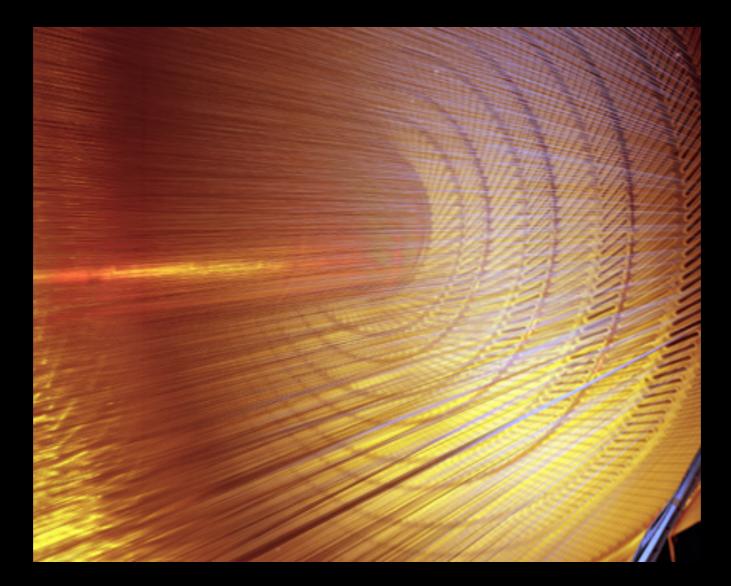
High-precision measurement of the W boson mass with the CDF II detector



Chris Hays, Oxford University

Imperial College seminar 31 May, 2023

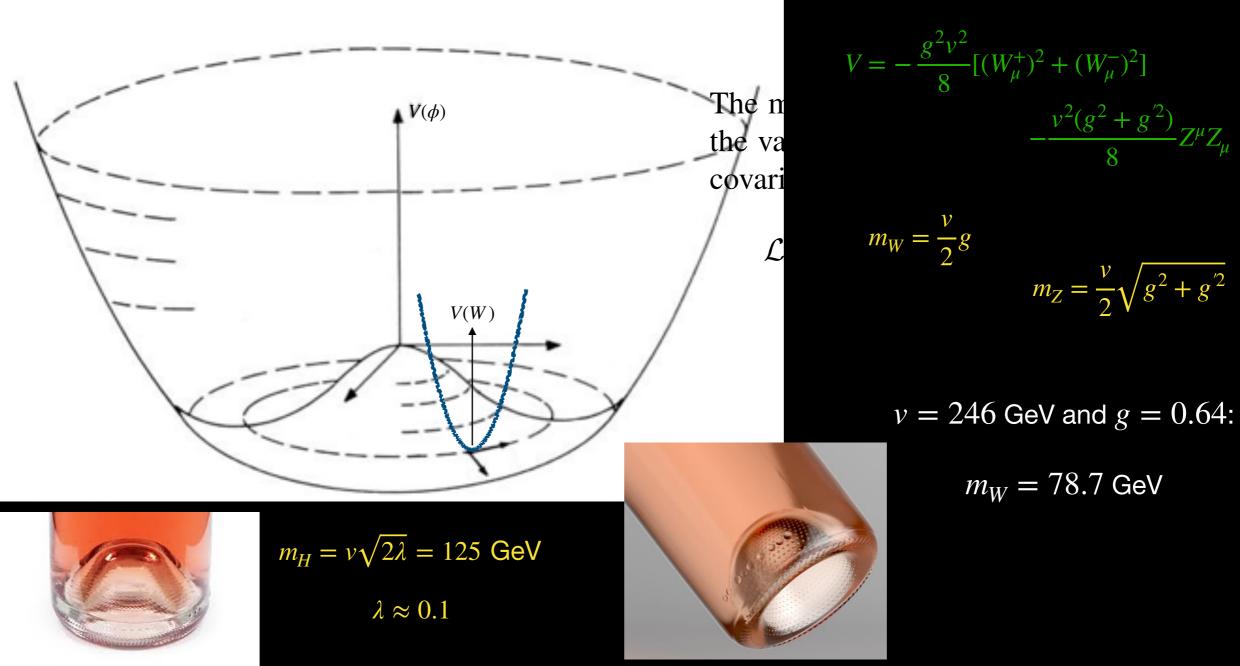




Boson masses

Higgs field potential

Gauge field potential



Quantum corrections

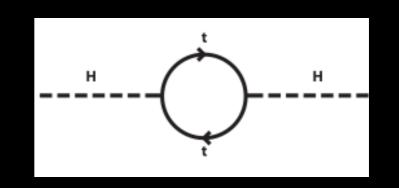
$m_W^2 = \frac{\hbar^3}{c} \frac{\pi \alpha_{EM}}{\sqrt{2}G_F (1 - m_W^2/m_Z^2)(1 - \Delta r)}$

Gauge quantum corrections

$$\Delta r_{tb} = \frac{c}{\hbar^3} \frac{-3G_F m_W^2}{8\sqrt{2}\pi^2 (m_Z^2 - m_W^2)} \times \left[m_t^2 + m_b^2 - \frac{2m_t^2 m_b^2}{m_t^2 - m_b^2} \ln(m_t^2/m_b^2) \right]$$

SM calculation of W boson mass yields $80358\pm4~\text{MeV}$

Higgs quantum corrections



Naively integrating to a cutoff scale Λ :

$$\Delta m_H^2 = \frac{3g^2 m_t^2}{16\pi^2 m_W^2} \Lambda^2$$

If there is no new physics up to scale Λ then we need 'fine-tuning' to cancel the quantum corrections

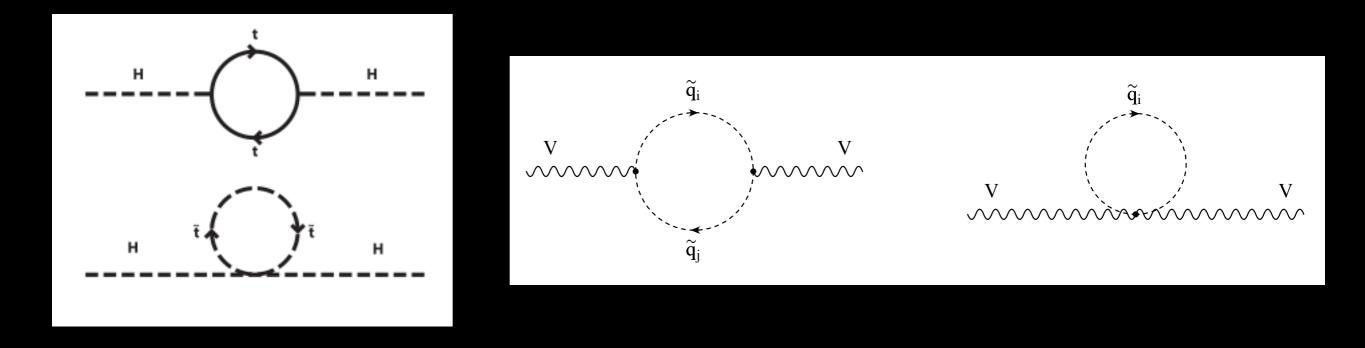
1% fine tuning: $\Lambda = 6.6$ TeV

Motivates TeV-scale new physics

W boson mass

The W boson mass is the most sensitive observable to sources of 'naturalness'

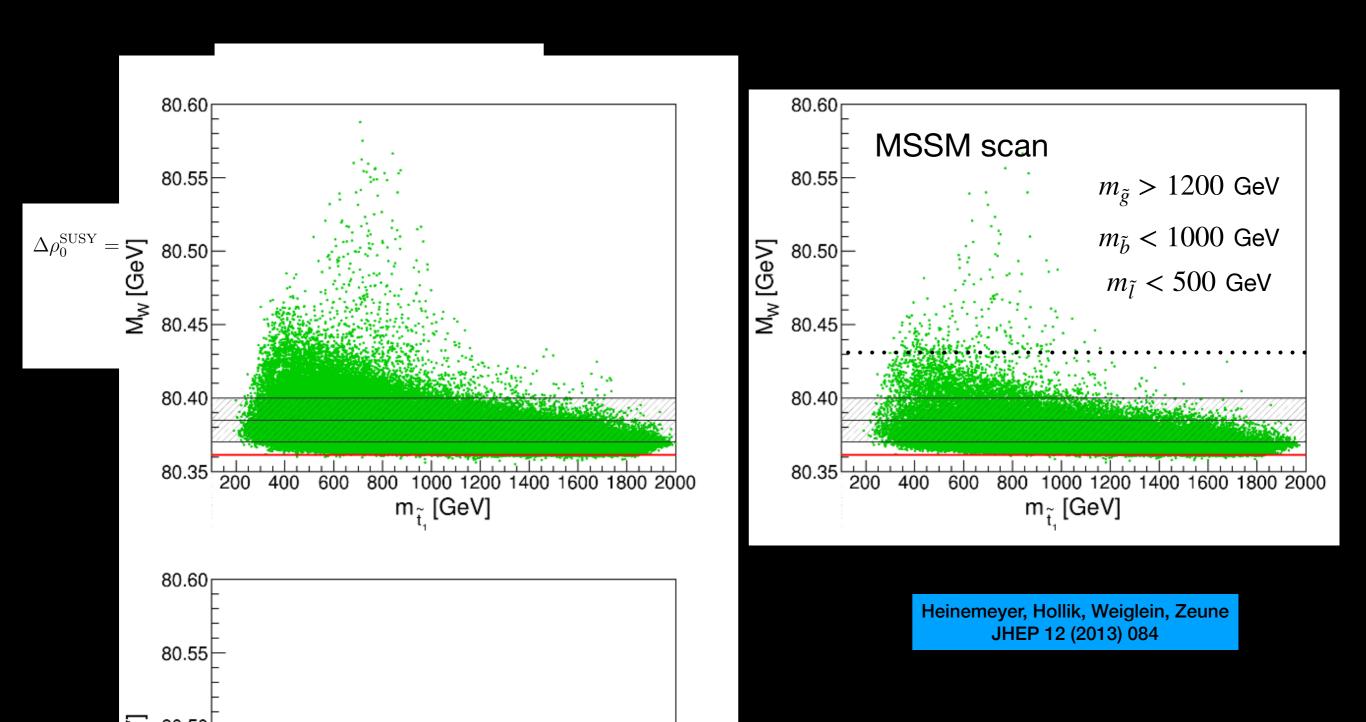
Classic example: Supersymmetry



Mass splittings in supersymmetric isospin doublets: different mass shifts for W & Z bosons

