

# The Curse of Spin: Lurching from One Crisis to the Next

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Thus the path of spin is strewn with the wreckage of discarded theories. The positive aspect is that better (hopefully) theories arise from the debris.

## Contents

- 1) The Ancient World (brief)
- 2) The Renaissance (the European Muon Collaboration experiment)
- 3) The Present (new problems)

# THE ANCIENT WORLD

## An example: Electroweak Theory

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$$1 \text{ and } \frac{i}{2}[\gamma_\mu, \gamma_\nu]$$

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Role of spin in comparing rates for  $\pi \rightarrow e\bar{\nu}$  and  $\pi \rightarrow \mu\bar{\nu}$  was crucial. Measurement of the **Helicity** of the neutrino was also a vital experiment in confirming this.

fig

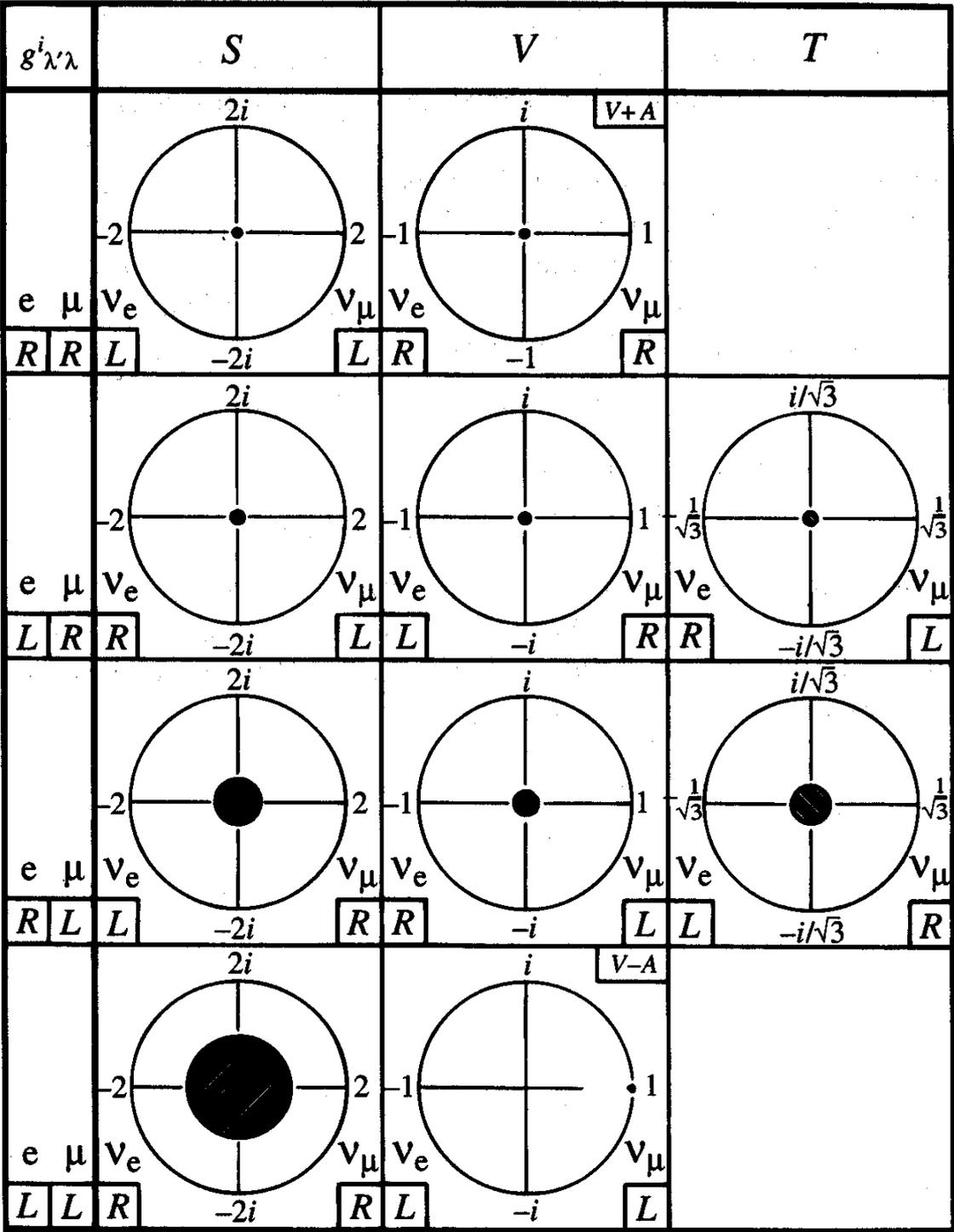
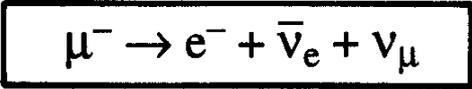


Fig. 1.8. 90% confidence level limits on the coupling constants  $g^{i\lambda\lambda}$  from the SIN experiments.

Without this unification of Weak and Electromagnetic interactions would have been impossible!

