

# A and DA tracking in NuFact muon chain - status -

F. Méot  
CEA & IN2P3  
LPSC, Grenoble

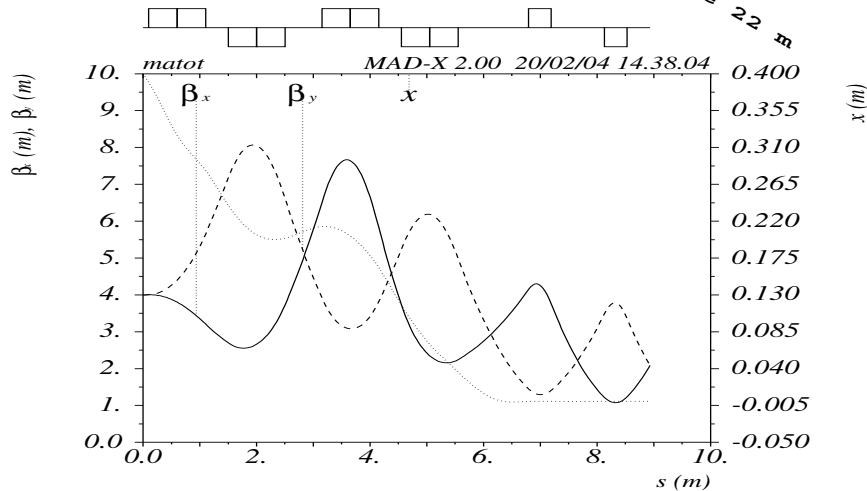
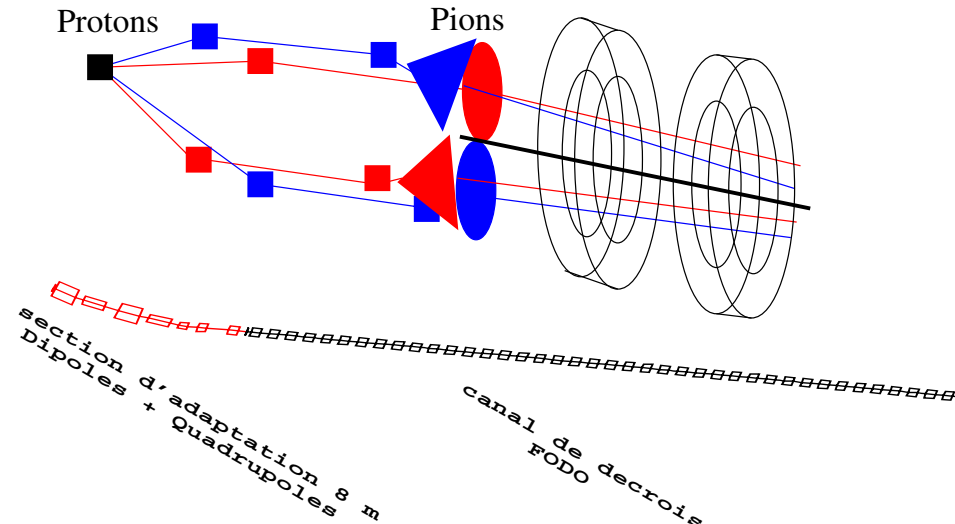
## Contents

1	<b>Muon front end</b>	<b>2</b>
2	<b>Acceleration, US-Study2a FFAG optics</b>	<b>4</b>
3	<b>Acceleration, NuFact-J optics</b>	<b>9</b>
4	<b>Acceleration, RAL isochronous FFAG</b>	<b>11</b>
5	<b>Muon storage ring, triangle</b>	<b>15</b>
6	<b>Muon storage ring, bowtie</b>	<b>17</b>
7	<b>Conclusions</b>	<b>19</b>
8	<b>Bibliography</b>	<b>20</b>

# 1 Muon front end

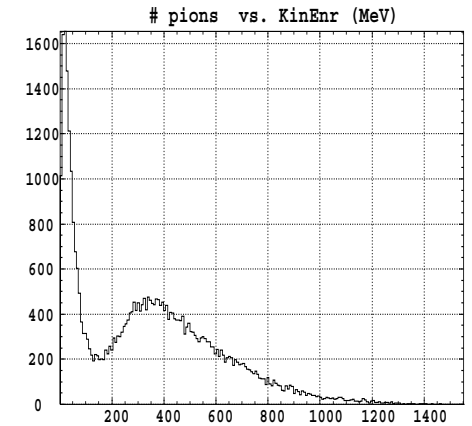
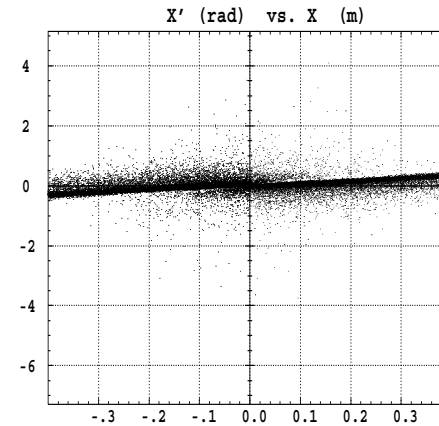
In the 2002-2004 period a muon front end has been studied at CERN, based on a quadrupole funnelling channel (in view of a 4-target system, aimed at decreasing the power on each target), and on a quadrupole collect channel. Transmission of  $\pi/\mu$  beam over the 32 meter long structure has been optimized.

Transmission through a 30 m long purely solenoid channel with optimized field, has been computed for comparison.

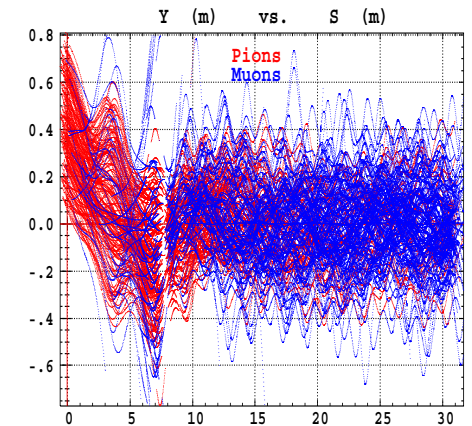
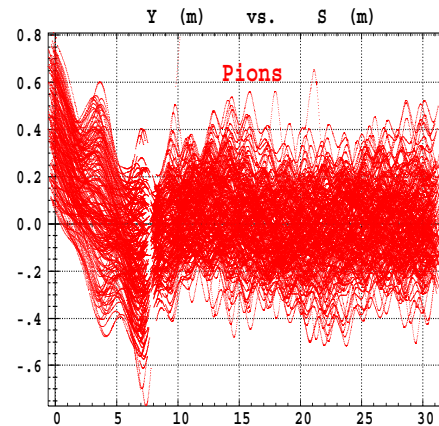


Optical functions and beam centroid orbit in funnel, from horn exit ( $s = 0$ ) to entrance of collect channel ( $s = 10$  m).

MARS distributions at horn exit are used.

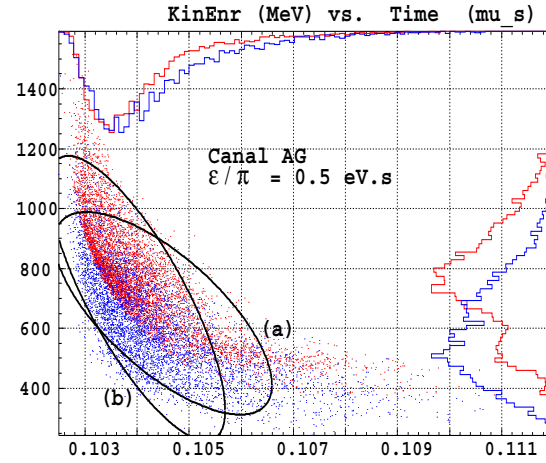
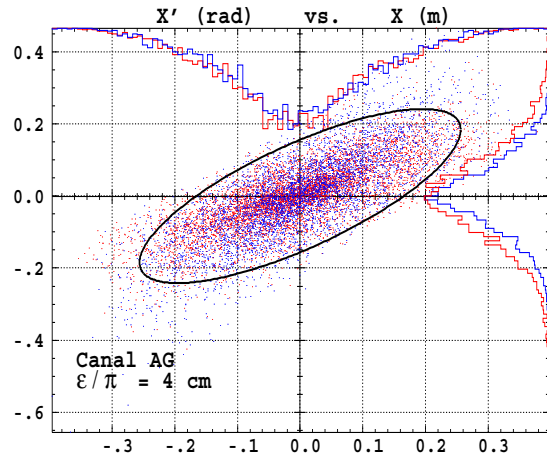


Aperture diameters are 80 cm in funnel, 40 cm in collect channel.