W boson mass

Difference in corrections to W and Z propagators encapsulated by ρ parameter



W boson mass

More generally the SM effective field theory parameterizes high-scale effects

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}^{(5)} + \mathcal{L}^{(6)} + \mathcal{L}^{(7)} + \cdots, \qquad \mathcal{L}^{(d)} = \sum_{i=1}^{n_d} \frac{C_i^{(d)}}{\Lambda^{d-4}} Q_i^{(d)} \quad \text{for } d > 4.$$

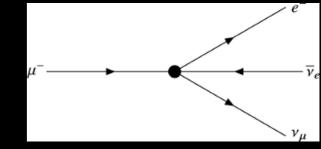
$$I. \text{ Brivio and M. Trott, Phys. Rep. 793 (2019) 1}$$

$$\mu \underbrace{\frac{p}{V_i}}_{V_i} \underbrace{V_j}_{V_j} \nu \qquad \frac{\delta m_W}{m_W} = \left(0.34c_{HD} + 0.72c_{HWB} + 0.37c_{Hl3} - 0.19c_{ll1}\right) \frac{v^2}{\Lambda^2}$$

For $\delta m_W/m_W = 0.1$ % and c_{HD}=1, $\Lambda = 4.5$ TeV e.g. Z' boson

For $\delta m_W/m_W = 0.1$ % and c_{HWB}=1, $\Lambda = 6.6$ TeV e.g. compositeness

Smaller $c_i \rightarrow \text{smaller } \Lambda$



Hadron-collider W boson mass measurements

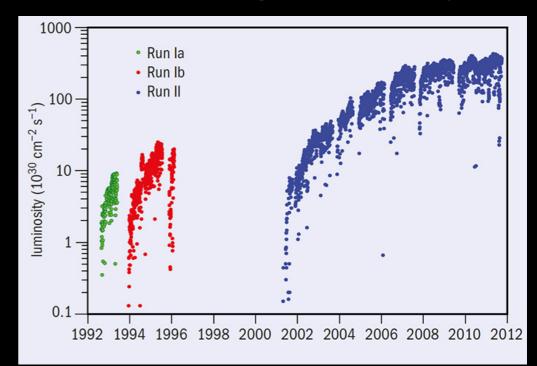
 $\sqrt{s}=1.96~{\rm TeV}$ proton-antiproton collisions from the Fermilab Tevatron



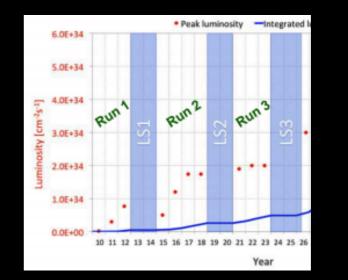
 $\sqrt{s} = 7$, 13 TeV proton-proton collisions from the Large Hadron Collider

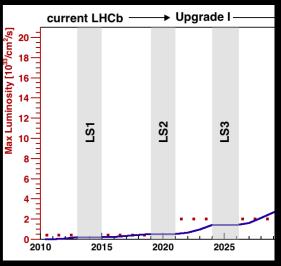


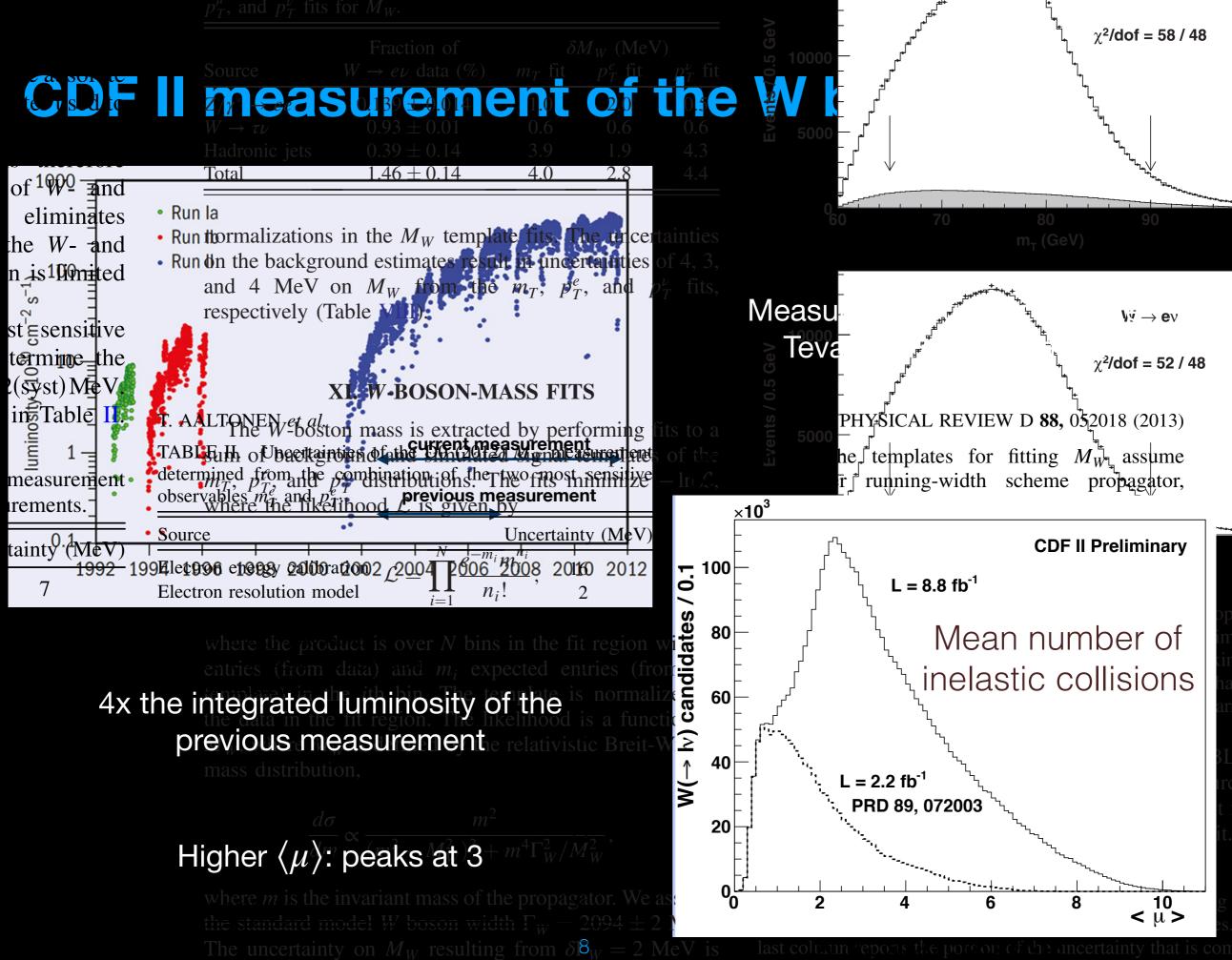
CDF: 8.8 fb⁻¹ of integrated luminosity D0: 5.3 fb⁻¹ of integrated luminosity



ATLAS: 4.1 fb⁻¹ of integrated luminosity (7 TeV) LHCb: 1.7 fb⁻¹ of integrated luminosity (13 TeV)



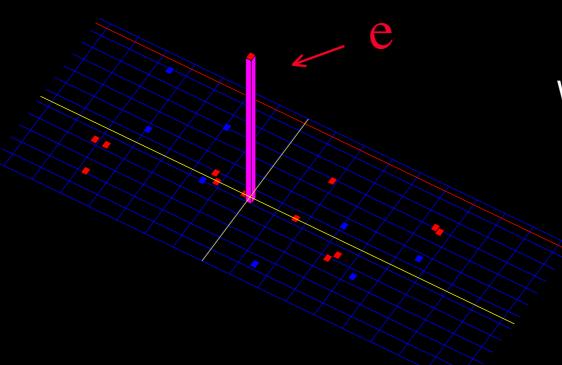




naglivible

in the $\mu\nu$ and $e\nu$ results.

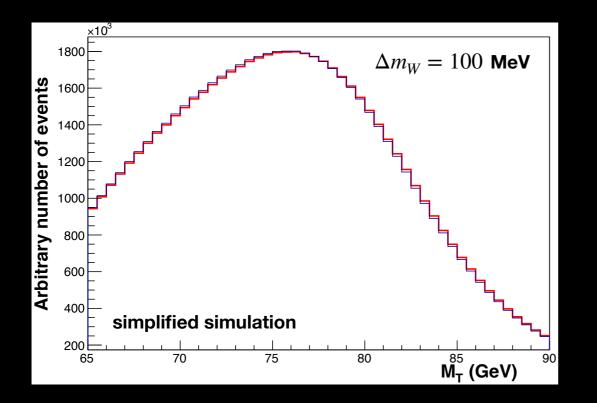
CDF II measurement of the W boson mass

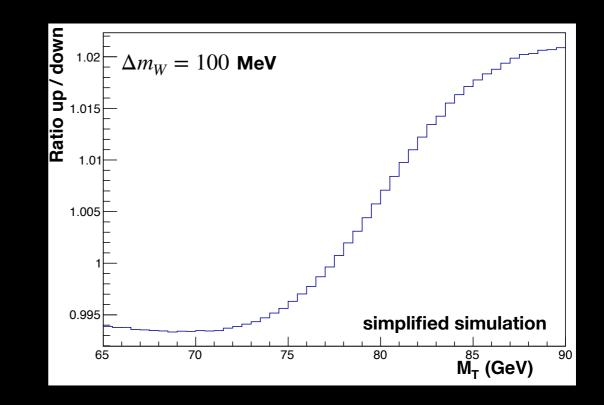


W bosons identified from their decays to $e\nu$ and $\mu\nu$

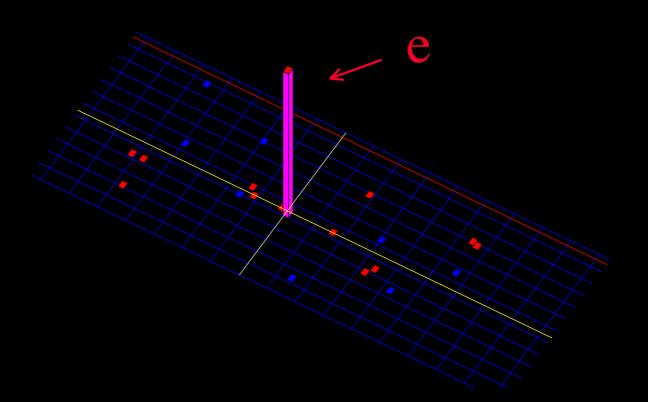
Mass measured by fitting template distributions of transverse momentum and mass

