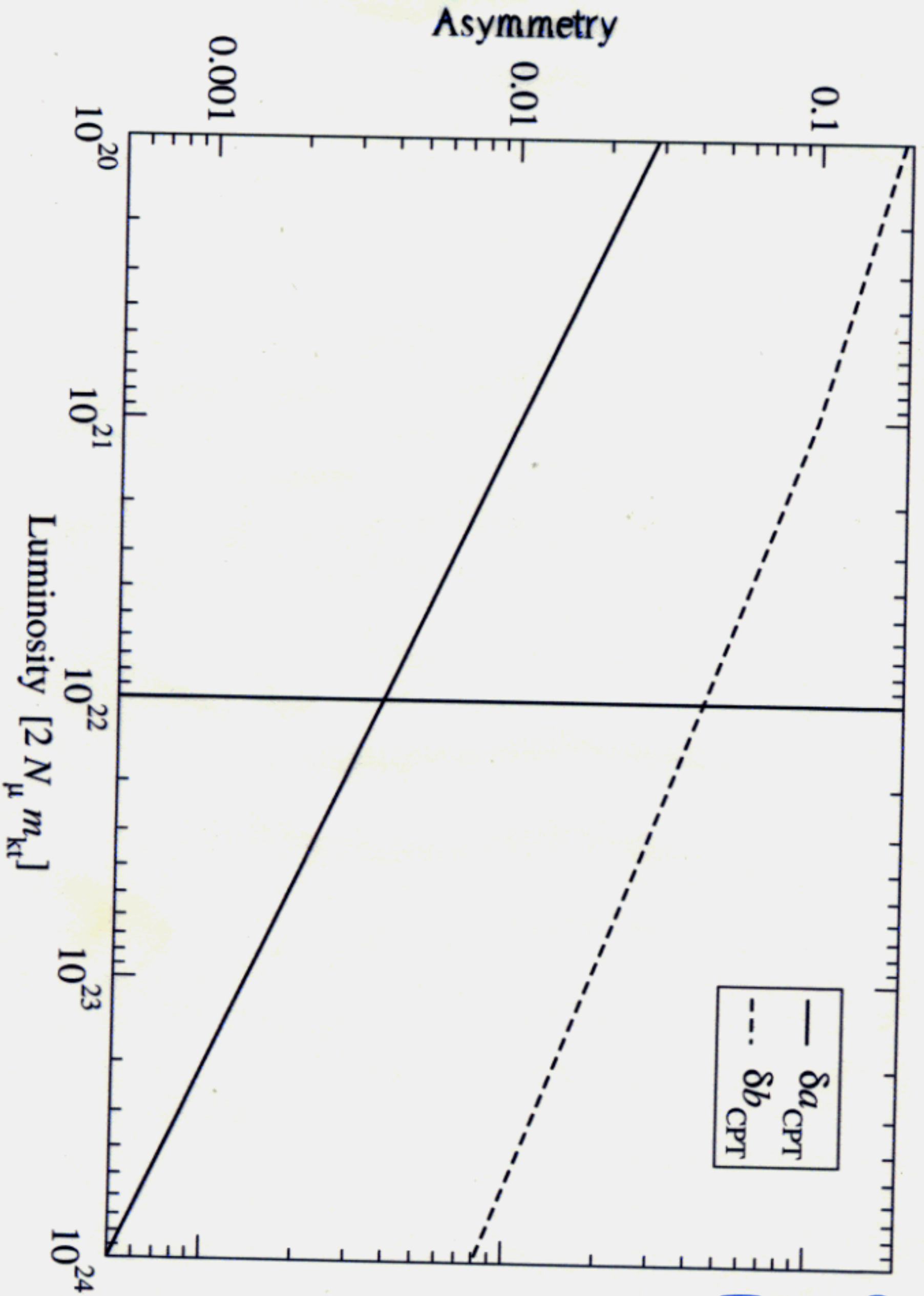
(2)

P. Huber

Sensitivity to CP-Violation at $\delta_{CP} = +\pi/2$ 

dependence
on Δm_{21}^2
is strong

Figure 21: The sensitivity to CP violation for $\delta_{CP} = +\pi/2$ at the 90% confidence level, plotted as function of $\sin^2 2\theta_{13}$. The plot shows the ranges of the sensitivity to CP violation for several values of Δm_{21}^2 , where the top row corresponds to the lower bound, the bottom row to the upper bound, and the middle row to the best-fit value of the LMA region. If no bar is drawn for an experiment, it does not have any CP violation sensitivity. For the parameters, the choose the LMA values.



$$a_{CPT} \equiv \frac{|m_3 - \bar{m}_3|}{(m_3)_{\text{average}}}$$

$$b_{CPT} \equiv \frac{|\theta_{23} - \bar{\theta}_{23}|}{(\theta_{23})_{\text{average}}}$$

difference
for ν & $\bar{\nu}$

Y. Y. Y. Wong
(黃婉瑩)

$$H = U \text{diag}(E_j) U^{-1} + \text{diag}(A, 0, 0) + 2E|\phi|U_G \text{diag}(\gamma_j) U_G^{-1}$$

[23]

$\gamma_j \neq 1$: different grav. coupl.