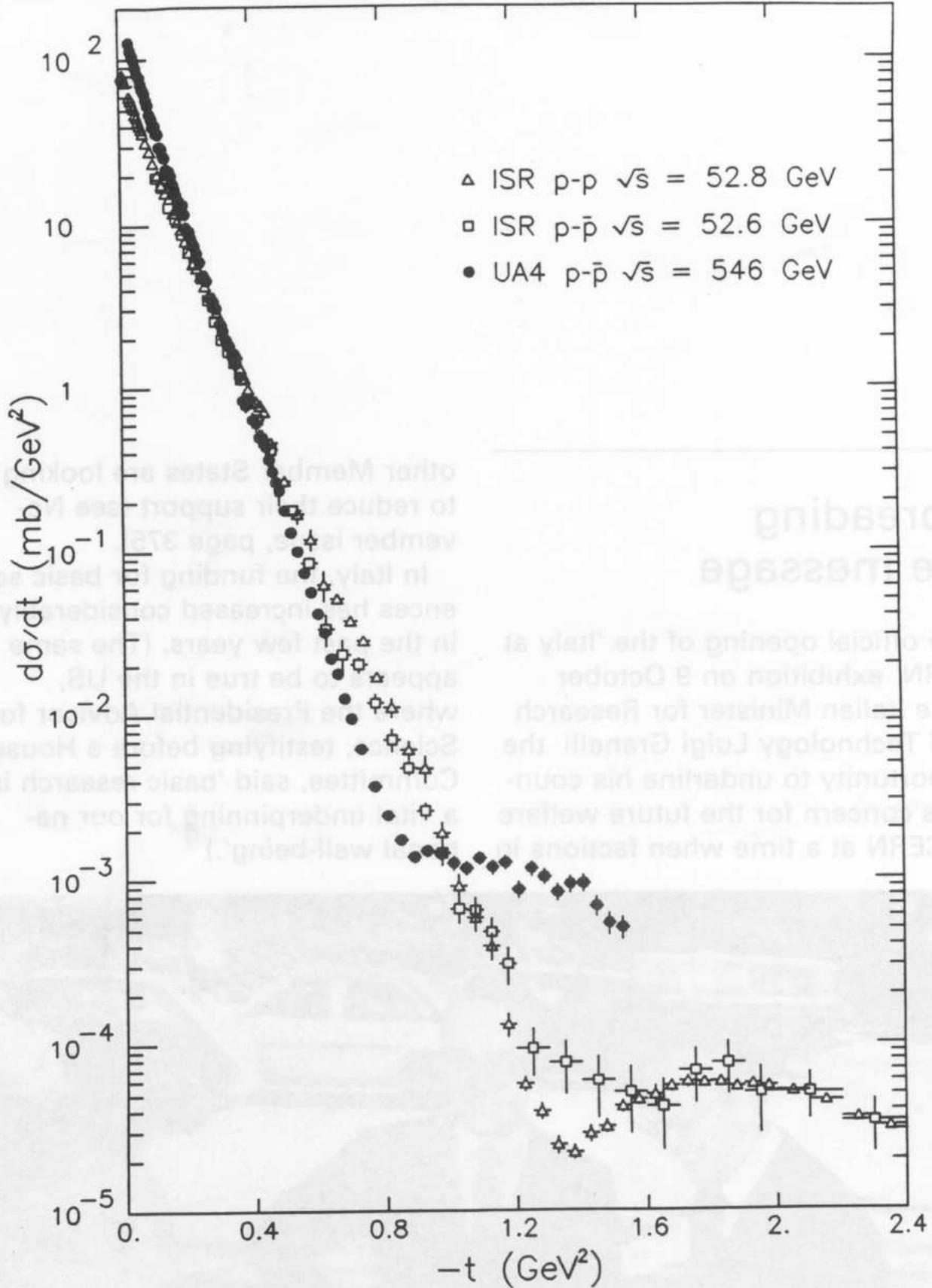
Another example: Regge Poles

Totally unexpected **SHRINKING** of diffraction peaks in  $\frac{d\sigma}{dt}$  for elastic cross-sections

$$A(p_1) + B(p_2) \rightarrow A(p_3) + B(p_4)$$

$$t = (p_1 - p_3)^2$$

fig



Beautiful explanation by Theory of Complex  
Angular Momentum: simplest version: Regge  
Poles—————**BUT**

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Total failure to predict **POLARIZATIONS**

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- 2) **Pedagogical-psychological:**

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Possibly two reasons:

1) **Practical:** Polarization measurements are very difficult. Sources, acceleration, depolarizing resonances etc etc

2) **Pedagogical-psychological:**

Spin had a difficult birth: fine structure of hydrogen (spin-orbit coupling); Stern-Gerlach experiment; “mysterious effects too complicated to explain in an undergraduate text” etc etc

slides

## 19.1 THE FINE STRUCTURE OF HYDROGEN

$$H_{\text{magn}} = \frac{1}{m^2 c^2} \frac{1}{r} \frac{dV}{dr} \mathbf{L} \cdot \mathbf{S} \quad (18.100)$$

When the actual calculation is made with the proper Lorentz transformations for the fields, it is found that owing to purely kinematic effects we must add a term to the energy, which has the same form as (18.100) but a different coefficient. Known as the *Thomas term*, this contribution to the Hamiltonian is

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Note that a direct calculation of the spin-orbit coupling, with the usual formulations of special relativity, gives a value *twice* as large as (13.22), and therefore a fine-structure splitting twice too large. This is why Pauli, at the end of 1925, did not believe in the idea of spin, and called it a “Irrleher” in a letter to Niels Bohr. However, in March 1926, L.H. Thomas remarked that the rest frame of the electron is not an inertial frame, and that a correct calculation introduces a factor of 1/2 in the formula (the Thomas precession<sup>2</sup>). This convinced Pauli of the validity of the spin-1/2 concept.

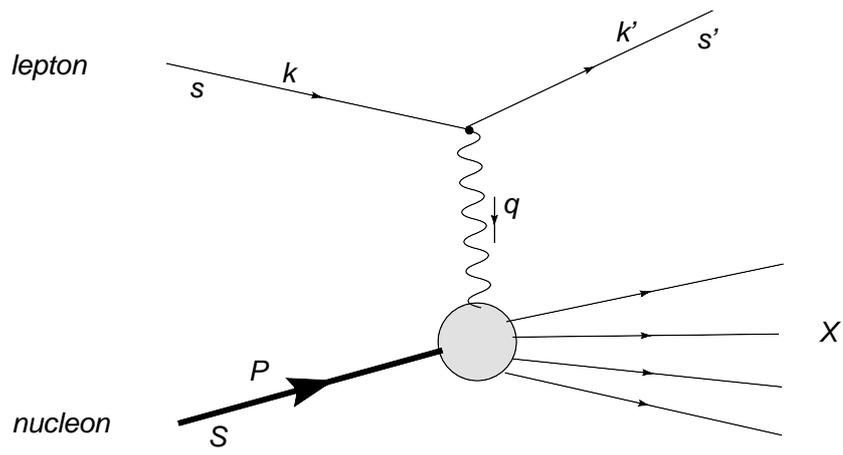


HERESY !