$$m_T = \sqrt{2p_T^{\ l} \not\!\!p_T \left(1 - \cos \Delta \phi\right)}$$



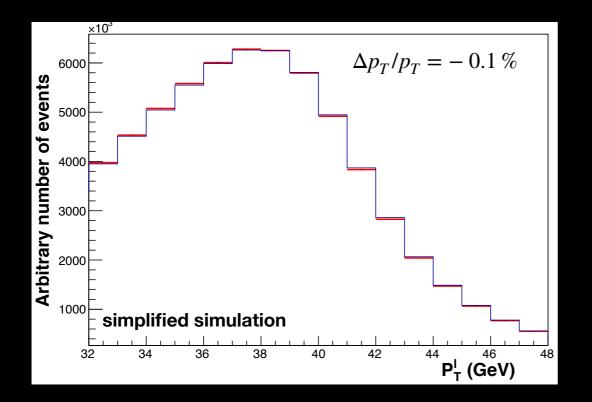


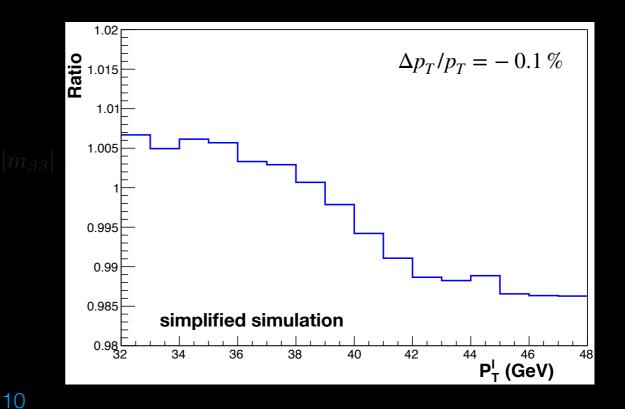
Calibrations



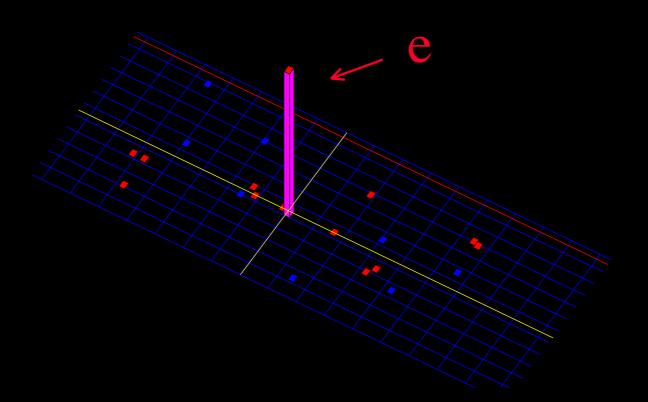
Measurement requires precise calibrations of momentum scale and resoution

Charged lepton scale





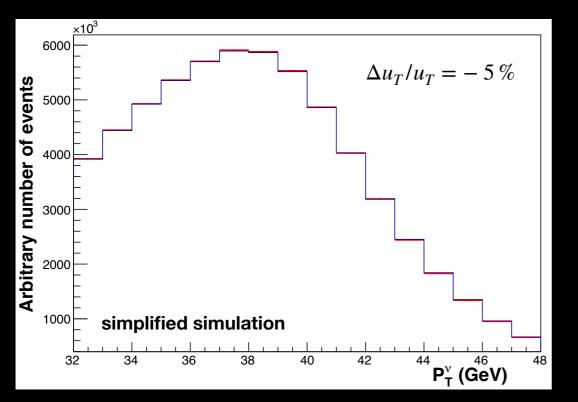
Calibrations

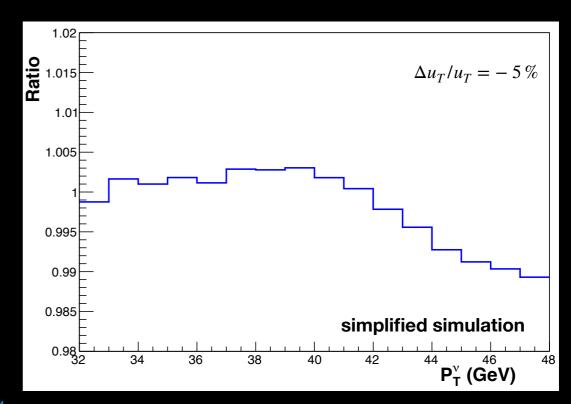


Measurement requires precise calibrations and momentum scale and resolution

$$\vec{p}_T = -(\vec{p}_T^{\ l} + \vec{u}_T) \qquad p_T^{\ell} \qquad u_T$$
Recoil scale
$$p_T^W \qquad p_T^W \qquad p_T$$

 p_T^{ν}





Detector simulation

Developed custom simulation for analysis

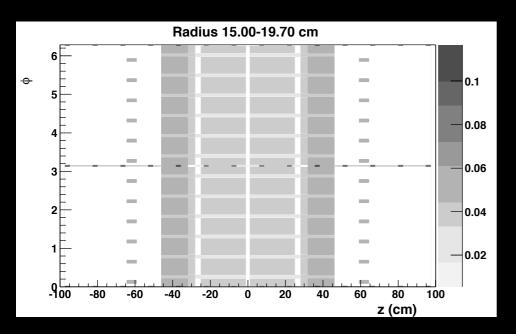
Models ionization energy loss, multiple scattering, bremsstrahlung, photon conversion, Compton scattering

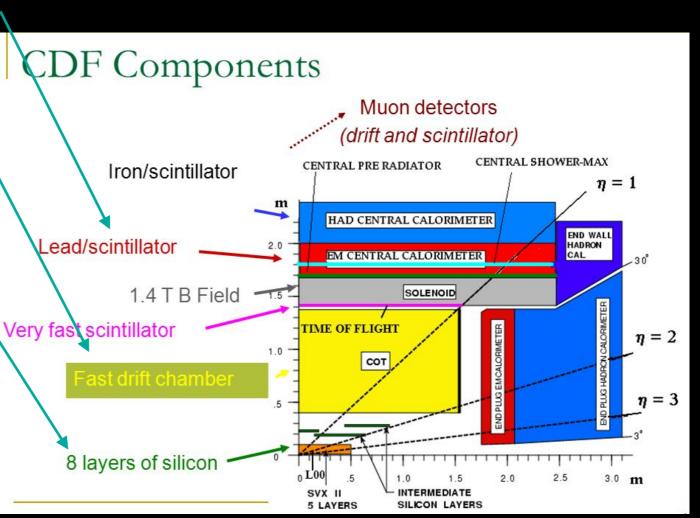
Acceptance map for muon detectors

Parameterized GEANT4 model of electromagnetic calorimeter showers Includes shower losses due to finite calorimeter thickness

Hit-level model of central outer tracker Layer-by-layer resolution functions and efficiencies

Material map of inner silicon detector Includes radiation lengths and Bethe-Bloch terms

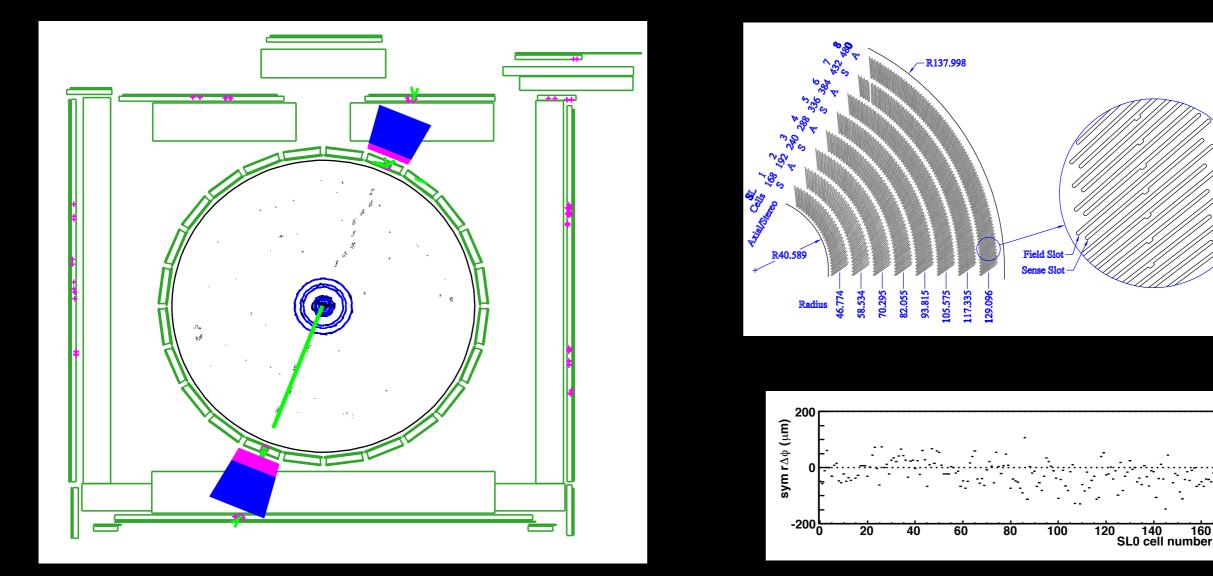




Kotwal & CH, NIMA 729, 25 (2013)