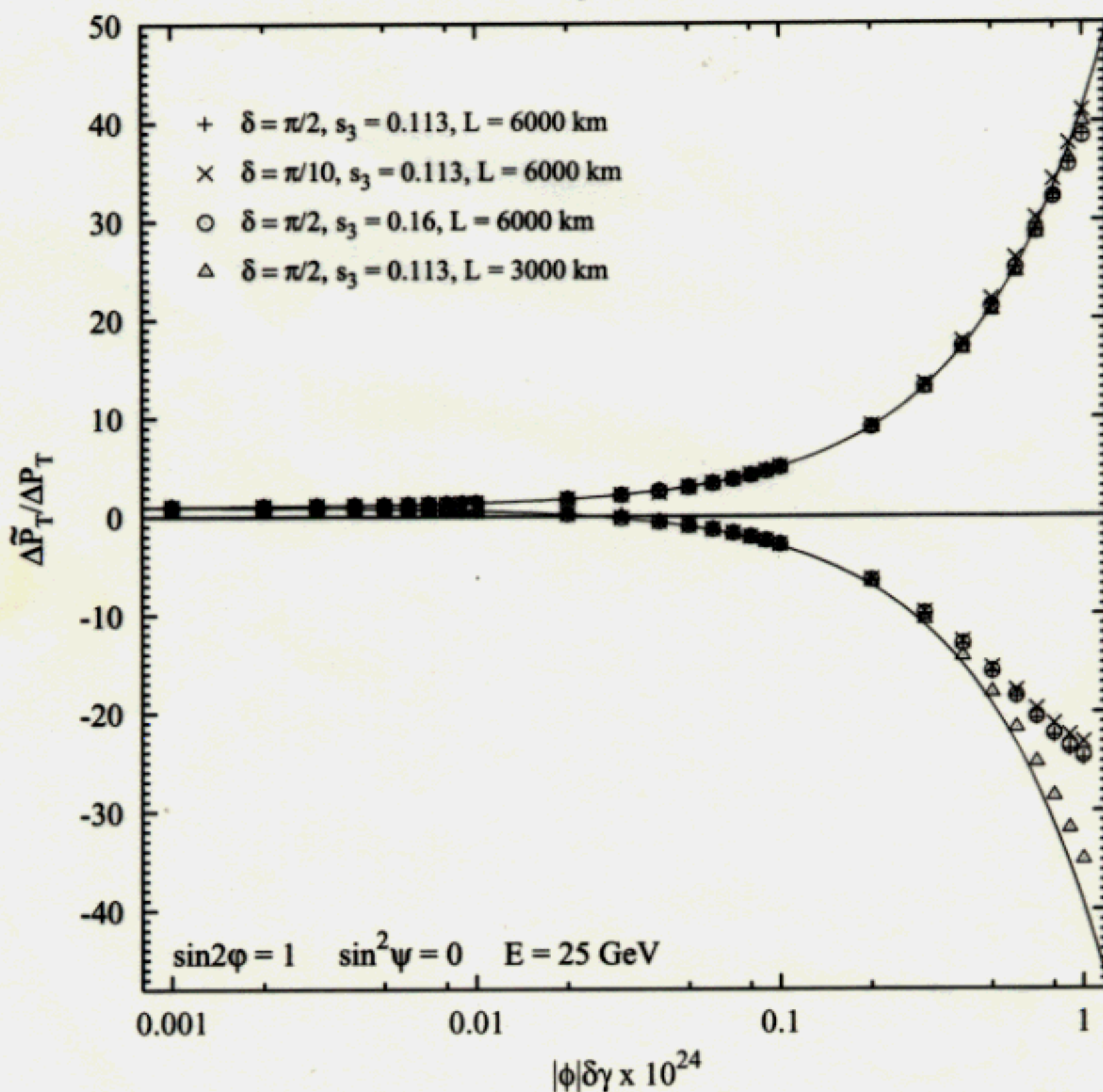
$N_\nu = 3$

Assume $|\Delta\gamma_{32}| \gg |\Delta\gamma_{21}|$ other phases $\rightarrow 0$

w/ violation of equivalence principle

$$\frac{\Delta \tilde{P}_T}{\Delta P_T} = 1 - \frac{4E^2}{\Delta m_{21}^2} \frac{\sin 2\theta_{\text{atm}}}{\sin 2\theta_0} \cdot |\phi| \Delta\gamma \sin 2\varphi$$

T violation gravitational potential



◦ New exotic interactions

J. Sato (佐藤 丈)

M. Campanelli

$$\mathcal{L}_{\text{new}} = \lambda (\bar{e} \gamma^\mu \mu) (\bar{\nu}_\mu \gamma_\mu \nu_\beta) \quad \beta \neq e$$

gives the same signal w/ ν osc.

$$U \text{diag}(E_1, E_2, E_3) U^{-1} + \text{diag}(A, 0, 0) \\ + V \begin{pmatrix} \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix}$$

However the energy dependence
is different from ν osc.