# THE RENAISSANCE

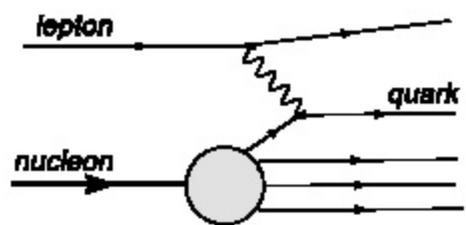
Deep Inelastic Scattering: a reminder

slide



Deep Inelastic Scattering in the parton model

fig



Deep Inelastic Scattering in the parton model

$$Q^2 \equiv -q^2 = -(k - k')^2 \quad \nu \equiv E_{Lab} - E'_{Lab}$$

$$x \equiv x_{Bjorken} = \frac{Q^2}{2M\nu}$$

The cross-sections are expressed in terms of two (unpolarized) STRUCTURE FUNCTIONS:  $F_{1,2}$

In simple Parton Model:  $F_{1,2}(x)$

Including some aspects of QCD:  $F_{1,2}(x, Q^2)$

Slow evolution in  $Q^2$

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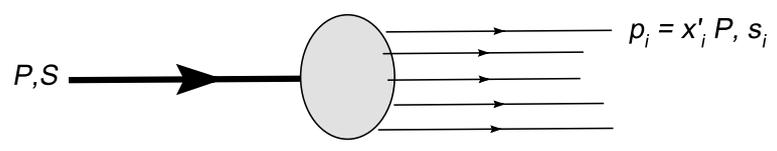
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Slow evolution in  $Q^2$

$$F_1(x, Q^2) = \frac{1}{2} \sum_{flav} e_j^2 [q_j(x, Q^2) + \bar{q}_j(x, Q^2)]$$

A key ingredient: the UNPOLARIZED parton number density  $q(x)$

fig



Quite analogously, POLARIZED cross-section expressed in terms of two spin-dependent STRUCTURE FUNCTIONS:  $g_{1,2}$

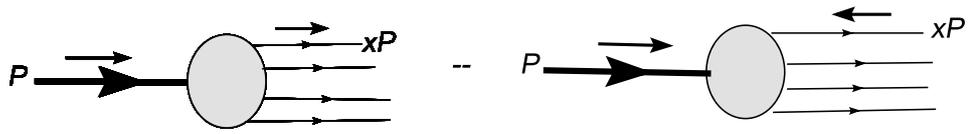
$$g_1(x, Q^2) = \frac{1}{2} \sum_{flav} e_j^2 [\Delta q_j(x, Q^2) + \Delta \bar{q}_j(x, Q^2)]$$

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The key ingredient here is the polarized quark density

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$$a_3 = \Delta u + \Delta \bar{u} - \Delta d - \Delta \bar{d}$$

$$= 1.267 \pm 0.0035$$

$$a_8 = \Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} - 2(\Delta s + \Delta \bar{s})$$

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Note that  $\Delta \Sigma = a_8 + 3(\Delta s + \Delta \bar{s})$

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But in naive parton model  $a_0 = \Delta\Sigma$

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Moreover, since

$$\Delta \Sigma = 2S_z^{quarks}$$

EMC seems to imply  $S_z^{quarks} = 0$

and there appears to be 'A crisis in the parton model: where, oh where, is the proton's spin?' [Anselmino and L, Z.Phys. **C41**,(1988) 239]

Resolution (??)of the crisis : The Anomalous  
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## Resolution (??)of the crisis : The Anomalous Gluon Contribution

The Operator Product Expansion has no gluon operator contributing to the first moment of  $g_1$ , but Feynman diagram approach yields result:

$$a_0 = \Delta\Sigma - \frac{3\alpha_s(Q^2)}{2\pi}\Delta G(Q^2) \quad (2)$$

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But even with present day estimates  $a_0 \approx 0.2$  this requires

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Is this acceptable? What do we know about  $\Delta G$ ?

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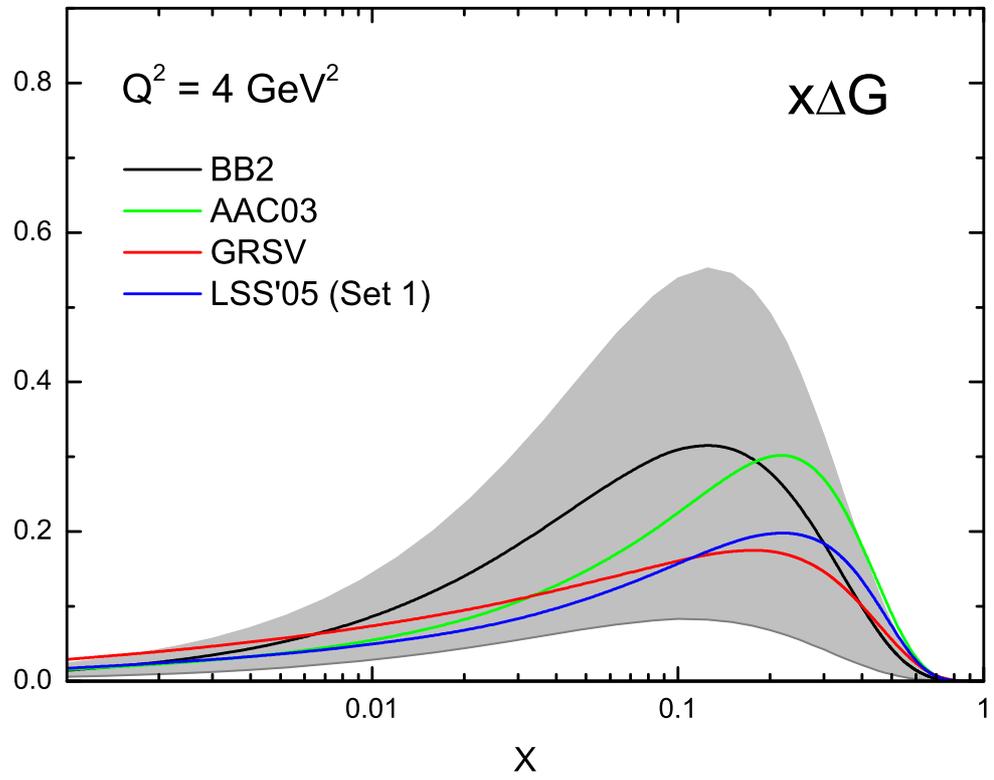
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fig world results on  $\Delta G(x)$



This is a test.

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(2)  $c\bar{c}$  production in DIS. Requires high energy lepton beam: COMPASS at CERN.