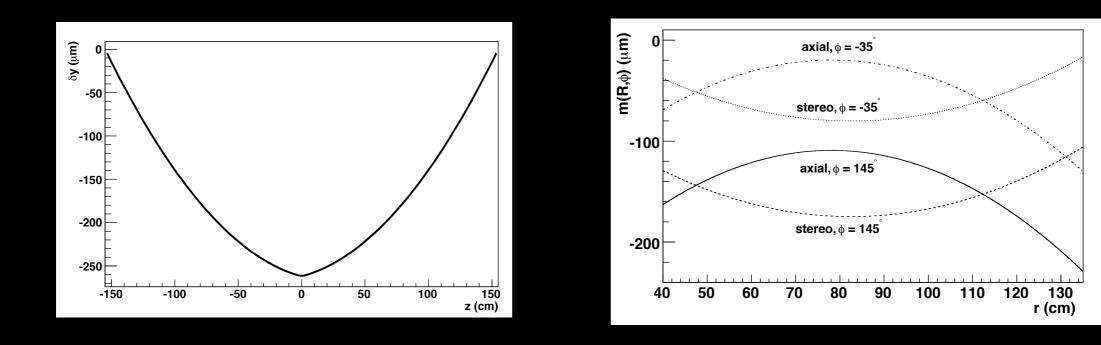
First step is to align the drift chamber (the "central outer tracker" or COT)

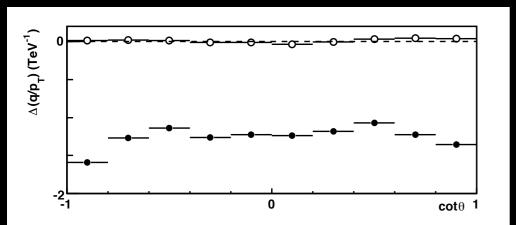
Two degrees of freedom (shift & rotation) for each of 2520 cells made up of twelve sense wires constrained using hit residuals from cosmic-ray tracks

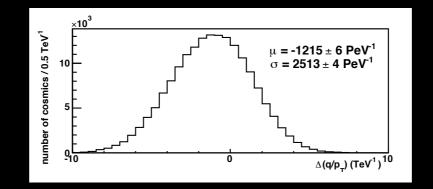


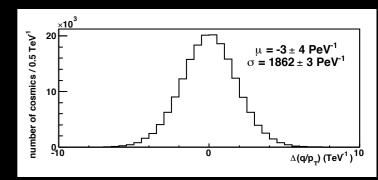
First step is to align the drift chamber (the "central outer tracker" or COT)

Two parameters for the electrostatic deflection of the wire within the chamber constrained using difference between fit parameters of incoming and outgoing cosmic-ray tracks





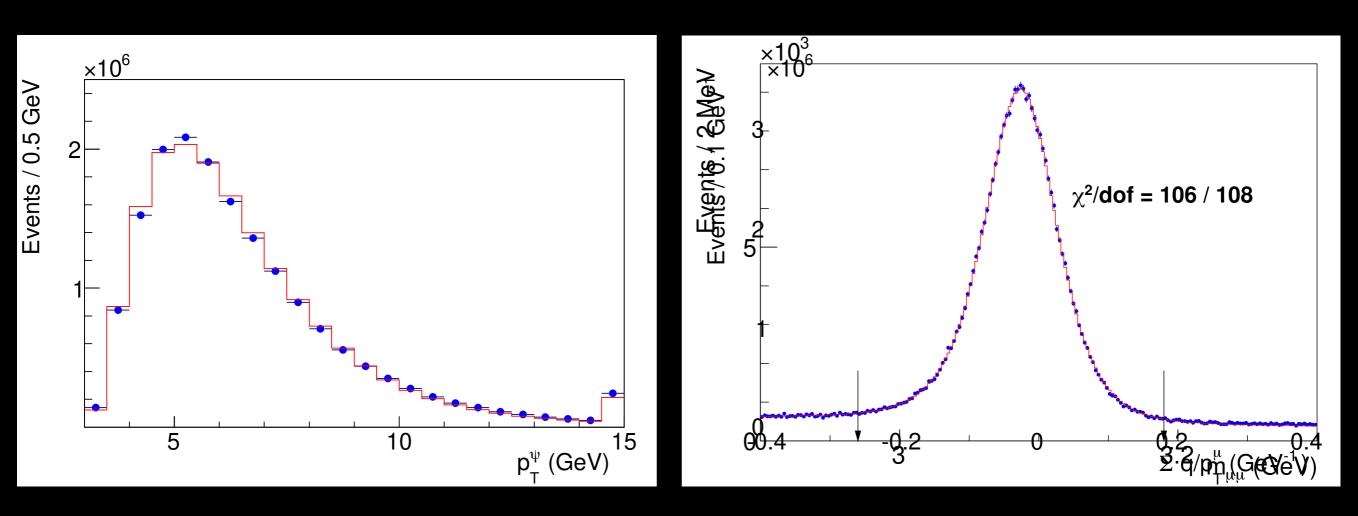




Second step is to calibrate the momentum scale using J/ψ decays to muons

Simulation:

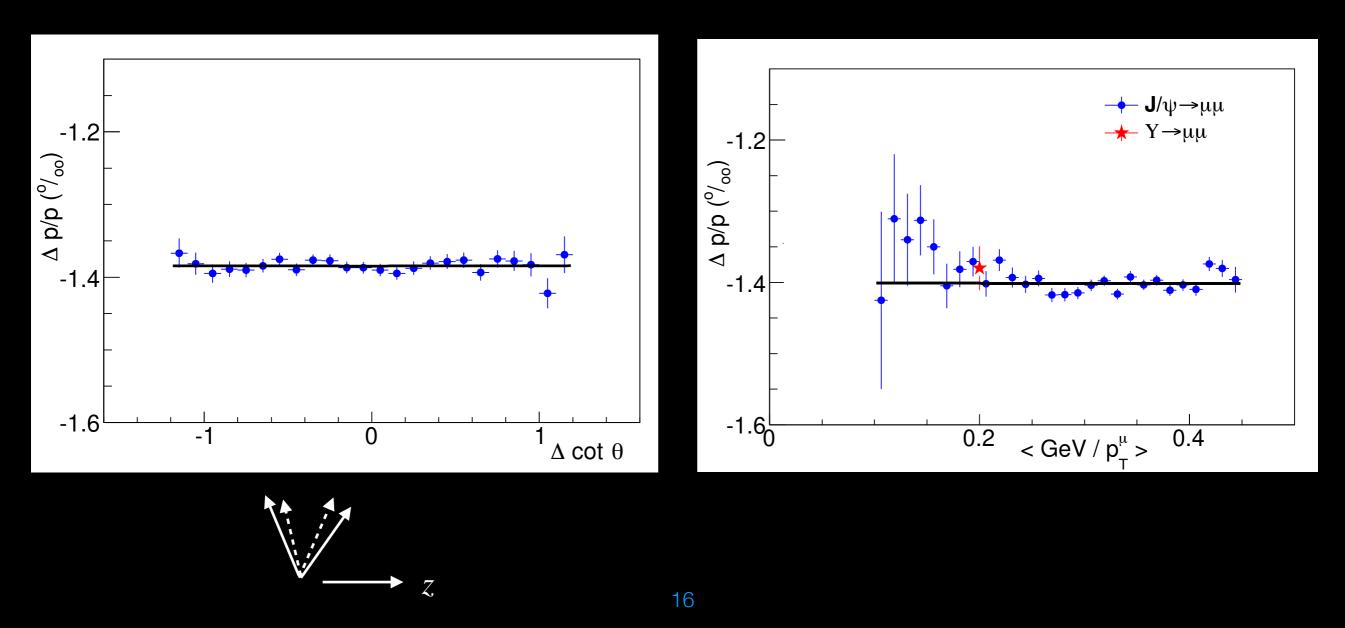
Adjust kinematics to match the data Model resonance shape using hit-level simulation and NLO form factor for QED radiation



Second step is to calibrate the momentum scale using J/ψ decays to muons

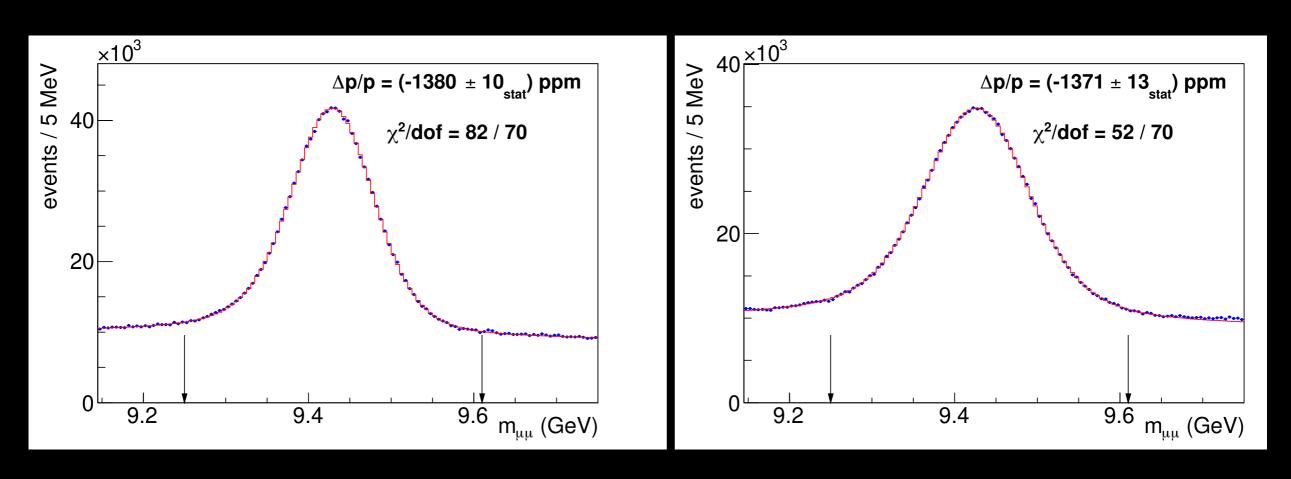
Simulation corrections:

Correct the length scale of the tracker with mass measurement as a function of $\Delta \cot \theta$ Correct the amount of upstream material with mass measurement as a function of p_T^{-1}



Third step is to calibrate the scale using Υ decays to muons

Compare fit results with and without constraining the track to the collision point



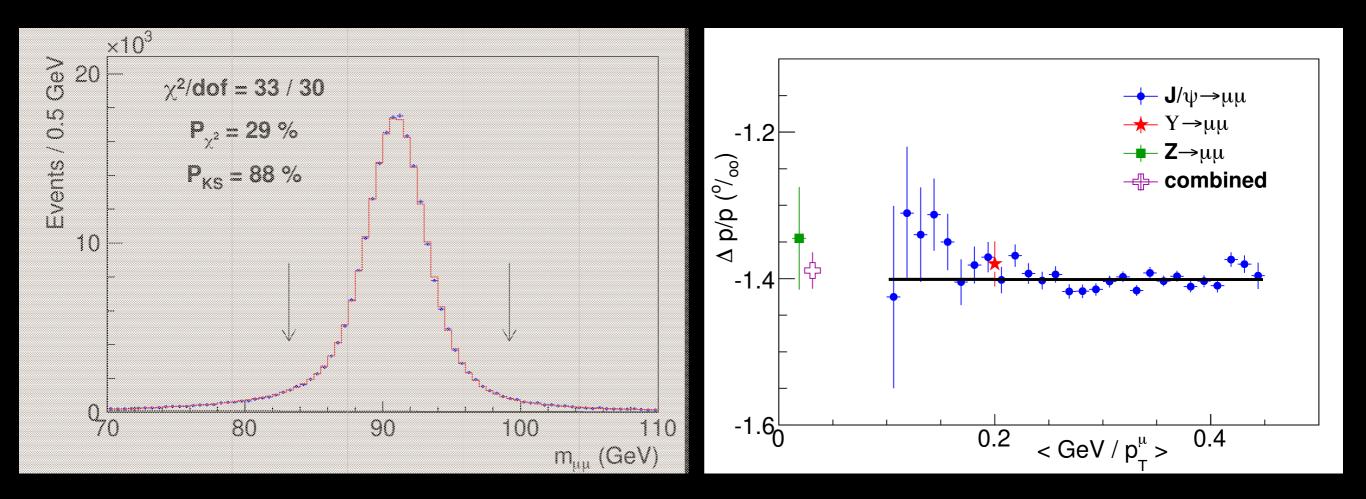
without constraint

with constraint

Final step is to measure the Z boson mass

 $M_Z = 91 \ 192.0 \pm 6.4_{stat} \pm 4.0_{sys} \ \text{MeV}$

Most precise determination of the Z boson mass at a hadron collider: uncertainty $3.6 \times LEP$ Combine all measurements into a final charged-track momentum scale

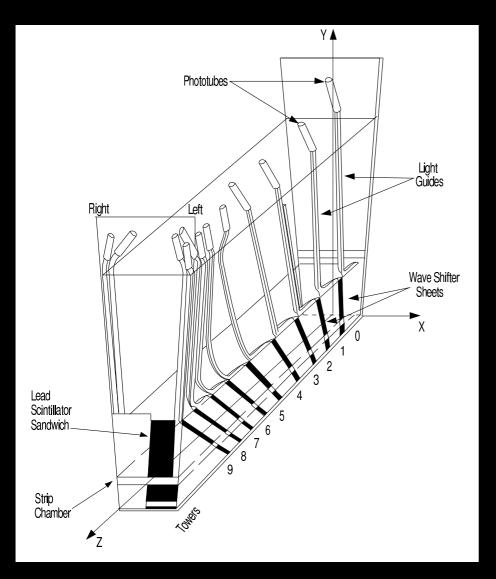


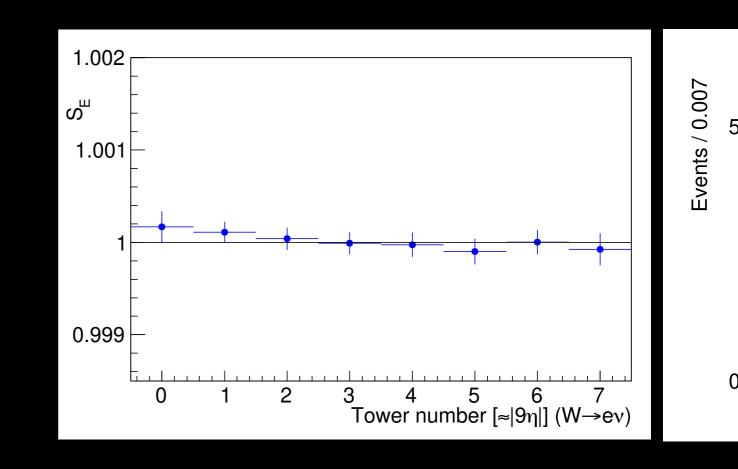
Electron momentum calibration

First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Data corrections:

Use mean E/p to remove time dependence & response variations in tower Fit ratio of calorimeter energy to track momentum to correct each tower in η

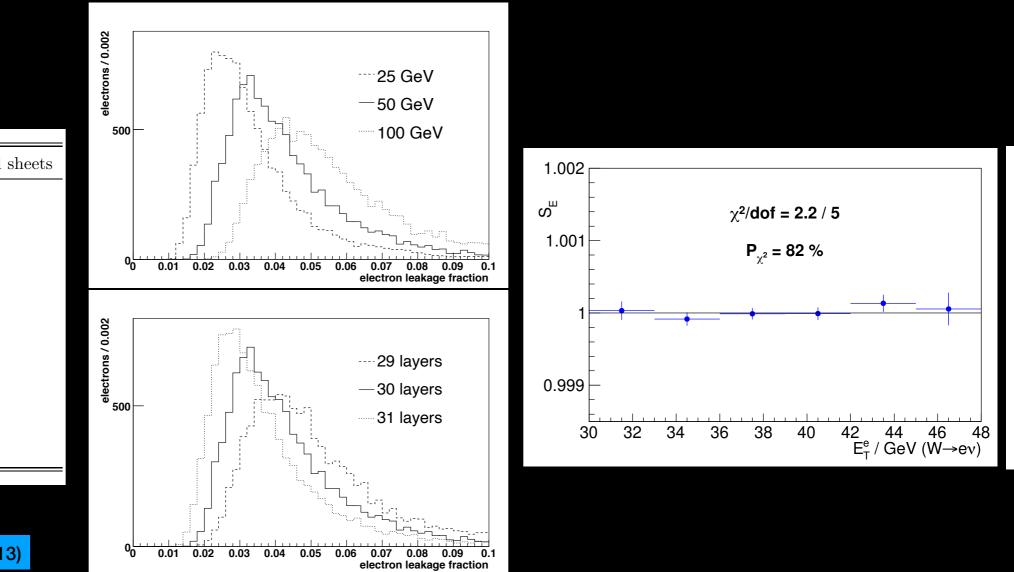




Electron momentum calibration

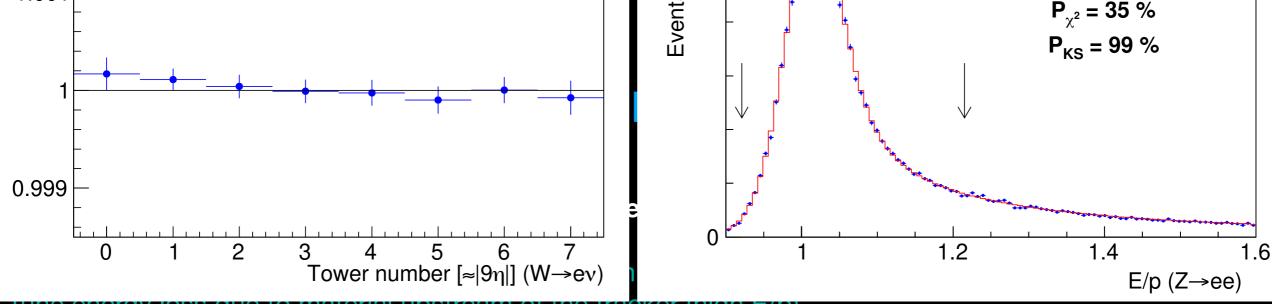
First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Parameterize calorimeter shower deposition and leakage based on GEANT4 Determine small calorimeter thickness corrections using region of low E/p in data Fit calorimeter scale as a function of E_T to correct for any remaining energy dependence