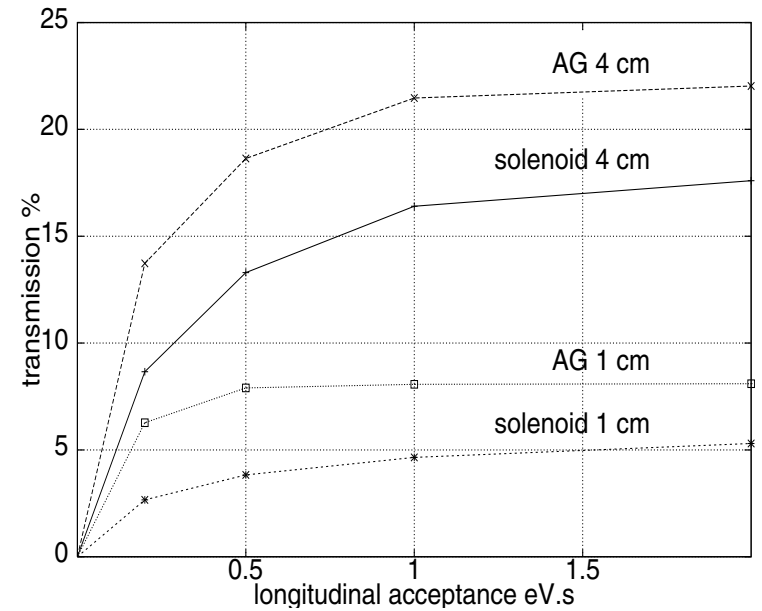
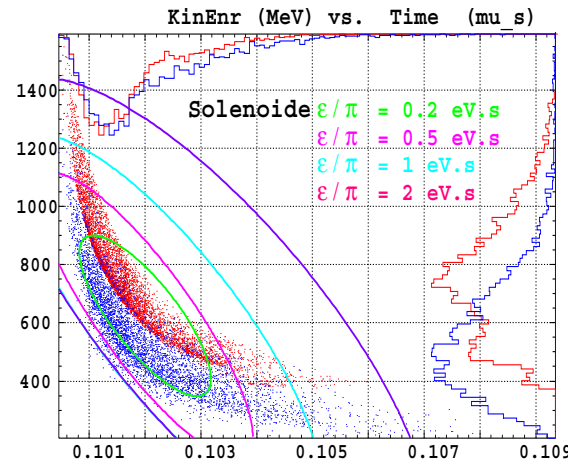
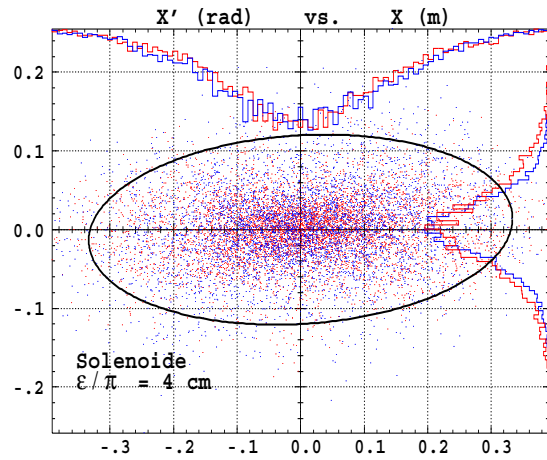


**Optimization of transmission :**

- counting through transverse ellipses ( $\pi$  or  $4\pi$ , geometrical) and longitudinal ellipses ( $0.2 - 2$  eV.s) are maximized,
- fit variables are ellipse shape and positioning, and optical parameters (magnetic fields, etc.).
- apertures are fixed, 40 cm in solenoid, 40 cm in quadrupole channel, 80 cm in funnel.



**Funnel + quadrupole channel, 32 m long.**



**Transmission.**

**Full solenoid channel, 30 m long.**

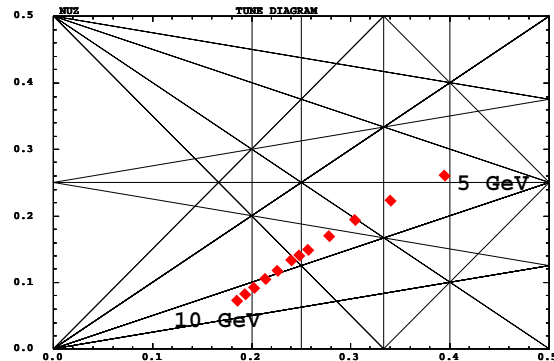
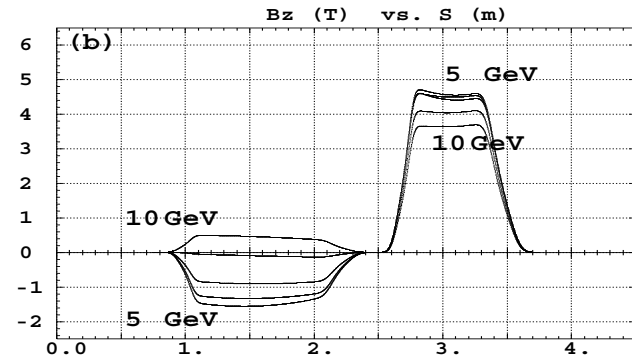
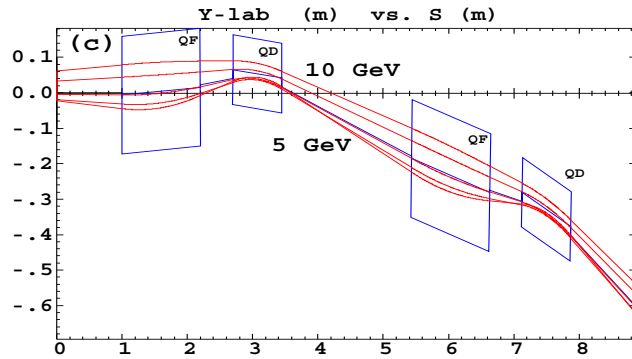
## 2 Acceleration, US-Study2a FFAG optics

DA in 10→20 GeV NuFact-J scaling FFAG rings has been tracked. Cells of concern are shown below. All characteristics accounted for in these simulations are those given on web ISS-NuFact webpage.

Linear FFAG optics of concern :

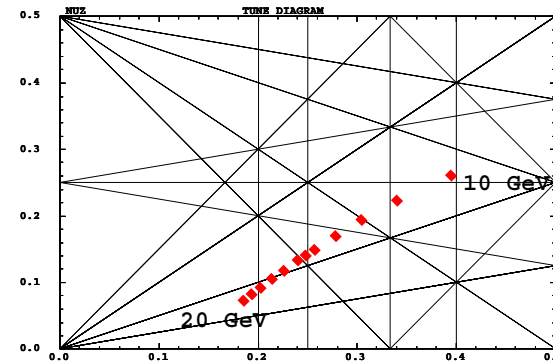
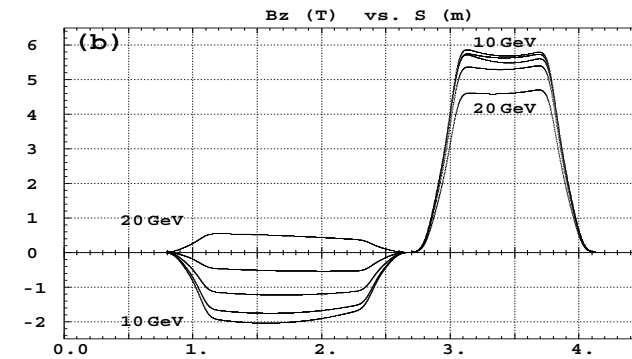
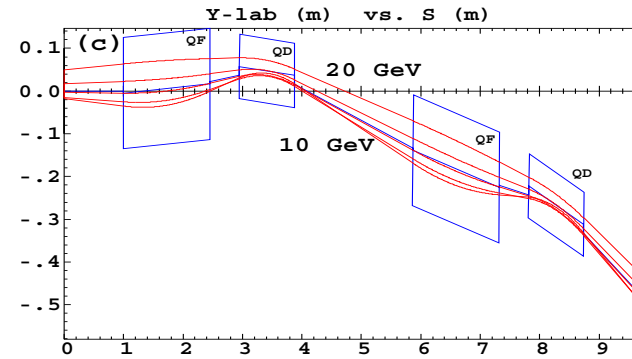
5-10 GeV

64 cells, 284 m circ., 10.3 turns

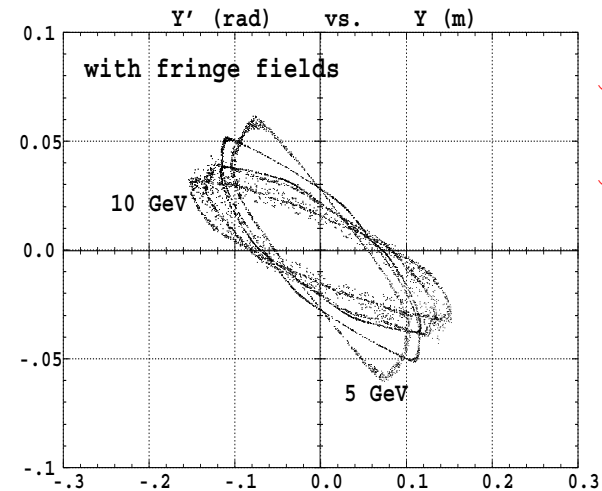
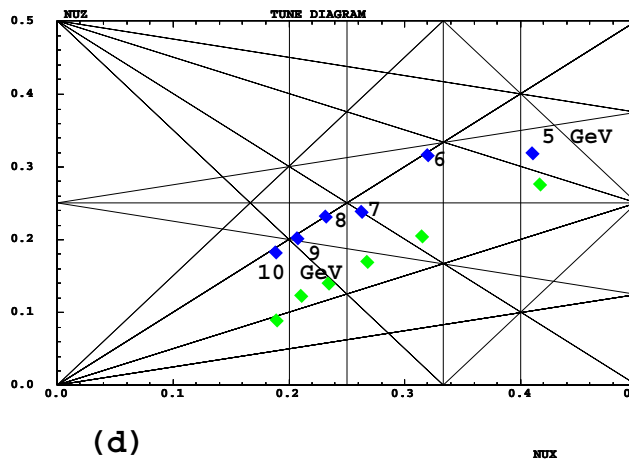
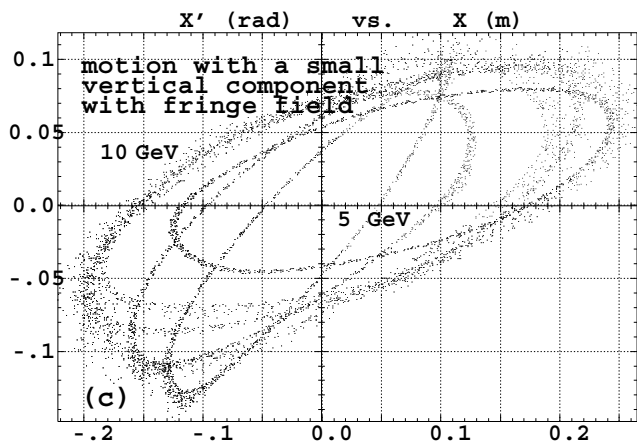
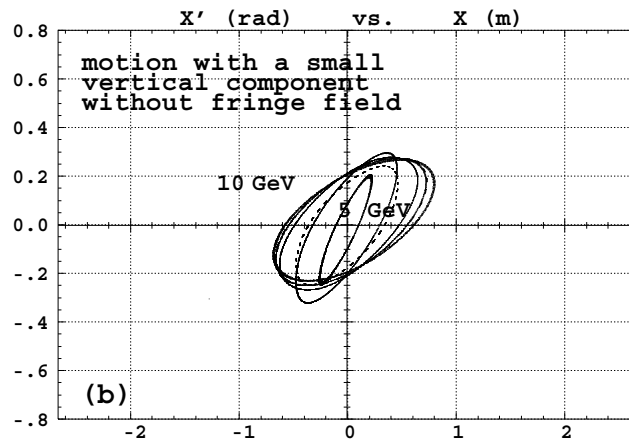
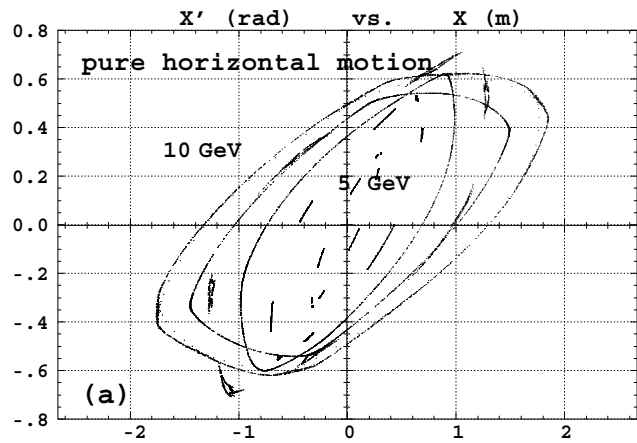