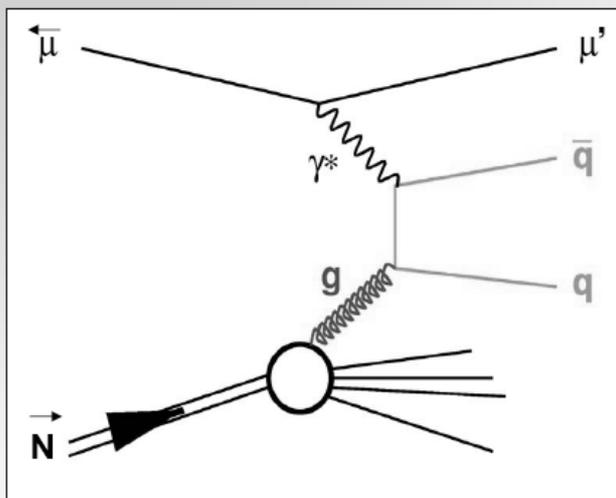
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Given that the nucleon has no **INTRINSIC** charm, the  $c\bar{c}$  are produced via 'gluon-photon fusion'.

fig

## Photon-Gluon fusion



$q = c$

“OPEN CHARM”

cross section difference  
in charmed meson production

→ *theory well understood*

→ *experiment challenging*

$q = u, d, s$

“HIGH  $p_T$  HADRON PAIRS”

cross section difference in 2+1  
jet production in COMPASS:

events with 2 hadrons with  
high  $p_T$

→ *experiment “easy”*

→ *theory more difficult*

Detecting BOTH charmed particles would be an absolutely clean signal for the mechanism!

But the intensity is too low—factor of 30 in rate lost in detecting second charmed meson—  
- so rely on single charm production. Also on back-to-back jets—much less clean.

Figure shows some of the COMPASS results

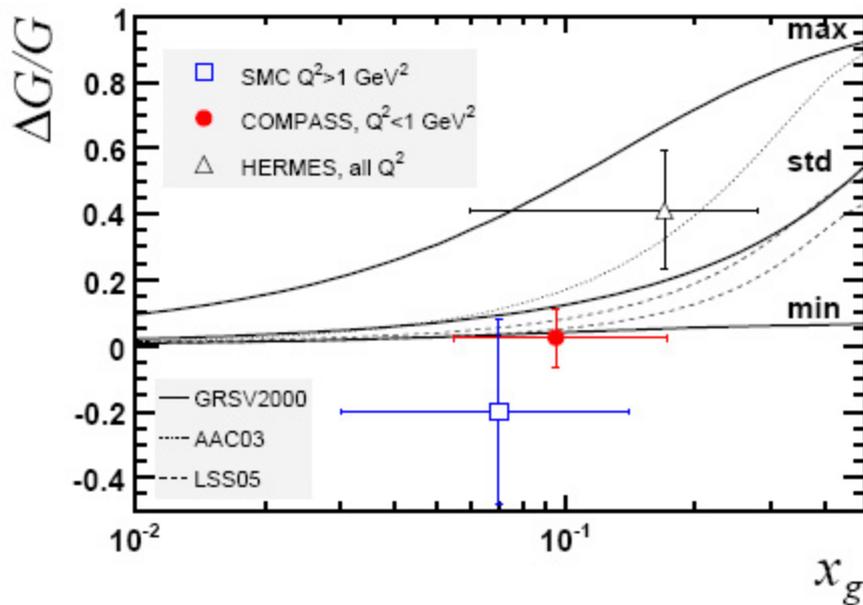


Figure 3: Comparison of the  $\Delta G/G$  measurements from COMPASS (present work), SMC [14], and HERMES [23]. The horizontal bar on each point represents the range in  $x_g$ . The curves show various parametrizations from NLO fits in the  $\overline{\text{MS}}$  scheme at  $\mu^2 = 3 \text{ (GeV/c)}^2$ : GRSV2000 [20] (3 curves, please see text for details), AAC03 [24], and LSS05 sets 1 and 2 [25].

Suggests very small  $\Delta G$  compatible with result quoted above

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(3)  $A_{LL}$  with polarized protons: uniquely at RHIC.

Several reactions:

$\vec{p} + \vec{p} \longrightarrow \pi^0 + X$  (needs **Fragmentation Functions**)

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Dominant partonic reactions:

$\vec{g} + \vec{g} \longrightarrow g + g$  : dominates at smaller  $p_T^2$

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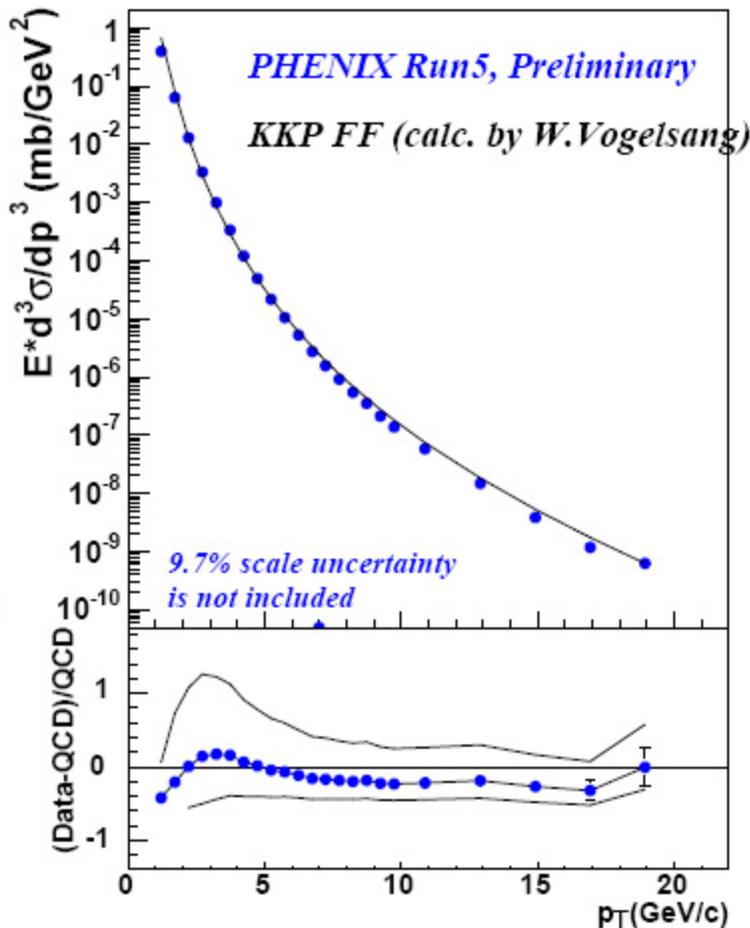
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Nice test: PQCD describes cross-sections quite well. **Fig**

# $\pi^0$ Cross Section

- > Data points extend from 1 to 20 GeV/c in  $p_T$ .
- > pQCD calculation with KKP FF describes the data well over all measured  $p_T$  region. (range of  $10^9$ )
- > The cross section of other channel, for example charged pion, is also useful to test pQCD.