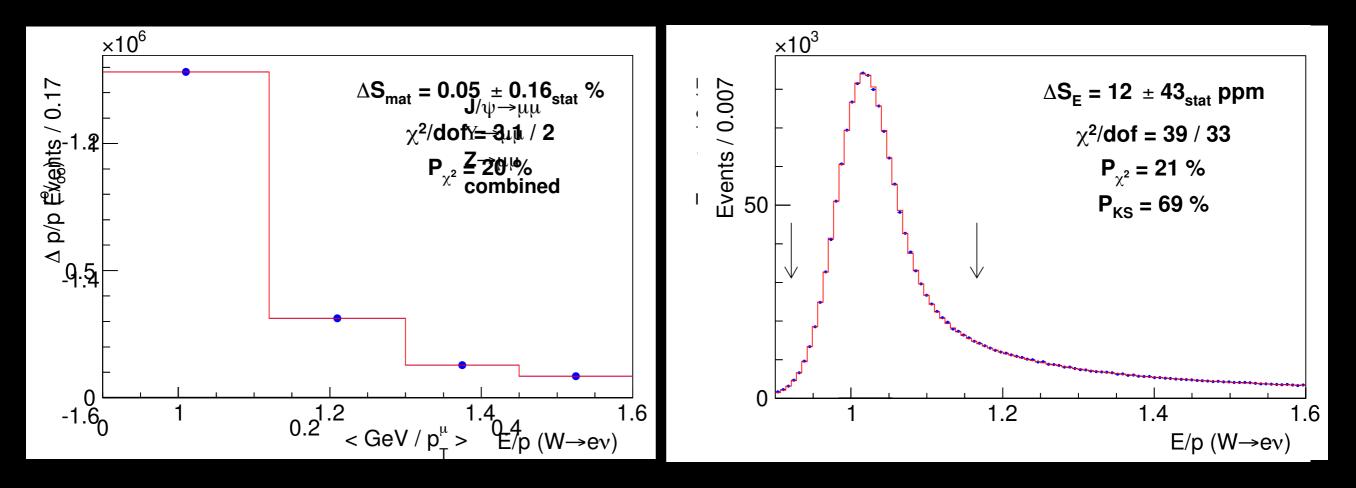
Tower	Thickness (x_0)	Number of lead sheets
0	17.9	30
1	18.2	30
2	18.2	29
3	17.8	27
4	18.0	26
5	17.7	24
6	18.1	23
7	17.7	21
8	18.0	20

Kotwal & CH, NIMA 729, 25 (2013)



Tune energy loss due to material upstream of the tracker (high E/p

Sampling resolution given by $\sigma_E/E = \sqrt{\frac{12.6\%}{E_T} + \kappa^2}$ with $\kappa = 0.7 - 1.1\%$ increasing with tower η



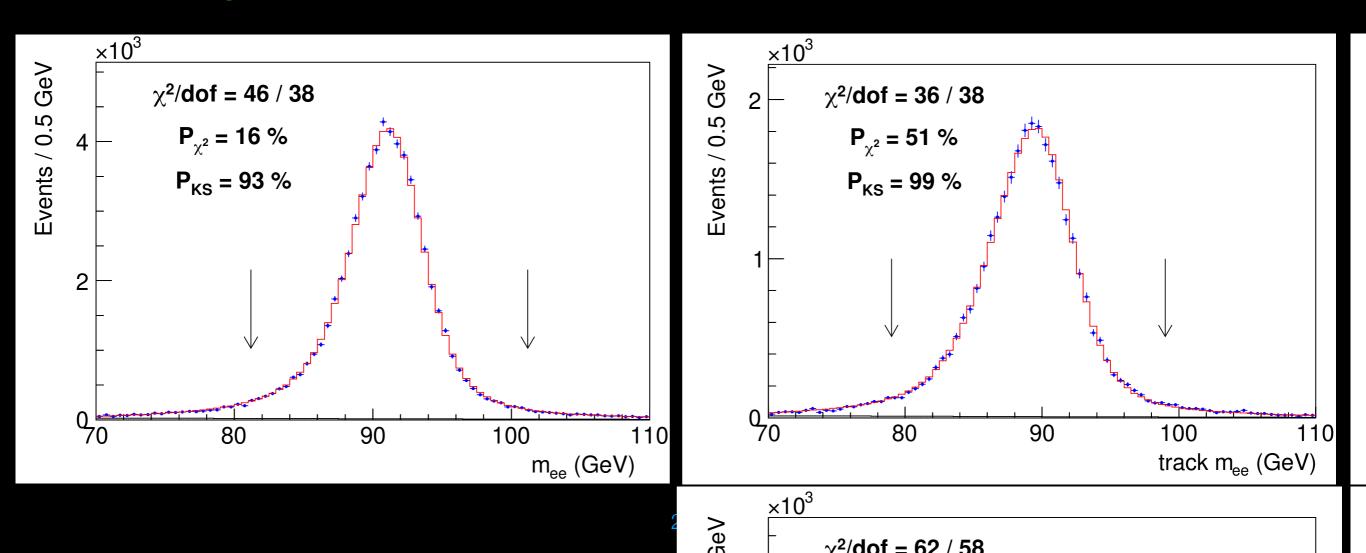
Electron momentum calibration

Second step is the measurement of the Z boson mass

 $M_Z = 91\ 194.3 \pm 13.8_{stat} \pm 7.6_{sys}$ MeV

As a consistency check measure mass using only track information e.g. $M_Z = 91\ 215.2 \pm 22.4$ MeV for non-radiative electrons (E/p<1.1)

Same blinding as for muon channel



Recoil momentum calibration

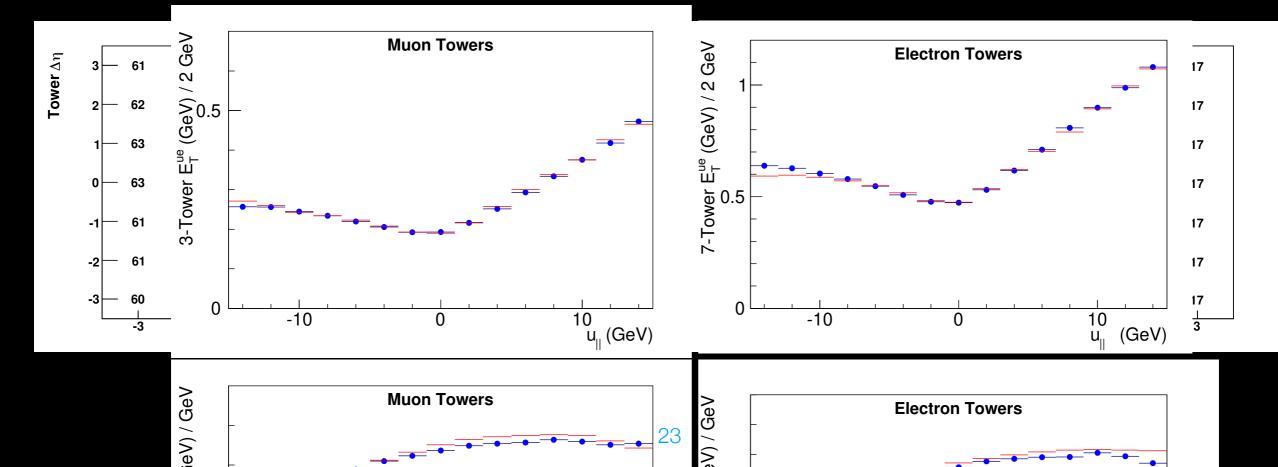
 ϕ_u

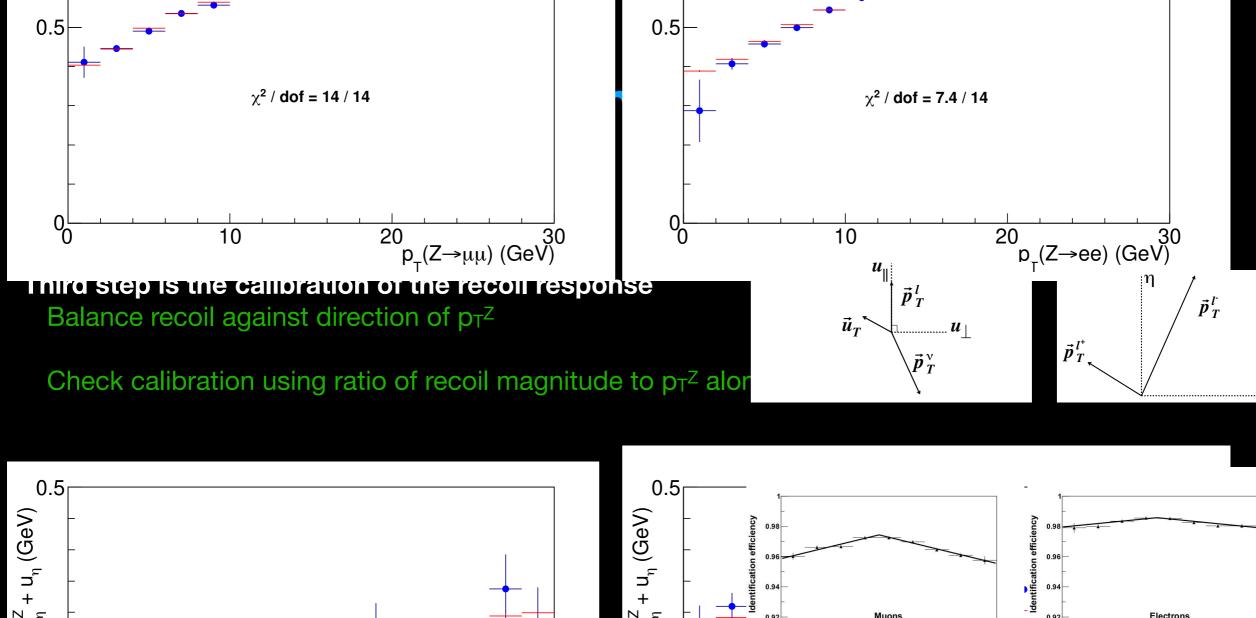
First step is the alignment of the calorimeters

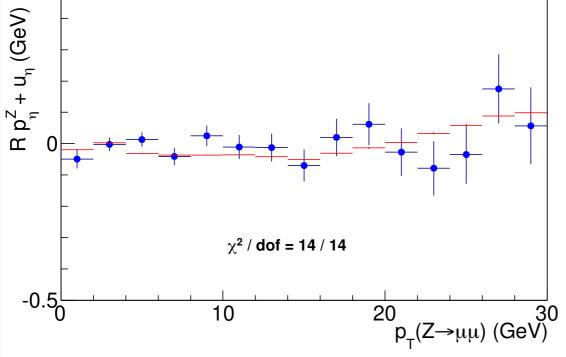
Misalignments relative to the beam axis cause a modulation in the recoil direction Alignment performed separately for each run period using minimum-bias data