10-20 GeV

84 cells, 409 m circ., 15.5 turns



# 5-10 GeV

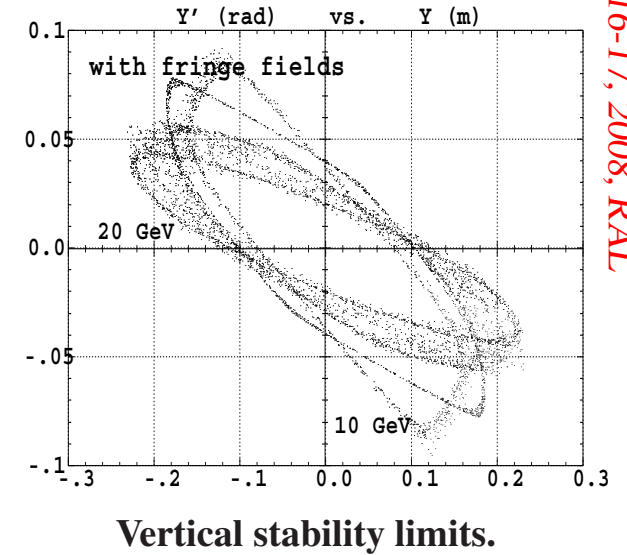
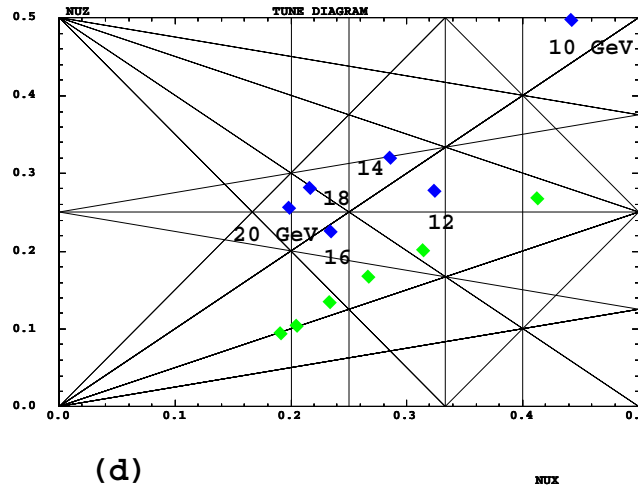
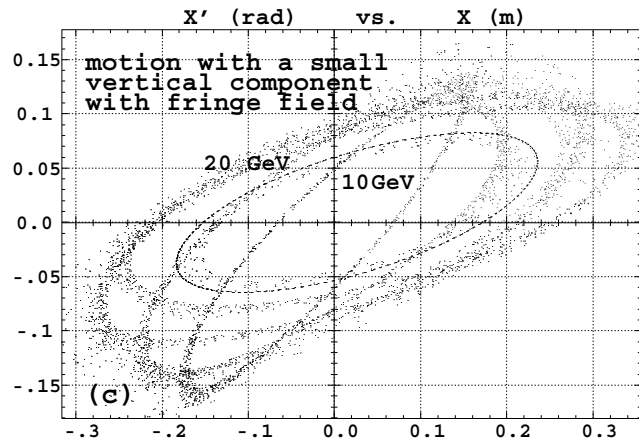
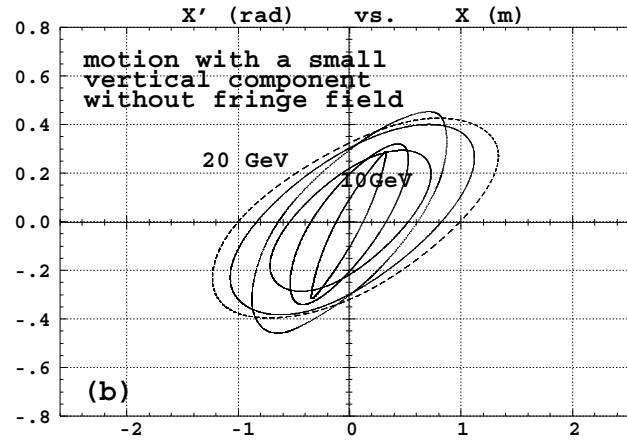
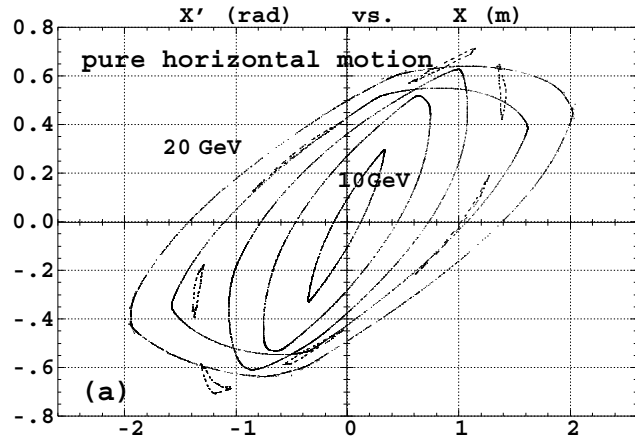


**Vertical stability limits.**

**Horizontal stability limits for energies 5,6,7,8,9,10 GeV.**

**(a) and (b) : hard edge. (c) : fringe fields set. Note the different scales in (c).  
Qx-Qz path : green squares correspond to (b), blue squares correspond to (c).**

# 10-20 GeV

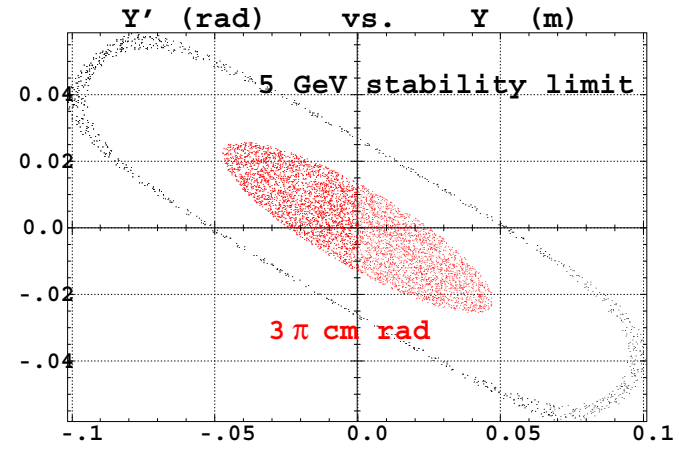
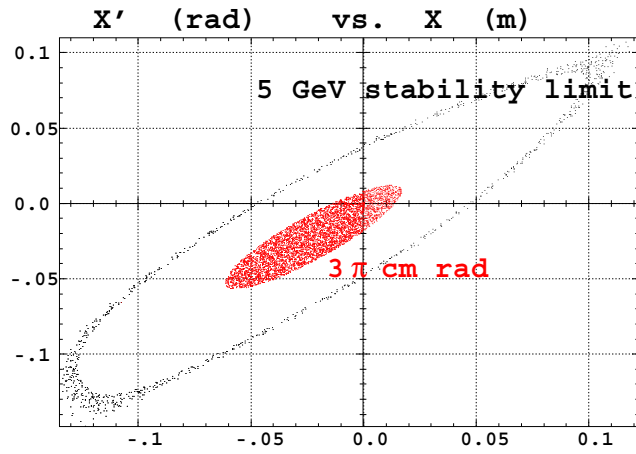


**Horizontal stability limits for energies 10,12,14,16,18,20 GeV.**

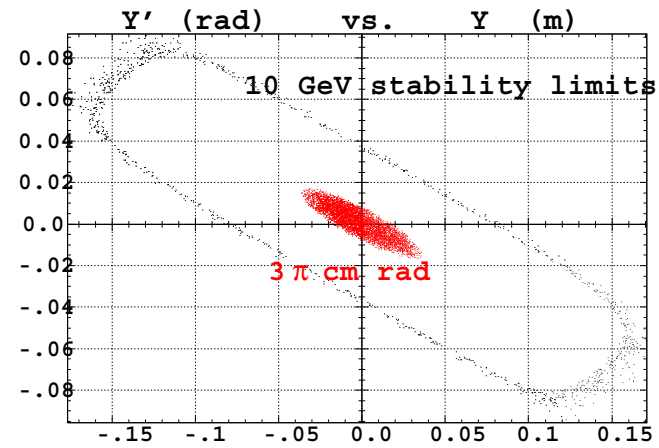
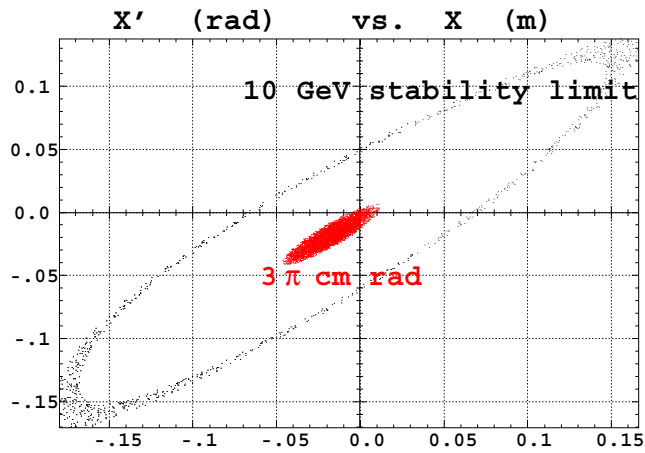
(a) and (b) : hard edge. (c) : fringe fields set. Note the different scales in (c).