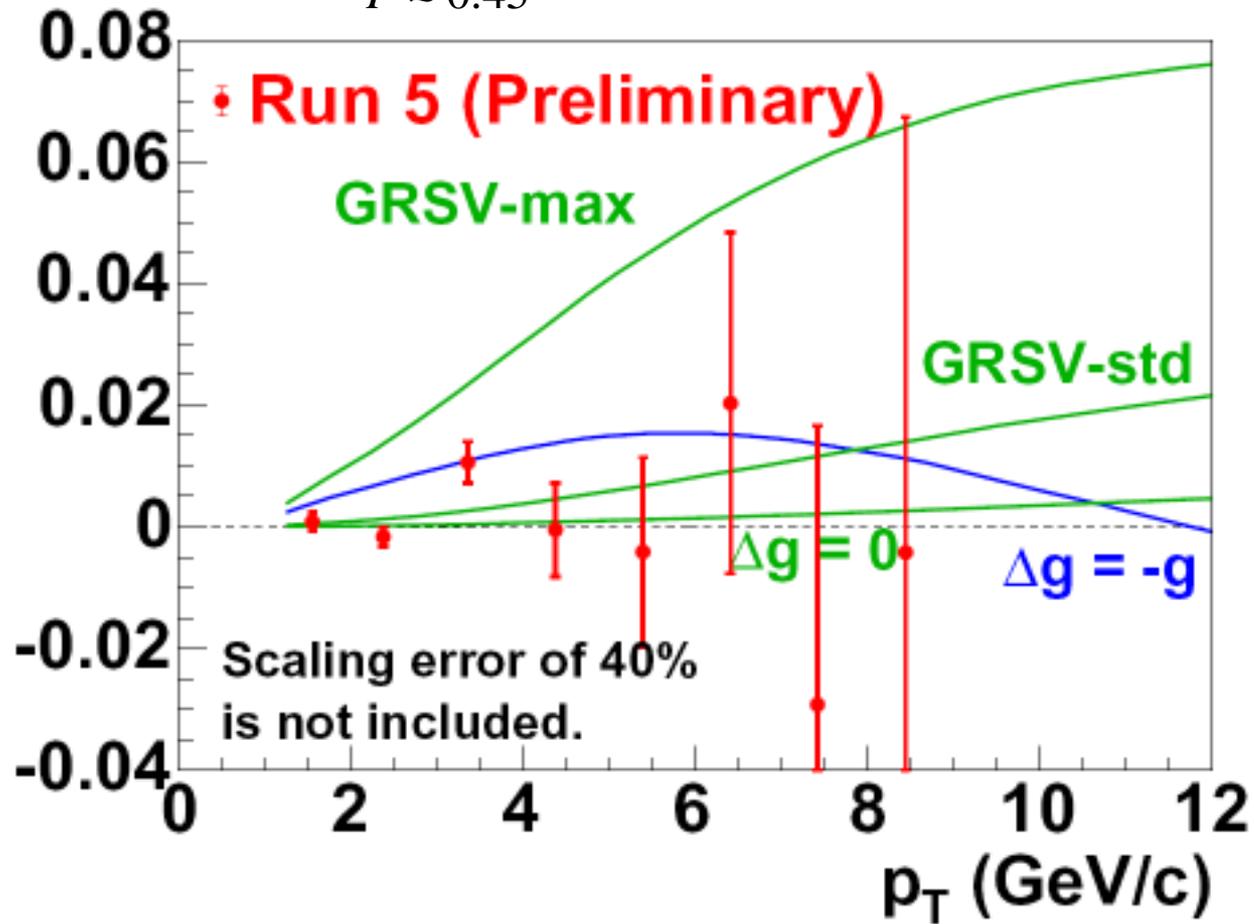
Results:  $A_{LL}$  is SMALL!

Fig

$A_{LL}(\pi^0)$

$$\int Ldt = 2.7 pb^{-1}$$

$$P \approx 0.45$$



Consistent with ZERO gluon polarization

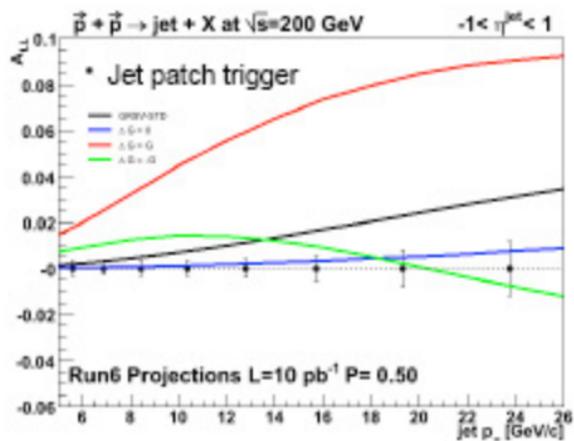
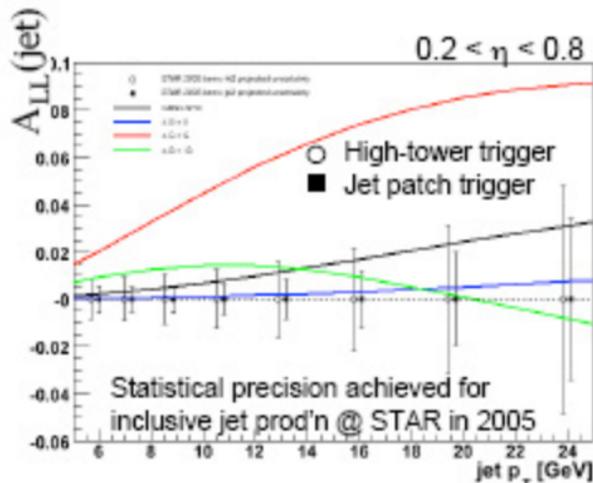
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**THE SPIN CRISIS  
IS STILL WITH US !**

Expect more definite statement on  $A_{LL}$  very soon: much improved accuracy

fig

# Prospects for Run5 (first long pp run) and Run6(ongoing)



Run5 improvements:

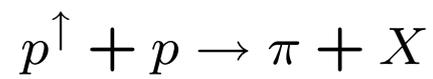
- $P_b \sim 45\%$  ( $\sim 40\%$  in Run4)  $L = 3/\text{pb}$  ( $0.3/\text{pb}$  in Run4)
- $\text{FoM}(\text{Run5})/\text{FoM}(\text{Run4}) = 16$

- Acceptance: 3/4 BEMC complete (1/2 in Run4)
- Two complementary jet triggers permit assessment of trigger bias due to q vs. g jet differences in shape, multiplicity, hardness in z.

