

How far does a particle travel at a particular energy?

Case 1: After the ion source i.e. at 60 keV

To calculate the distance travelled we need to know the velocity and time.

Time is the easier one so:

One RF period takes $\frac{1}{324 \times 10^6} = 3.09 \times 10^{-9}$ seconds

Calculating the **velocity** of a particle at 60keV:

Kinetic energy = $\frac{1}{2} mv^2$

Therefore, $v = \sqrt{2 \times (K.E.)}$

$$K.E. = \frac{\text{Beam energy} \times (1 \times \text{electron charge})}{\text{Mass of particle}}$$

Where, mass of particle = mass of proton + mass of 2 electrons

(we can ignore electron mass because it is 1/2000th of proton mass)

So,

Beam energy = 60×10^3 eV

Electron charge = 1.602×10^{-19} Coulomb

Mass of particle = 1.67×10^{-27} kg

$$\text{Therefore, } v = \sqrt{\frac{2 \times (60 \times 10^3) \times (1.602 \times 10^{-19})}{1.67 \times 10^{-27}}}$$

$v = 3.39 \times 10^6$ m/s (or 7 million miles per hour) (for comparison $c = 300 \times 10^6$ m/s)

Distance = velocity x time

= $(3.39 \times 10^6) \times (3.09 \times 10^{-9})$

= 0.0105m

Answer: The distance travelled in one RF period by a H- particle at 60keV is **10.5mm**

Case 2: After the RFQ i.e. at 3 MeV

Particle velocity = 24×10^6 m/s

Distance travelled during 3.09×10^{-9} seconds at 3 MeV = 0.074m or **74mm**