Qx-Qz path : green squares correspond to (b), blue squares correspond to (c).

### 5-10 GeV



### 10-20 GeV



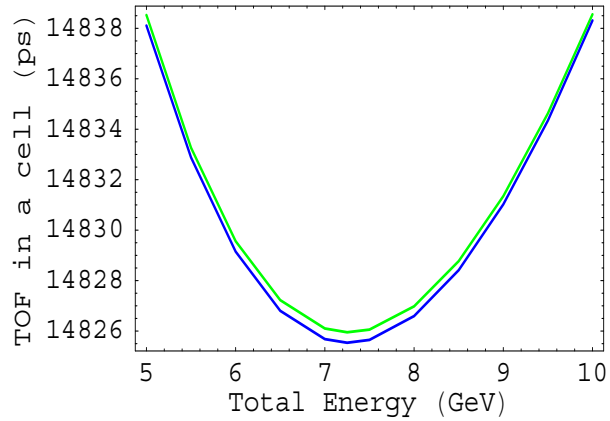
The  $3\pi$  cm beam, inscribed in horizontal and vertical stability limits.



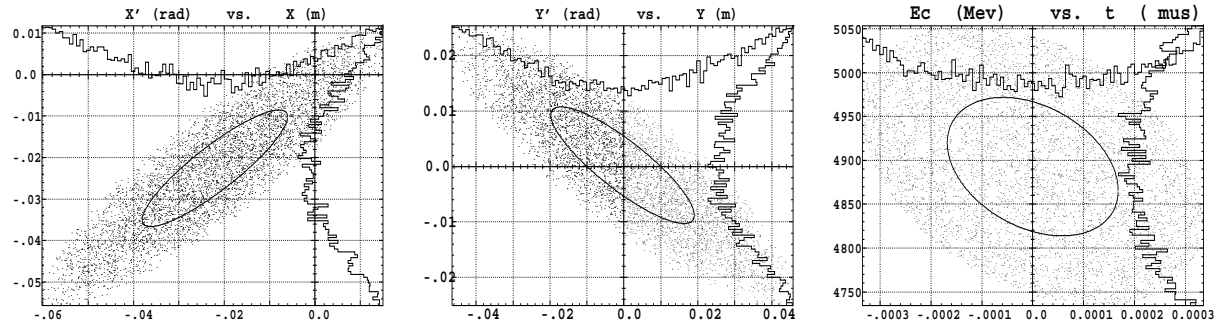
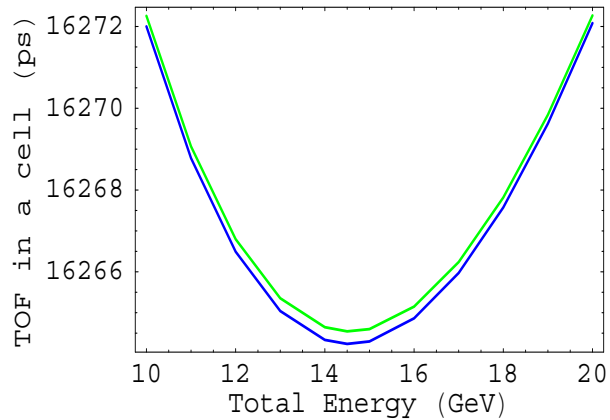
**Acceleration of a  $3 \pi$  cm rad and  $\epsilon_l = 0.05 \pi$  eV.s bunch :**

**TOF parabola**

**FFAG 5-10 GeV**



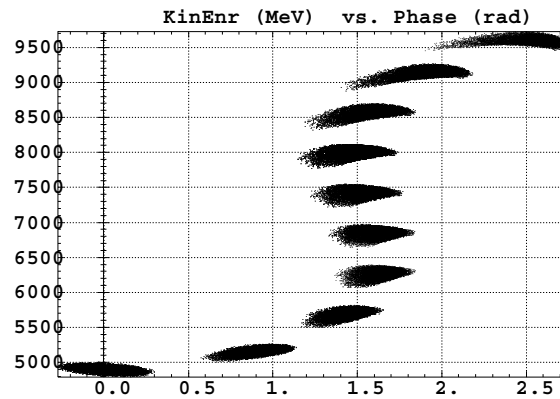
**FFAG 10-20 GeV**



**5 GeV distribution of 5000 muons, in normalized emittances  $3 \pi$  cm rad and  $\epsilon_l = 0.05 \pi$  eV.s.**

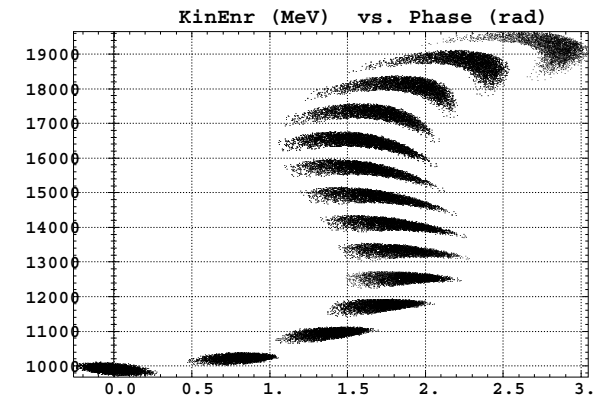
**FFAG 5-10 GeV**

**10.3 turns**



**FFAG 10-20 GeV**

**15.5 turns**



**Longitudinal motion of the 5000 muons during the acceleration cycle.**

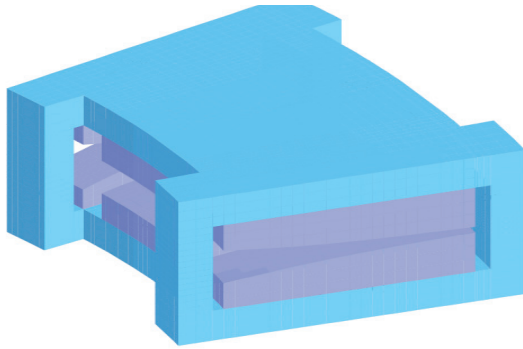
**100% transmission is observed in both rings (no decay).**



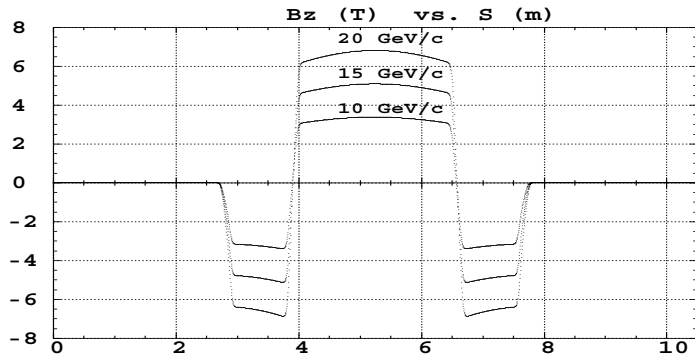
### 3 Acceleration, NuFact-J optics

DA in 10→20 GeV NuFact-J scaling FFAG rings has been tracked. Magnet of concern is shown below. All characteristics accounted for in these simulations are NuFact-J Report ones, also available on web ISS-NuFact webpage.

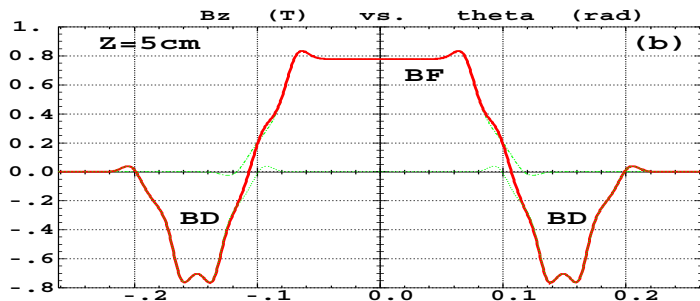
120 cells, k=280, R=200 m, 6 T in dipole



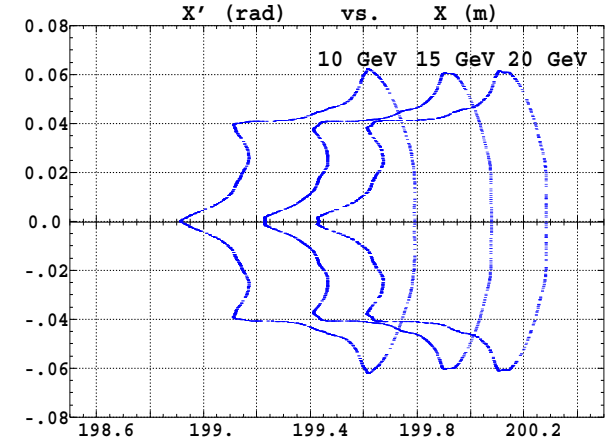
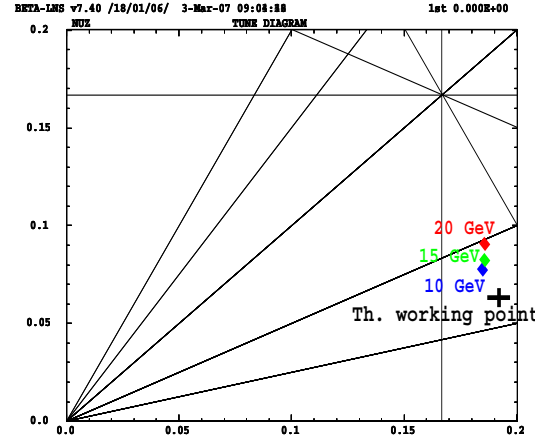
Type of magnet considered in this DA study.