*Potential to discriminate between several  $A_{LL}$  predictions based on DIS parametrizations*

# TRANSVERSE SINGLE-SPIN ASYMMETRIES

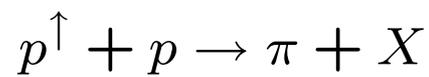
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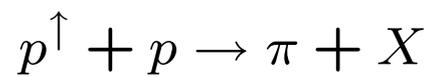
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Asymmetry under reversal of direction of polarisation

$$A_N \equiv \frac{d\sigma^\uparrow - d\sigma^\downarrow}{d\sigma^\uparrow + d\sigma^\downarrow}$$

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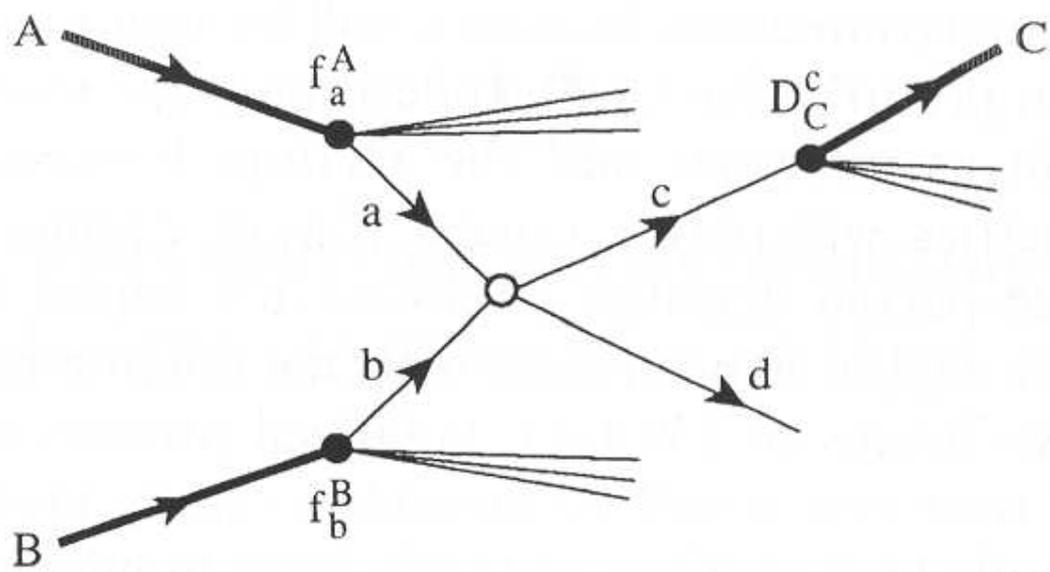
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Partonic mechanism:

fig



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$$\hat{a}_N = \alpha_s \frac{m_q}{\sqrt{s}} f(\theta^*)$$

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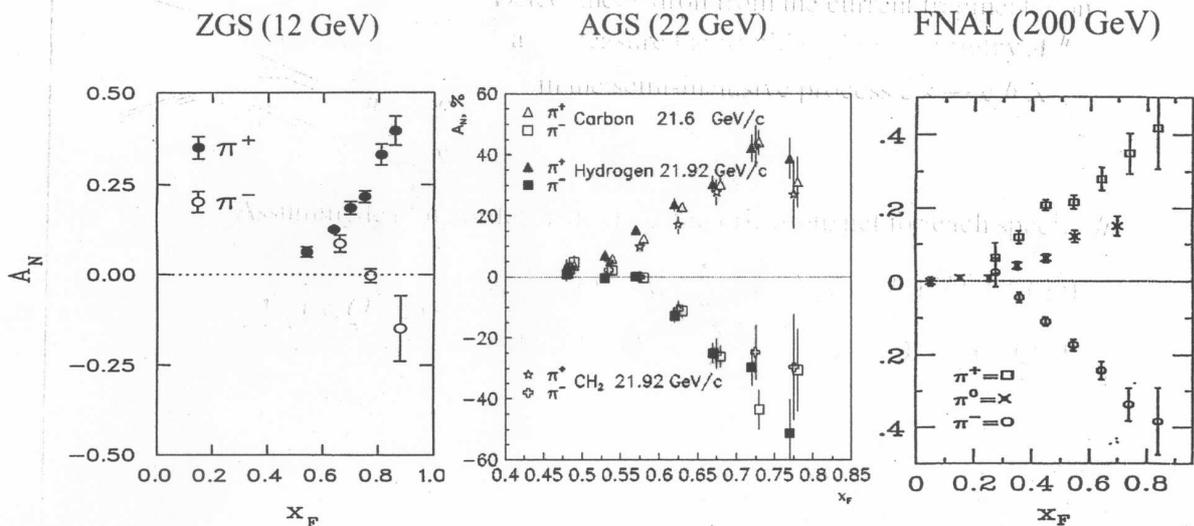
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**THE DATA STRONGLY CONTRADICT THIS!**

fig

# Asymmetry in pion production at large $X_F$



Phys.Rev.D65:092008,2002

Phys. Lett. B261(1991)201  
Phys. Lett. B264(1991)462



Large asymmetry in pion production  
Asymmetry persists to high energy  
No asymmetry in proton production at the AGS (not shown)

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a) SIVERS: Number density of quarks with momentum  $x\mathbf{P} + \mathbf{k}_T$  depends on polarization  $\mathcal{P}$  of parent hadron:

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Conceptually no problem; but makes serious calculations horrendous.

2) Invent new SOFT mechanisms—beyond the parton model

a) **SIVERS**: Number density of quarks with momentum  $x\mathbf{P} + \mathbf{k}_T$  depends on polarization  $\mathcal{P}$  of parent hadron:

$$q(x, \mathbf{k}_T) = A + B_S \mathcal{P} \cdot (x\mathbf{P} \times \mathbf{k}_T)$$

**BUT** can show this violates Parity and Time Reversal invariance **IF**

$$\textit{hadron} \rightarrow \textit{quark} + X$$

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Number density of hadrons with momentum  $\mathbf{P}_h = \frac{1}{z}\mathbf{p} + \mathbf{k}_T$  depends on polarization  $\mathcal{P}$  of fragmenting quark.

$$D(z, \mathbf{P}_h) = A + B_C \mathcal{P} \cdot (\mathbf{p} \times \mathbf{P}_h)$$

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So again lose universality.

Moreover, can't calculate  $B_S$  or  $B_C$  so need to introduce new functions phenomenologically, for each flavour of quark and antiquark. Ugly!