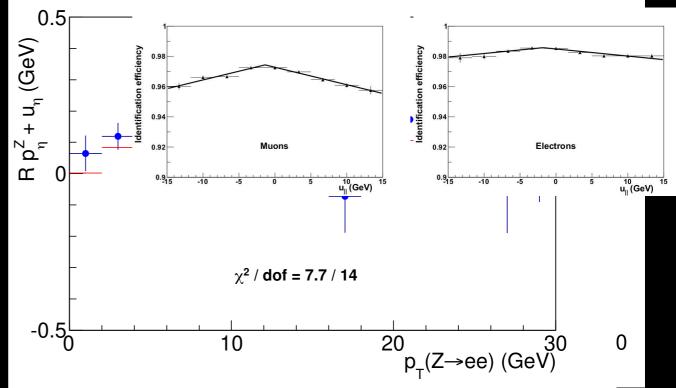
Second step is the reconstruction of the recoil

Remove towers traversed by identified leptons Remove corresponding recoil energy in simulation using towers rotated by 90° validate using towers rotated by 180°







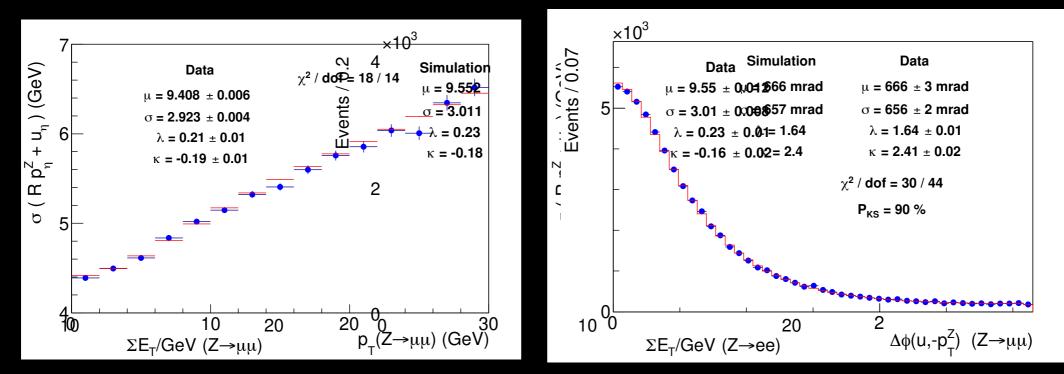


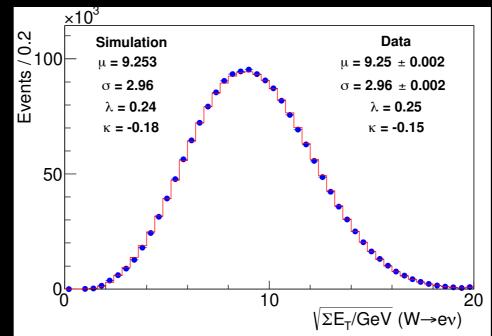
rec L

Recoil momentum calibration

Fourth step is the calibration of the recoil resolution

Includes jet-like energy and angular resolution, additional dijet fraction term, and pileup

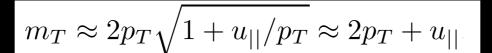




Recoil momentum validation

W boson recoil distributions validate the model

Most important is the recoil projected along the charged-lepton's momentum $(u_{||})$

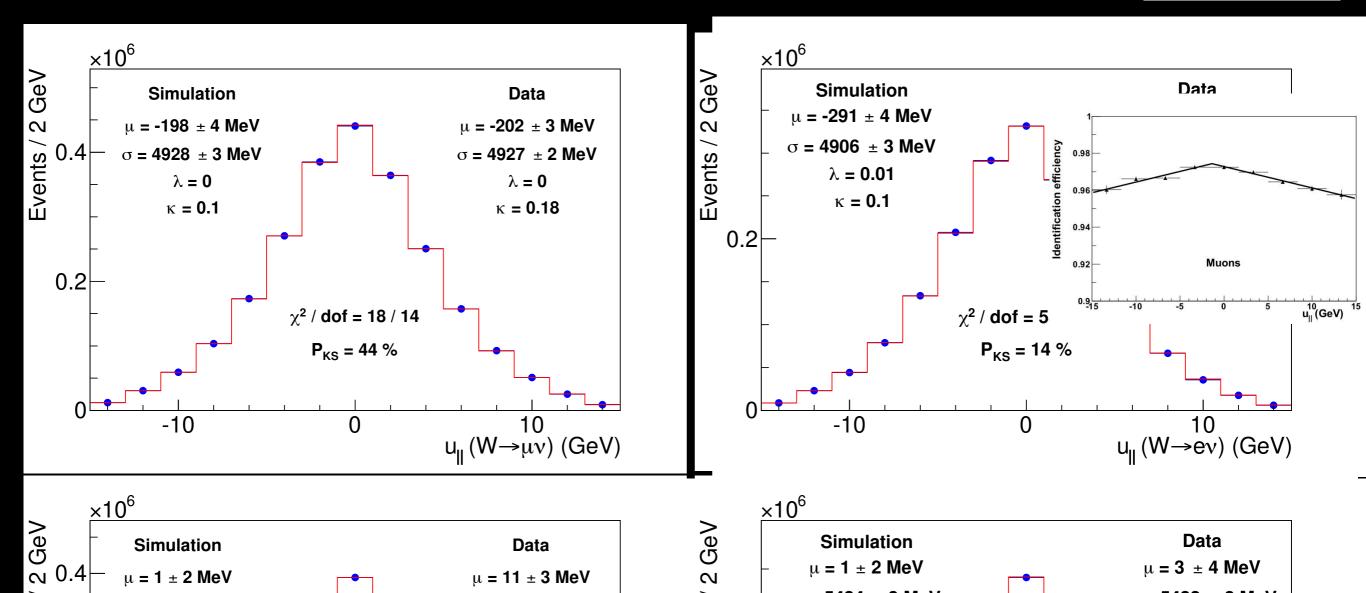


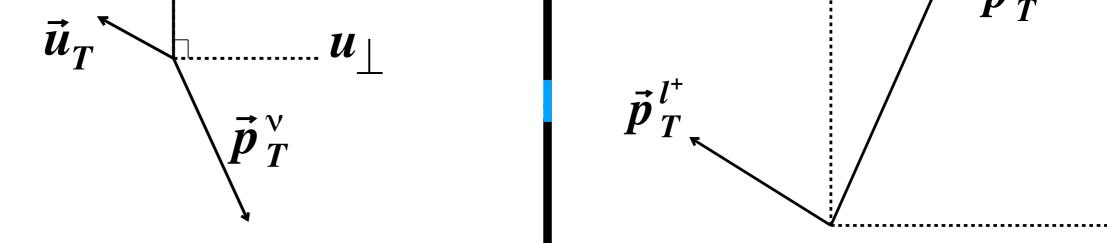
 \vec{u}_T

 \vec{p}_T^l

 \vec{p}_T^{ν}

 u_{\parallel}

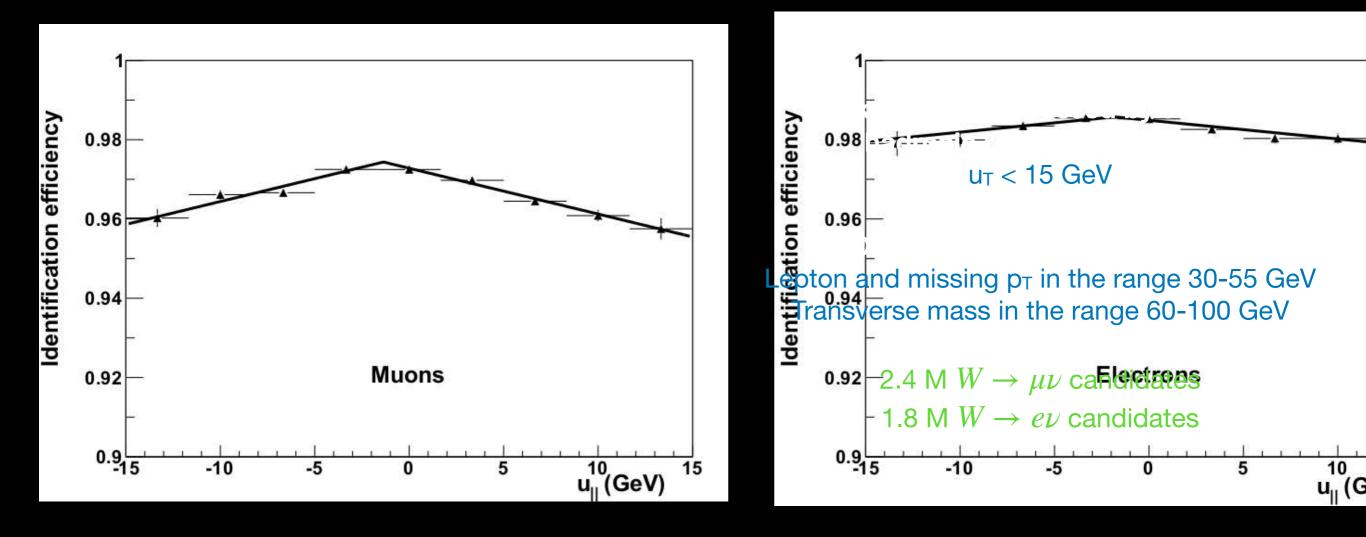


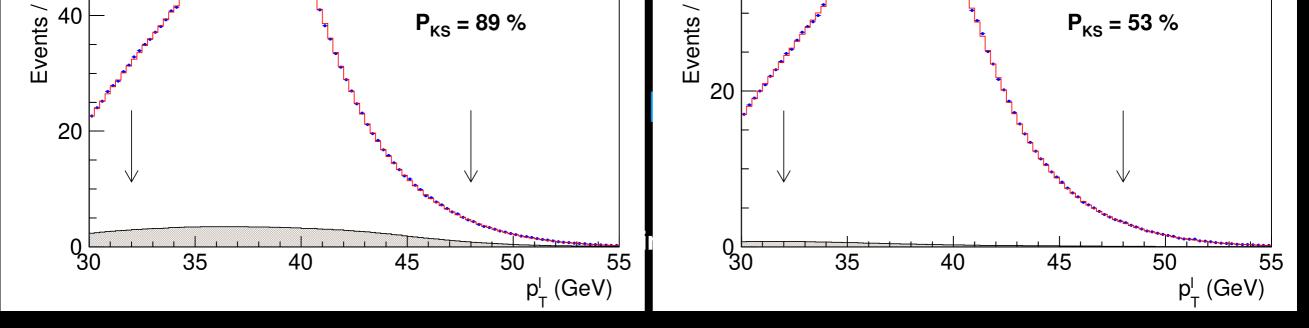


Triggers with low momentum thresholds (18 GeV) and very loose lepton id

Offline id also loose, efficiencies vary by 2% as hadronic recoil direction changes