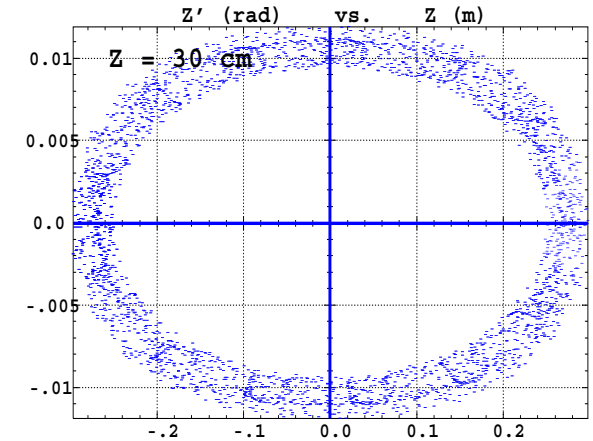
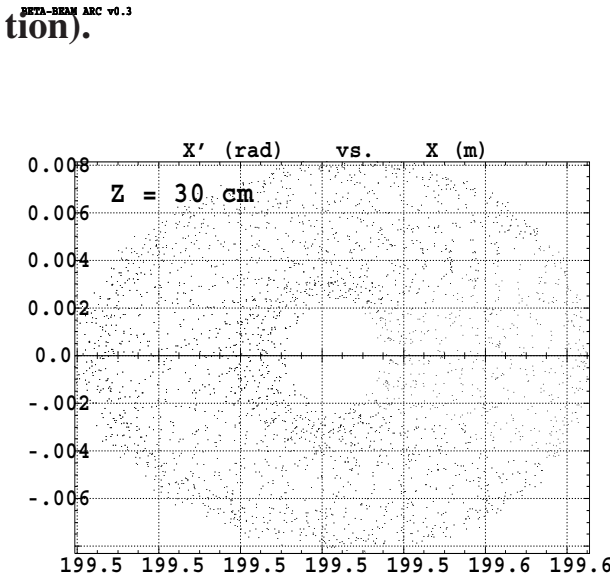
Typical field on closed orbits, in mid-plane.



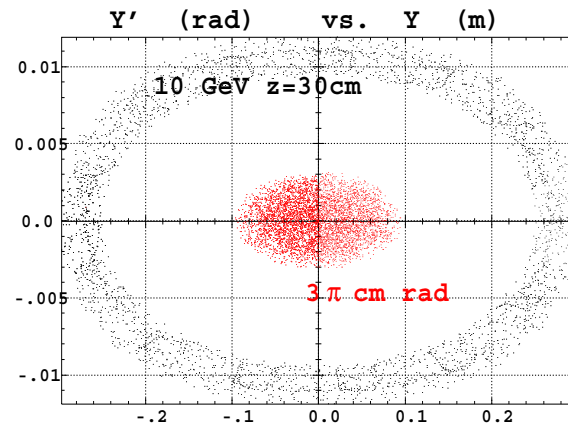
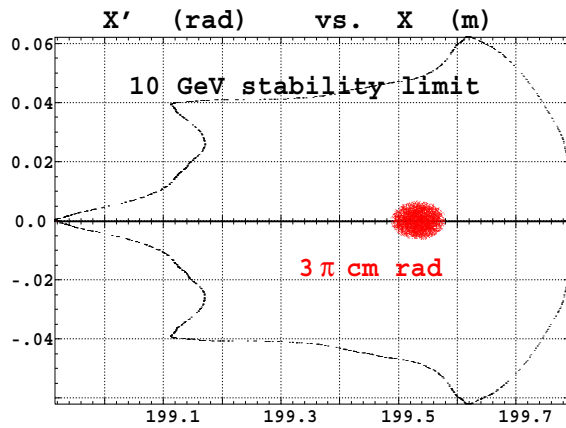
Off mid-plane field behaves ok...



Tunes on DAs (left) at 10, 15 and 20 GeV, and horizontal DAs (pure H motion).



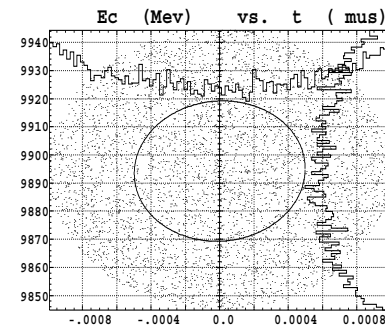
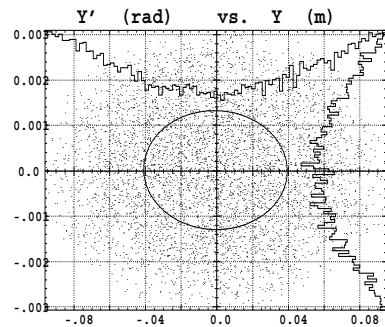
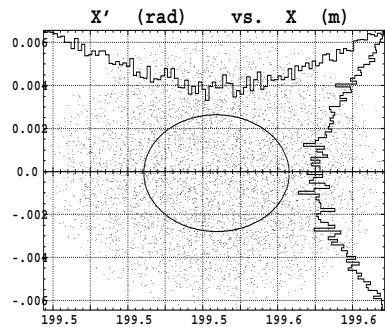
Horizontal motion induced (left), for a 10 GeV particle launched on  $z_0 = 30$  cm (right). Donuts due to proximity of  $Q_x = 2Q_z$  are stable, an indication of symplectic behavior.



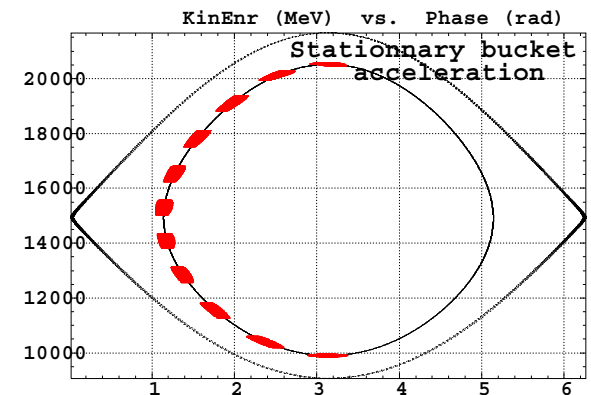
Transverse normalized emittances  $\epsilon_{N,x,z} = 3 \pi \text{ cm rad}$  within the stability limits at 10 GeV.

### 10 → 20 GeV transmission

- taking  $\epsilon_x = \epsilon_z = 3 \pi \text{ cm, norm.}, \epsilon_l/\pi = 0.05 \text{ eV.s}$  (by far too small, needs be re-visited)
- we get 100% efficiency (regardless of decay) :



Initial distributions in  $\epsilon_{N,x,z} = 3 \pi \text{ cm rad}$  and  $\epsilon_l = 0.05 \pi \text{ eV s}$ .



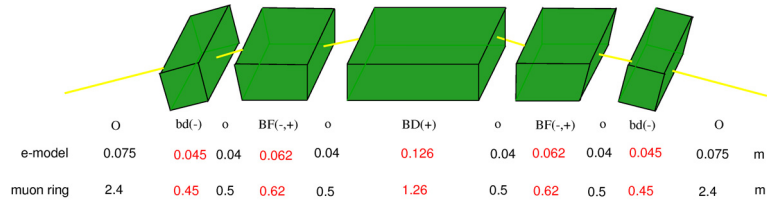
Muon acceleration in stationary bucket.

# 4 Acceleration, RAL isochronous FFAG

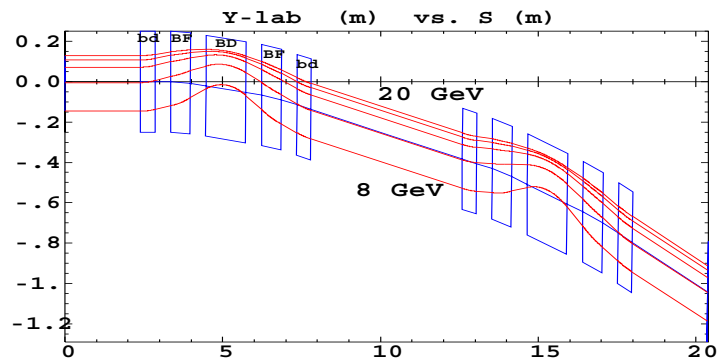
DA in 8→20 GeV isochronous FFAG has been tracked.

Machine parameters are the following :

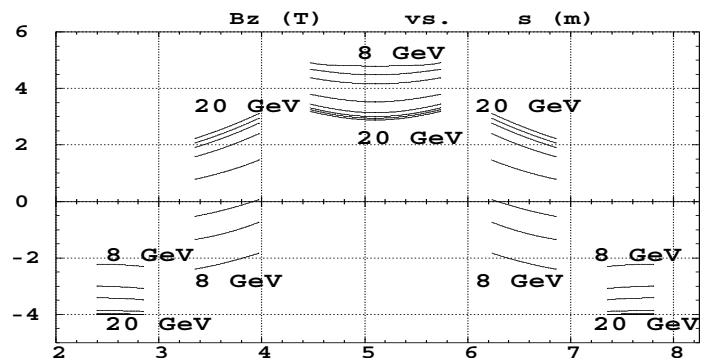
123 cells, circumference 1255 m, acceleration in 16 turns using 201 MHz, 18.3 MV RF, 1 cavity/3 cells.