# THE LATEST PROBLEM

One of the oldest and supposedly best understood reactions:



Measurement of the ELECTROMAGNETIC FORM FACTORS OF THE PROTON

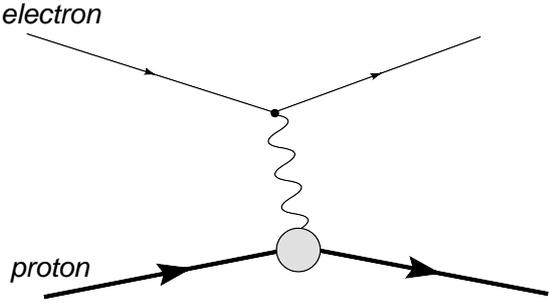
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As always, assume ONE PHOTON Exchange

fig



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$$\bar{u}(p') [\gamma_\mu F_1^{em}(Q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2M} \kappa F_2^{em}(Q^2)] u(p)$$

$$q = p' - p \quad \kappa = \text{anomalous magnetic moment}$$
$$Q^2 = -q^2$$

$F_{1,2}$  Dirac em form factors. Sachs more convenient:  $G_E = F_1 - \kappa\tau F_2$        $G_M = F_1 + \kappa F_2$

$$\tau = \frac{Q^2}{4M^2}$$

$$G_E(0) = 1$$

$$G_M(0) = \text{total magnetic moment}(\mu) = 2.79$$

Diff. cross-section in the LAB: ROSENBLUTH

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)'_{Mott} \left[ \frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2(\theta/2) \right]$$

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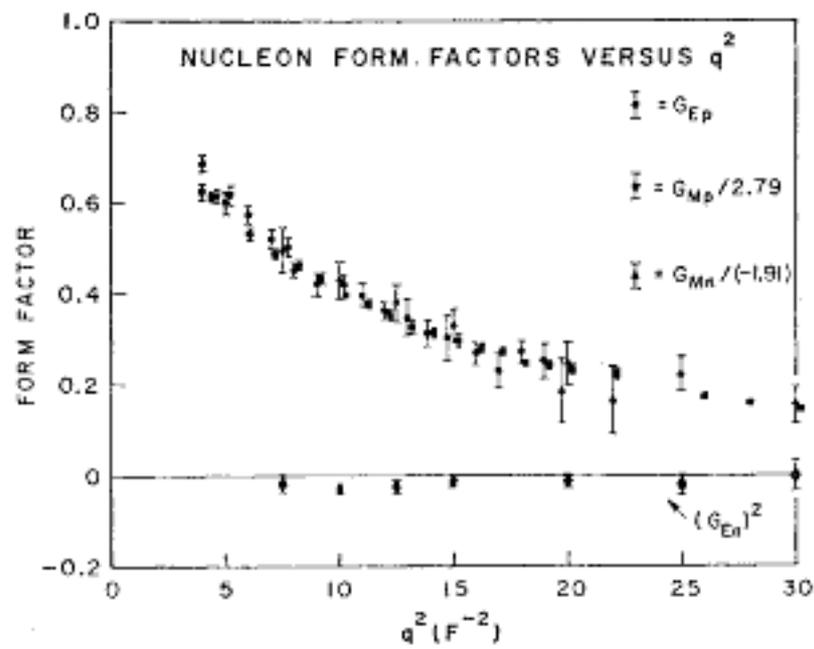
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Both  $G_E$  and  $G_M$  drop with increasing  $Q^2$

Long standing experimental assertion that

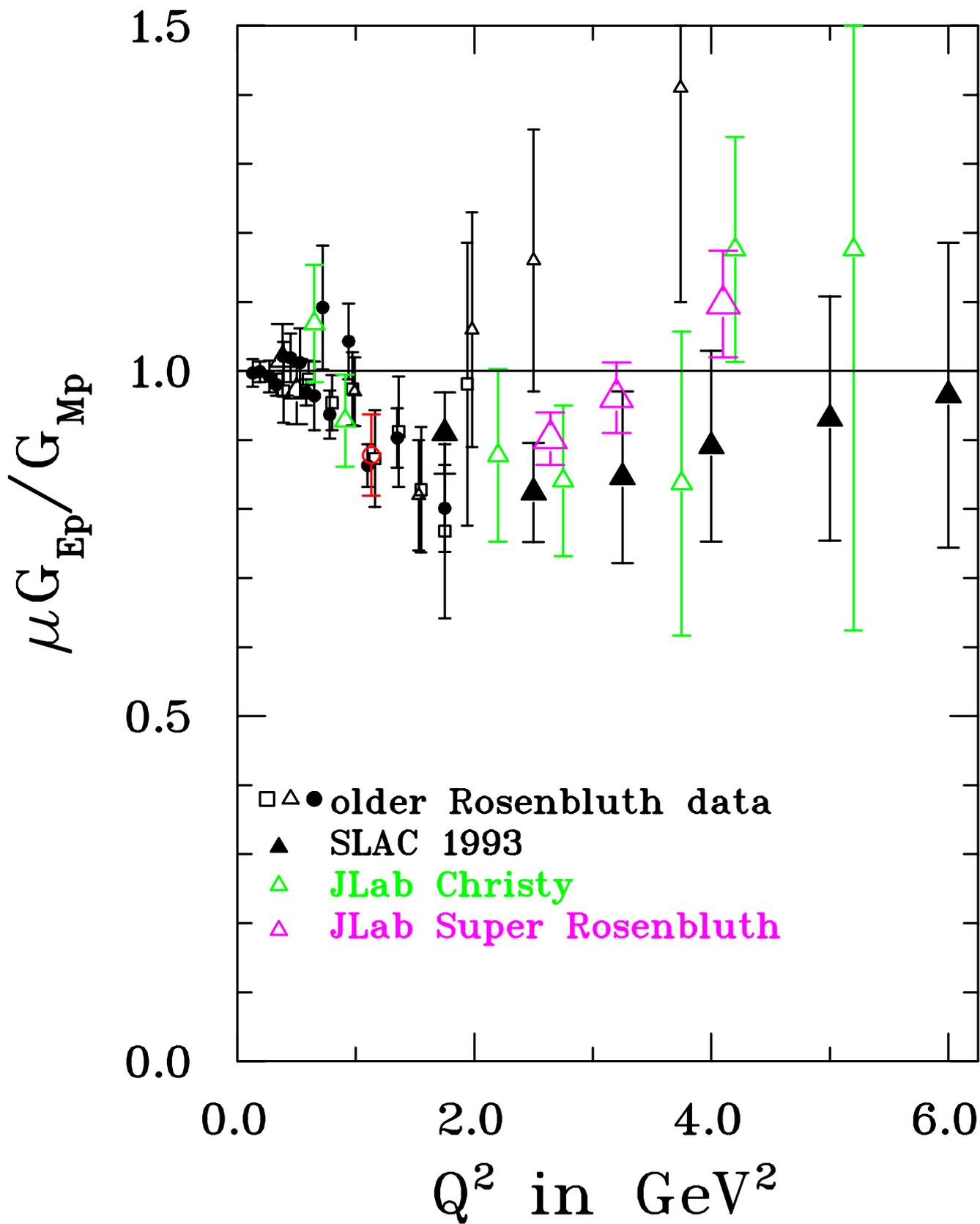
$$G_M(Q^2) \approx \mu G_E(Q^2)$$

fig



New cross-section measurements are consistent with this:

fig



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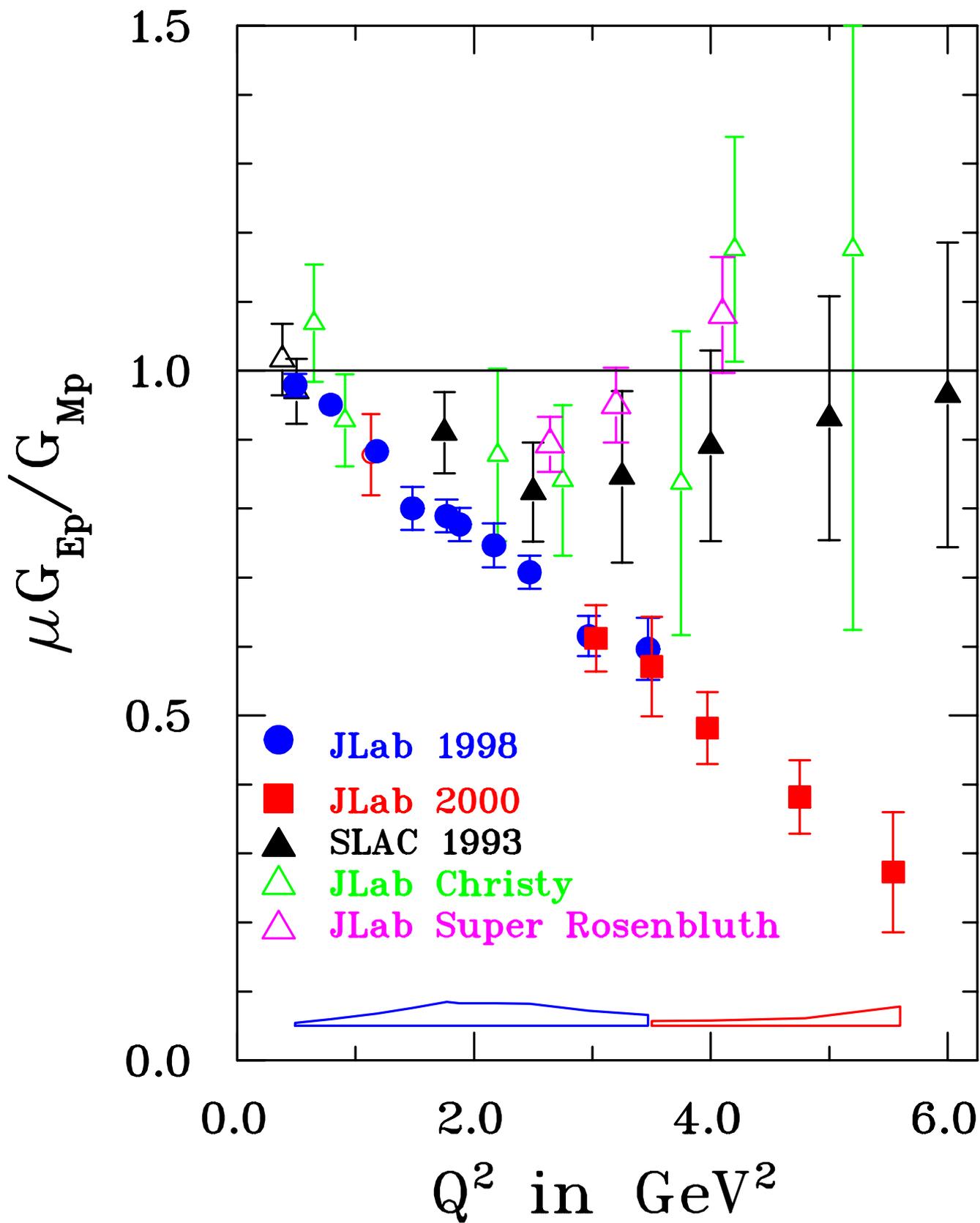
LONGITUDINAL polarization of the recoil proton:

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TRANSVERSE (in scattering plane) polarization of the recoil proton:

$$\mathcal{P}_T \propto -2\sqrt{\tau(1 + \tau)} G_E G_M \tan(\theta/2)$$

fig



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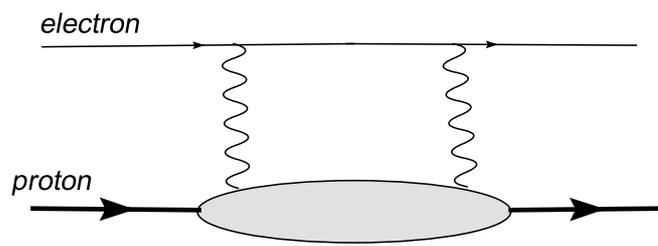
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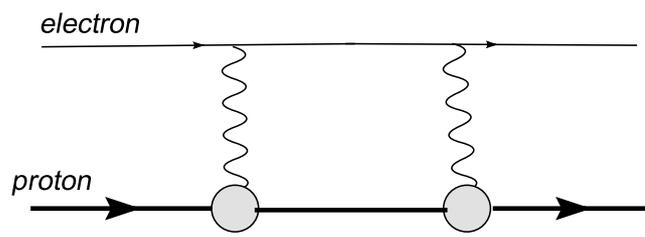
Exact calculation would require evaluation of Feynman graph:

fig



Not possible. Can do approximate calculation of simplest two photon graph:

fig



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What about famous prediction of perturbative QCD:

$$G_E/G_M \rightarrow \text{constant as } Q^2 \rightarrow \infty \quad ??????$$

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(c) We are facing the realization that what is arguably the best-understood of all reactions i.e. electron-proton elastic scattering, has, in fact, been significantly misunderstood