◇ For $(V - A)(V - A)$ interaction type

■ In $\nu_\alpha \rightarrow \nu_\beta$, the effects induced by $\epsilon_{\alpha\beta}^{s,m}$. The others are too small or easy to be absorbed into the error of the oscillation parameters.

■ The expected sensitivity is $\epsilon \gtrsim \mathcal{O}(10^{-4})$.

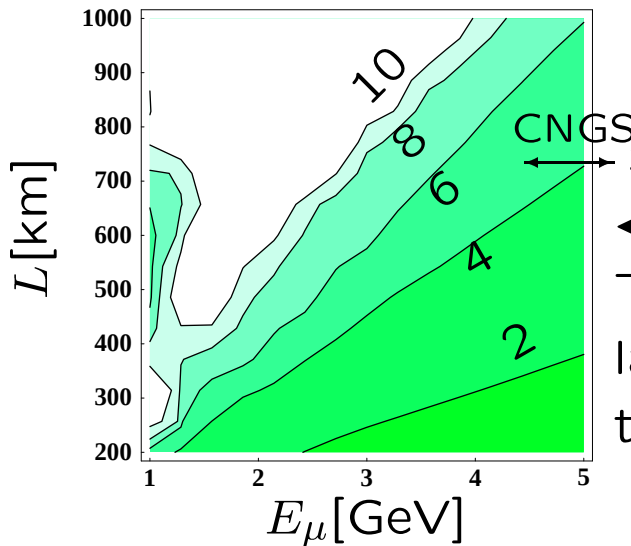
	$\epsilon_{e\mu}^{s,m}(\epsilon_{\mu e}^s)$	$\epsilon_{e\tau}^{s,m}$	$\epsilon_{\mu\tau}^{s,m}$
$\nu_e \rightarrow \nu_\mu$	△	△	×
$\nu_\mu \rightarrow \nu_\mu$	×	×	○
$\nu_e \rightarrow \nu_\tau$	×	○	△
$\nu_\mu \rightarrow \nu_\tau$	×	△	○
$\nu_\mu \rightarrow \nu_e$	△	×	×
$\nu_e \rightarrow \nu_e$	×	×	×

◇ In many models $\epsilon_{\mu\tau}$ is large.

→ τ appearance is important !

The CNGS experiments will be able to detect the new interactions with $\epsilon \gtrsim \mathcal{O}(10^{-2})$, depending on their phases.

Using the conventional beam: $\nu_\mu \rightarrow \nu_\tau$ channel



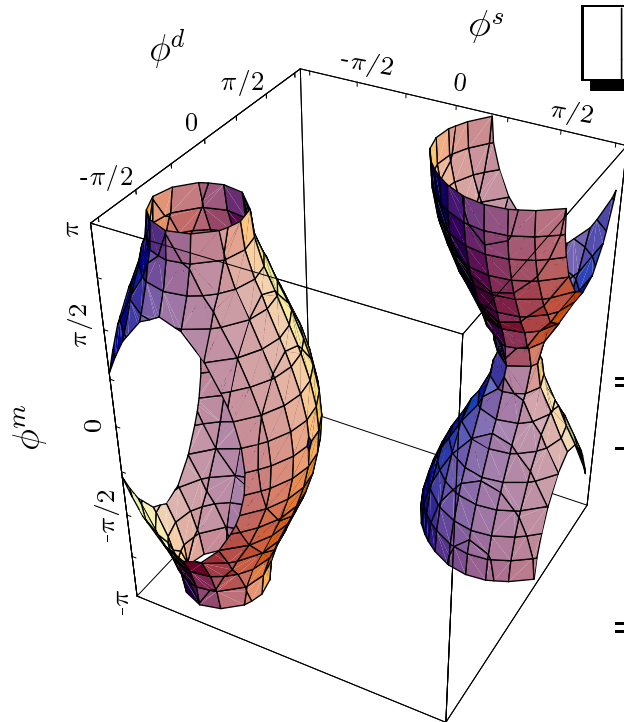
$$\epsilon_{\mu\tau}^s = 3 \times 10^{-3} i$$

$$\epsilon_{\mu\tau}^m = 0$$

◀ The unit is 10^5 neutrinos. This is the $\mathcal{O}(10^2)$ times larger exposure than that of the current experiments.

ICARUS and OPERA:

◊ Low statistics make a study of the energy spectra infeasible. We compare the total event number made by the new interaction with the error.



$$\epsilon_{\mu\tau}^s = \epsilon_{\mu\tau}^m = \epsilon_{\mu\tau}^d = 0.01$$

◀ The contour denotes that the effect made by new interactions is as large as the 1σ error.

	N_τ^{SM}	σ_{sys}^2	σ_{tot}
ICARUS-A	40.4	11	7.4
ICARUS-B	23.5	1.5	5.2
OPERA	16.3	0.75	4.3

[27] M. Campanelli

Use the energy spectrum of the wrong sign μ on's from $\tau \rightarrow \mu$ decays.

$\sin^2 2\theta$

$$U \text{diag}(E_j) U^{-1} + \text{diag}(A, 0, 0)$$

$$+ V \begin{pmatrix} \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix}$$