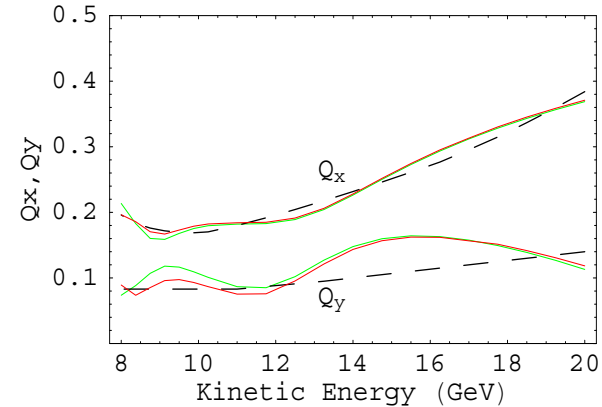
**Isochronous cell.**



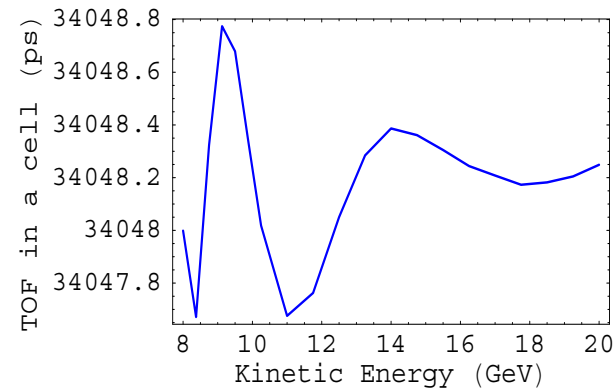
**Closed orbits**



**Magnetic fields along the closed orbits**  
(we used hard edge model).

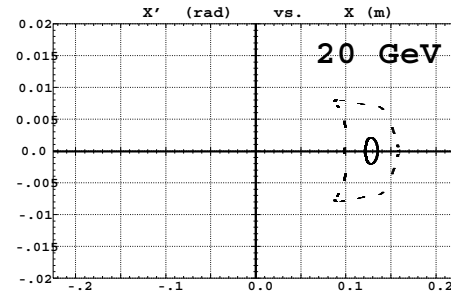
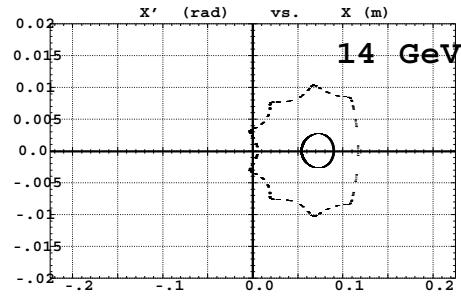
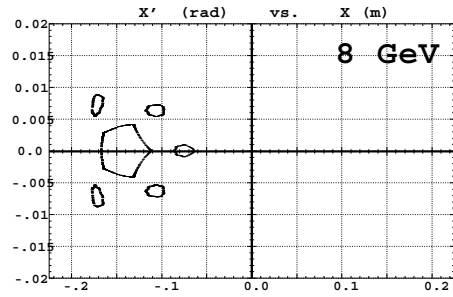


**Tunes.**

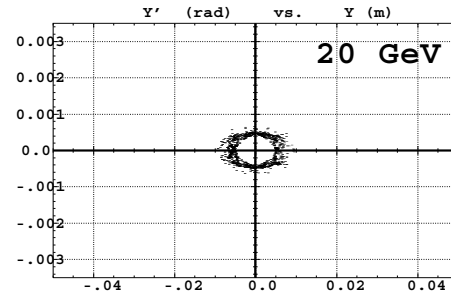
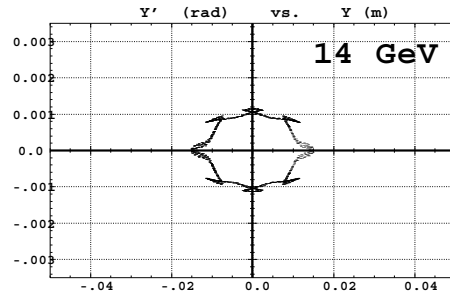
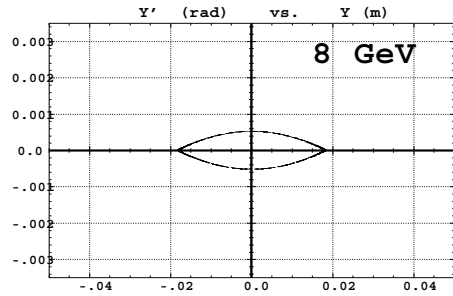


**Time of flight** (excursion about 1/10 that in linear FFAG optics).

**Horizontal stability limits, 8, 14 and 20 GeV :**

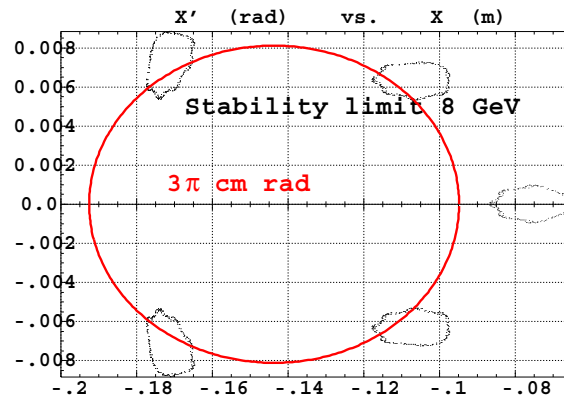


**Vertical stability limits, 8, 14 and 20 GeV :**

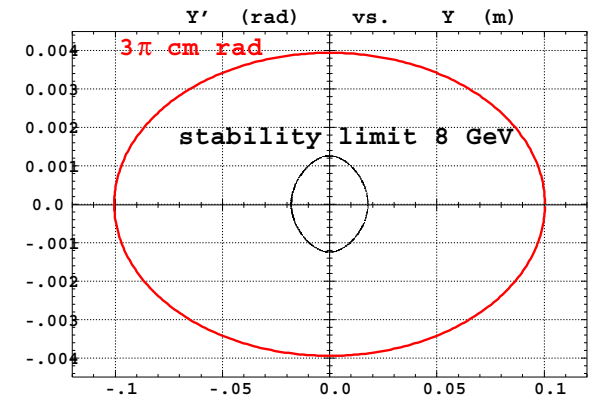


**Comparing to  $3\pi$  cm emittance (red ellipse) :**

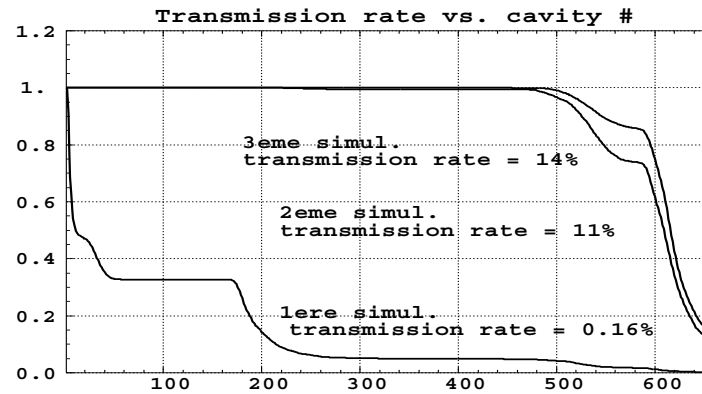
**Horizontal**



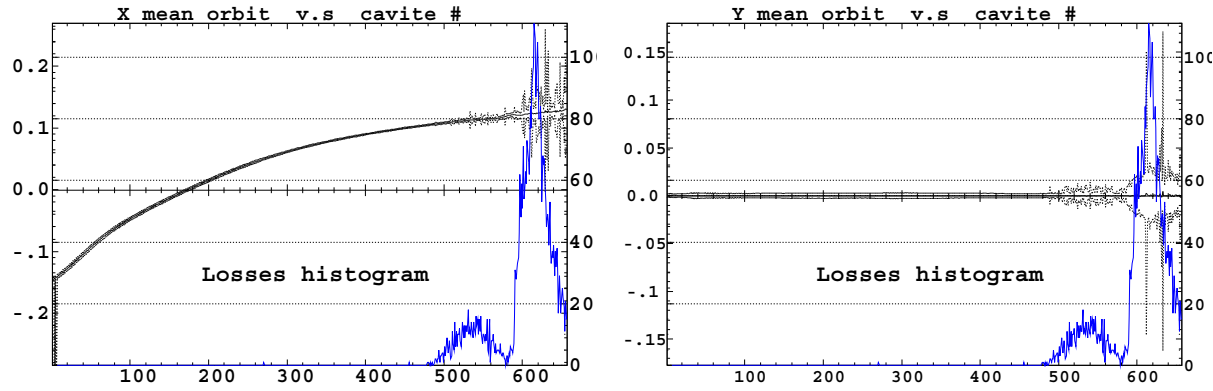
**Vertical**



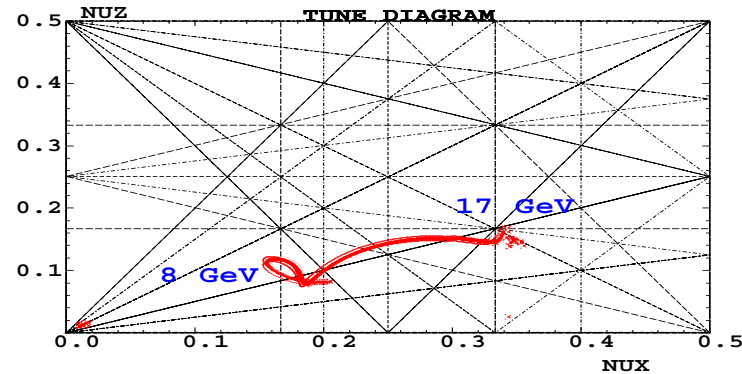
# Muon Transmission :



Transmission rate as a function of the number of passages through the cavities.  
Lossless transmission up to 17 GeV, for  $\epsilon_{N,x} \leq 2 \cdot 10^{-3} \pi \text{ cm}$ ,  $\epsilon_{N,y} \leq 0.5 \cdot 10^{-4} \pi \text{ cm}$ .



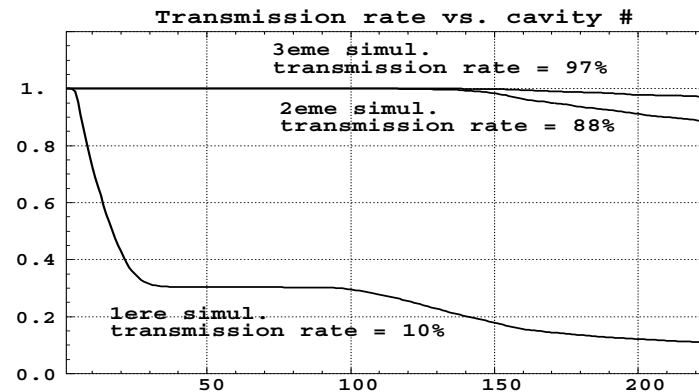
Horizontal and vertical beam envelopes and histograms of the muons losses.



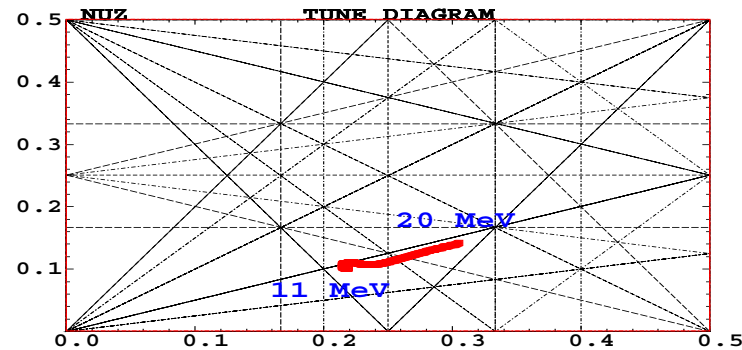
Beam trajectory in the tune diagram  
(regular systematic resonances up to the 6th order shown).

Notes :

**(i) case of the 11-20 MeV electron model**



Transmission rate as a function of the number of passages through the cavities.



Beam trajectory in the tune diagram (regular systematic resonances up to the 6th order shown).

**(ii) optics with insertion was also proposed, lower Qz and Qx excursions, still needs be tracked**

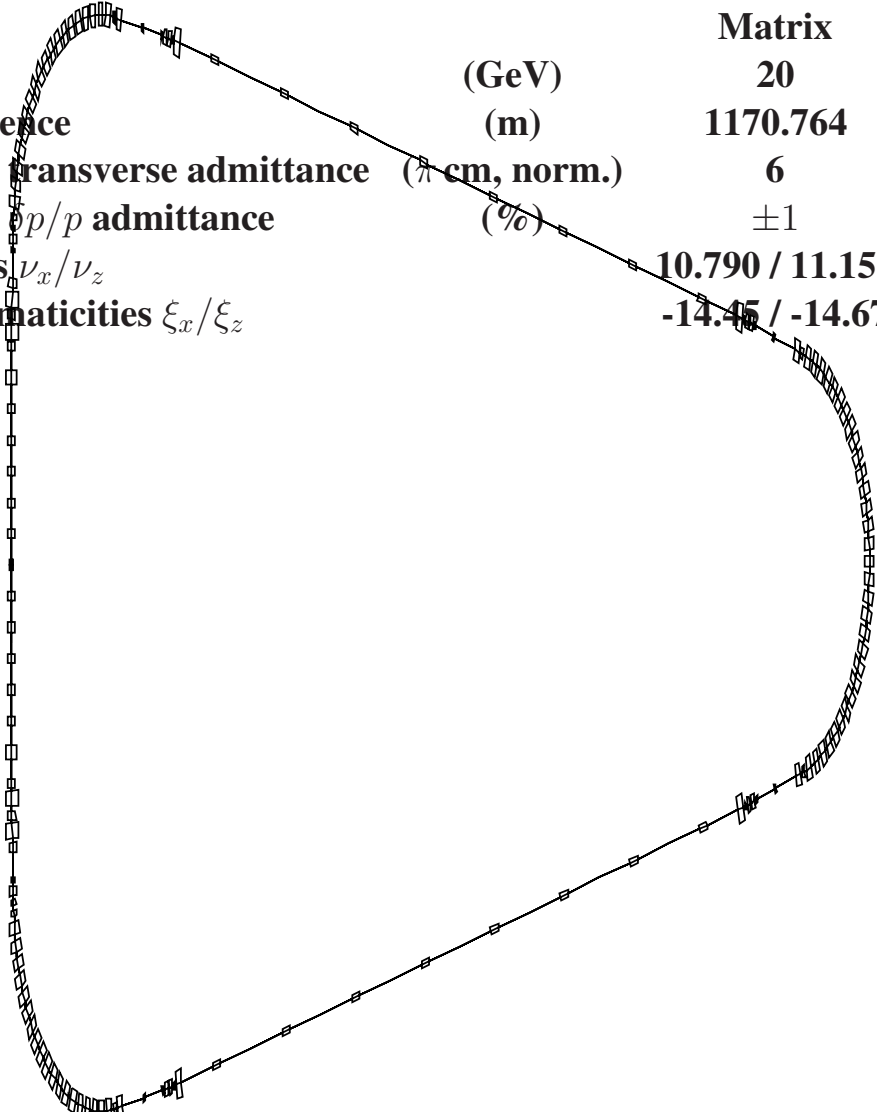


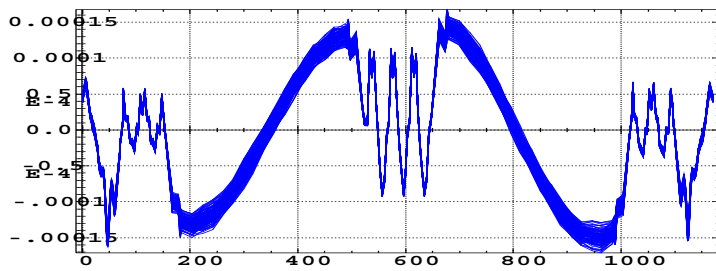
## 5 Muon storage ring, triangle

Table 1 : Muon storage ring parameters.

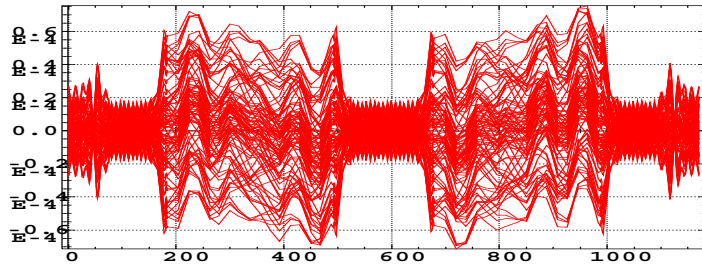
The right column gives, where worth, the stepwise ray-tracing data.

		Matrix	Ray-tracing
Energy	(GeV)	20	
Circumference	(m)	1170.764	
Requested transverse admittance	( $\hbar$ cm, norm.)	6	
Requested $p/p$ admittance	(%)	$\pm 1$	
Total tunes $\nu_x/\nu_z$		10.790 / 11.151	10.791 / 11.147
Total chromaticities $\xi_x/\xi_z$		-14.45 / -14.67	-14.35 / -14.92

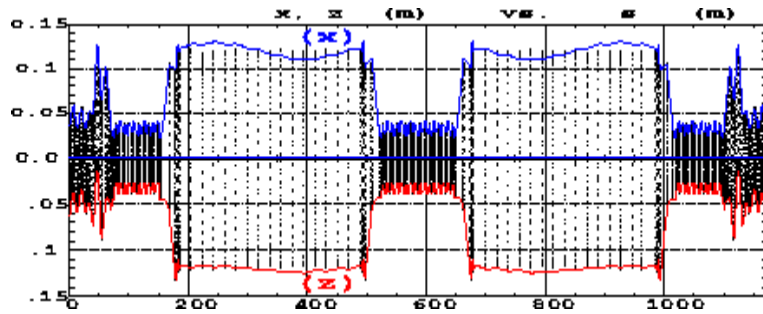




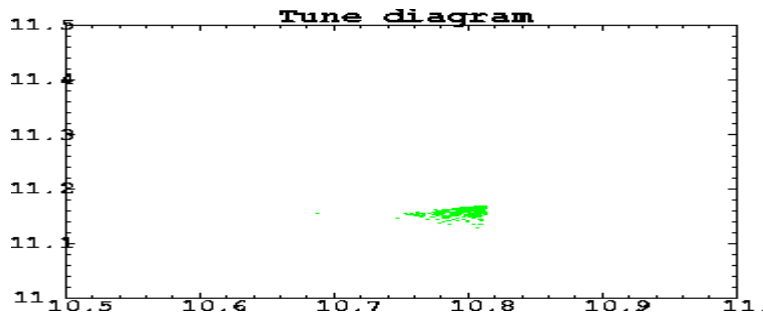
Residual H closed orbit, chromaticity corrected.



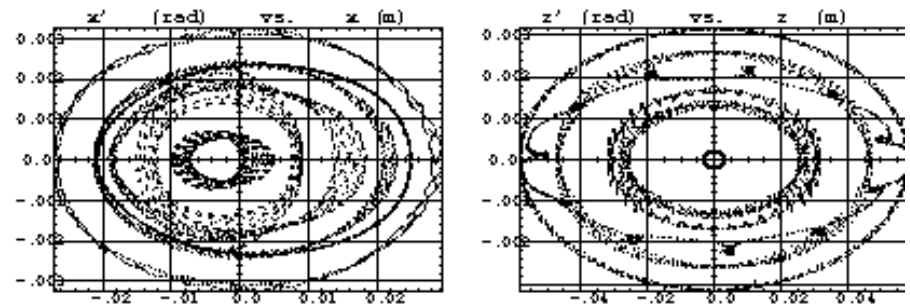
Residual V closed orbit, chromaticity corrected.



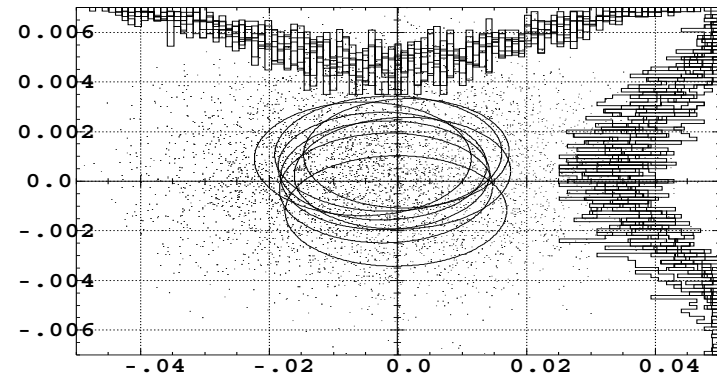
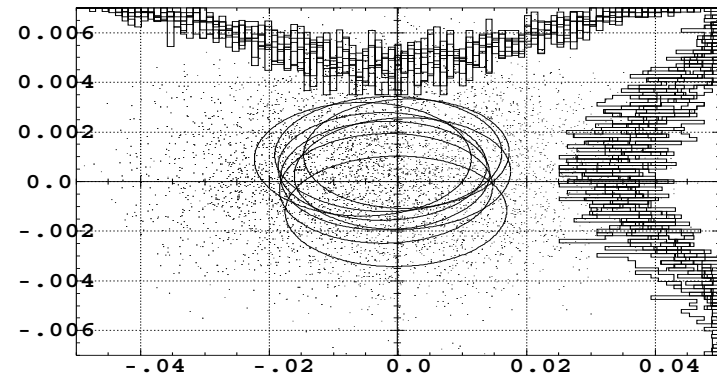
Beam envelopes,  $6\pi$  cm emittance.



Beam footprint in tune diagram, chromaticity corrected,  $6\pi$  cm emittance,  $dp/p = \pm 4\%$ .



Sample multiturn tracking, arbitrary particles with various H, V and  $\delta p/p$  conditions. It shows the good behavior of the numerical integration (no evidence for prohibitive non-symplectic behavior).



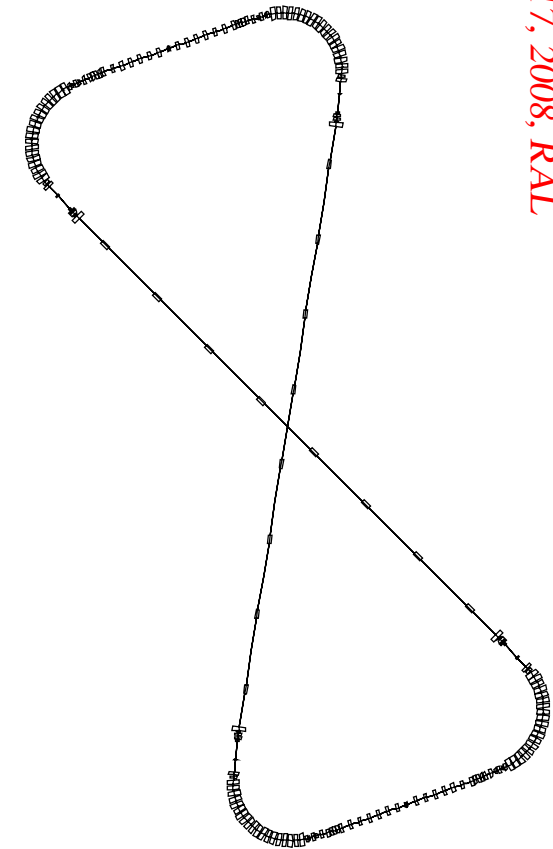
Horizontal (top) and vertical (bottom) admittance, for various sets of errors. The rms matching ellipses correspond to more than  $3\pi$  cm norm., total.

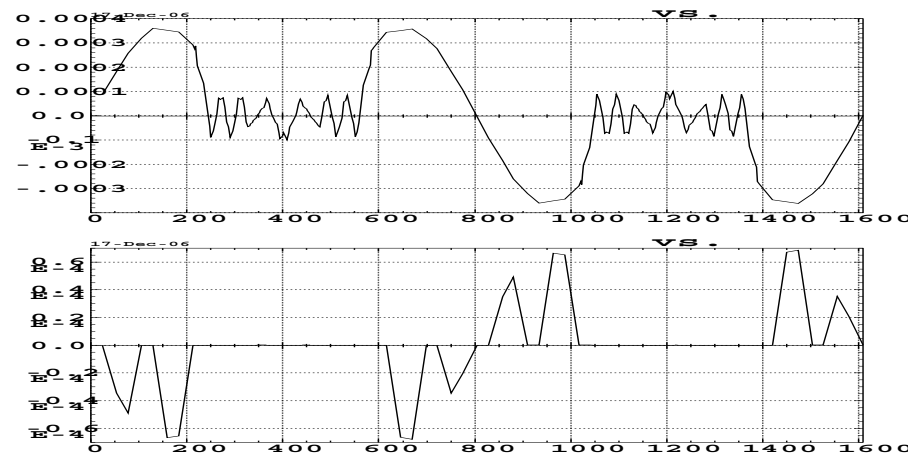
# 6 Muon storage ring, bowtie

Ray-tracing data files have been installed.

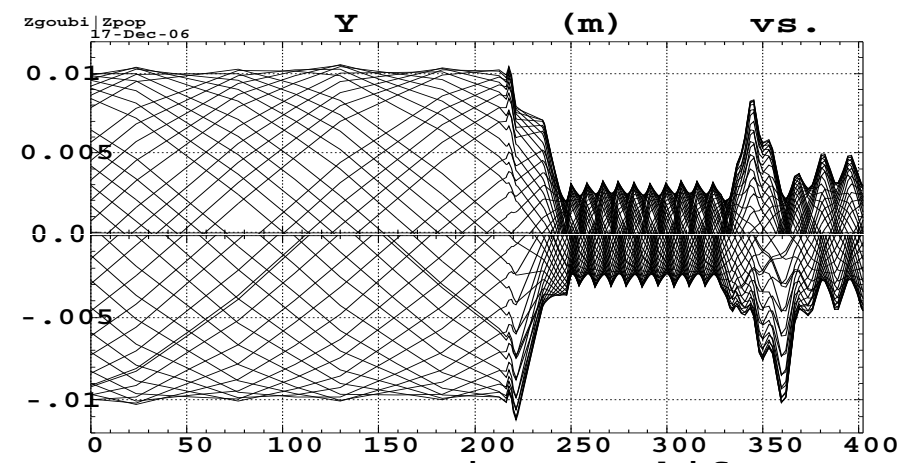
## Muon storage ring parameters.

<b>Energy</b>		<b>(GeV)</b>	<b>20</b>			
<b>Circumference</b>		<b>(m)</b>	<b>1608.8</b>			
<b>Requested transverse admittance</b>		<b>(<math>\pi</math> cm, norm.)</b>	<b>6</b>			
<b>Requested <math>\delta p/p</math> admittance</b>		<b>(%)</b>	<b><math>\pm 1</math></b>			
<b>Total tunes <math>\nu_x/\nu_z</math></b>			<b>14.3749 / 12.7882</b>			
<b>Total chromaticities <math>\xi_x/\xi_z</math></b>			<b>-17.7 / -17.7</b>			
<b>Phase advances, <math>H/V</math> :</b>		<b>(<math>2\pi</math>)</b>				
<b>Arc cell</b>			<b>0.2 / 0.2</b>			
<b>production straight</b>			<b>0.69963 / 0.69963</b>			
<b>sol./arc match section</b>			<b>0.252525 / 0.205128</b>			
<b>tuning straight</b>			<b>1.98279 / 1.284238</b>			
<b>Matching conditions :</b>	$\beta_x$	$\alpha_x$	$\beta_x$	$\alpha_z$	$D_x$	$D'_x$
<b>collimation st centre</b>	<b>8.86984</b>	<b>0</b>	<b>21.08630</b>	<b>0</b>	<b>0</b>	<b>0</b>
<b>arc input/output</b>	<b>3.78758</b>	<b>0</b>	<b>12.67568</b>	<b>0</b>	<b>0.837046</b>	<b>0</b>
<b>production st waists</b>	<b>94.21980</b>	<b>0</b>	<b>94.21980</b>	<b>0</b>	<b>0</b>	<b>0</b>





Residual geometrical closed orbits. The (negligible) vertical one is due to residual coupling in the silenoid.



Horizontal (top) and vertical (bottom) beam envelopes ( $\epsilon_{x,z} = 1$ ) in the bowtie ring, from ray-tracing.

Ready for DA tracking. Ready for spin tracking too.

## 7 Conclusions

- Tools are there
- Defect studies can be pursued
- A lot is ready for s2e tracking
- It might be a good idea to have a kind of reference magnet design, 3D, including multipole defects and fringe fields.
- Planning to take a PhD student in the frame of EURONu program to work on IDS-NuFact topics

## 8 Bibliography

**Muon front end and acceleration : Franck Lemuët, PhD thesis, CEA & CERN, April 2007.**

**Triangle storage ring : F. Mot, G. Rees, Report CEA DAPNIA-06-04 / IN2P3 LPSC 06-38**

**Bow-tie storage ring : F. Mot, Note LPSC 06-127(NuFact)**