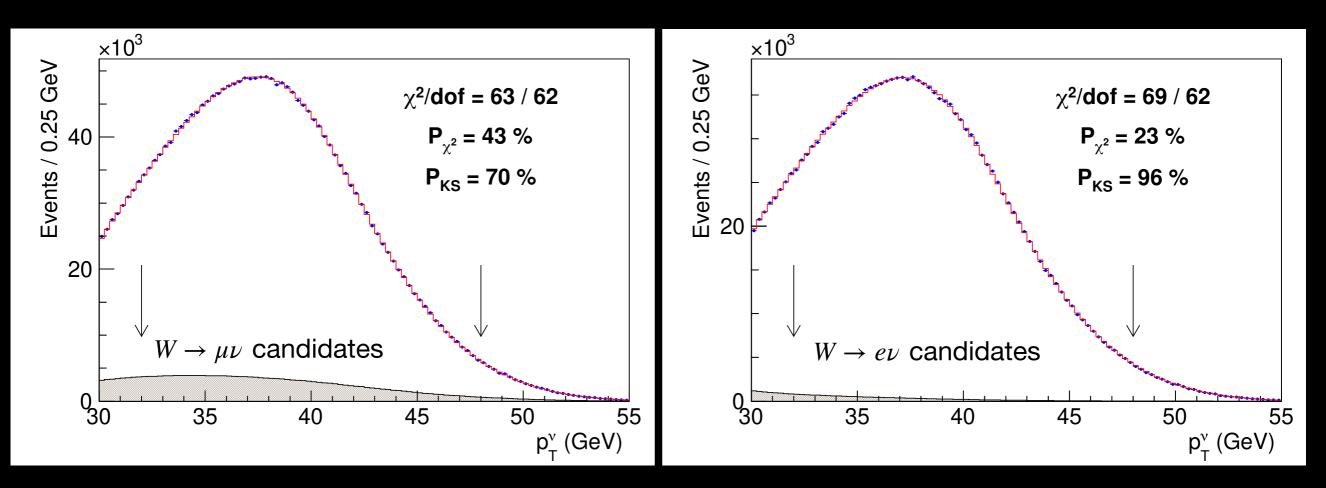
No lepton isolation requirement in trigger or offline selection





Largest background is $Z \rightarrow \mu\mu$ with one unreconstructed muon: **7.4% of data sample** $W \rightarrow \tau\nu$ background is ~1% in each channel: largest background in electron sample

Background from hadrons misreconstructed as leptons estimated using data: 0.2-0.3%



W boson transverse momentum

Boson p_T impacts the p_T distributions of the decay leptons

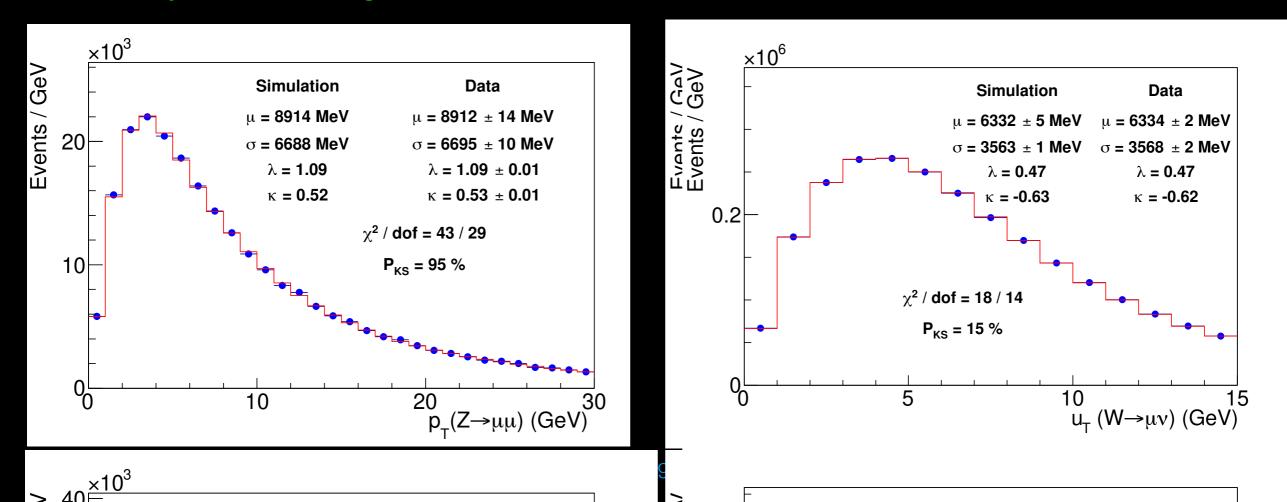
Transverse mass insensitive to p_T^W to first order

Resbos used to generate events with non-perturbative parameters and NNLL resummation to model the region of low boson p_T

Z boson p_T used to constrain the non-perturbative parameter g₂ and the perturbative coupling α_s

Resbos models W boson p_T well

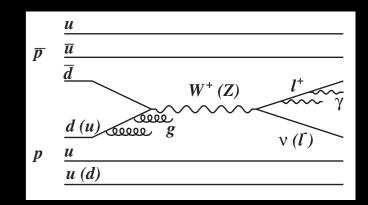
uncertainty estimated using DYQT renormalization and resummation variations & constrained with data



W boson production and decay

Parton distributions impact the measurement through lepton acceptance Restriction in η reduces the fraction of low-p_T leptons

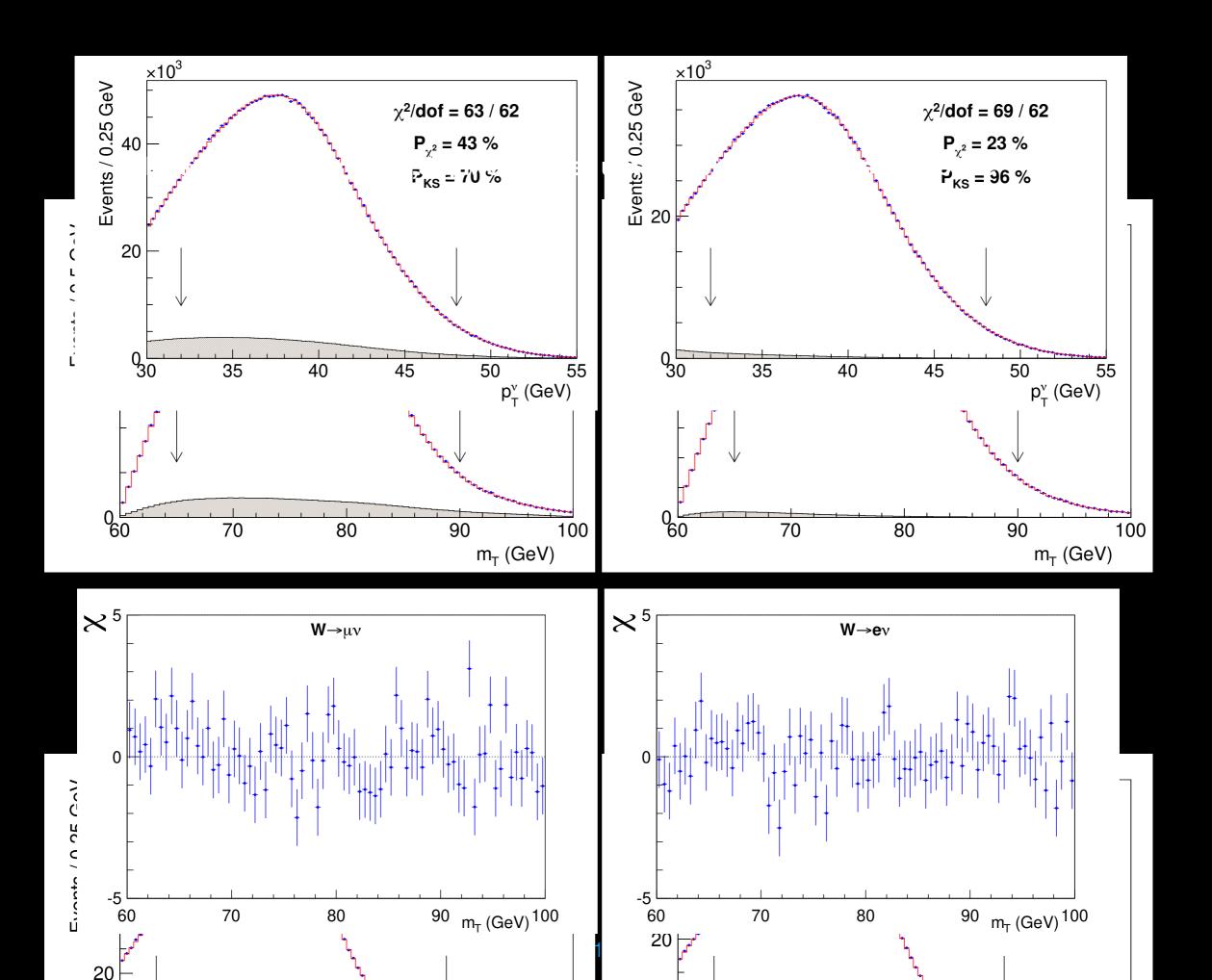
Small correction applied to update to NNPDF3.1 NNLO PDF The set with the most W charge asymmetry measurements at the time

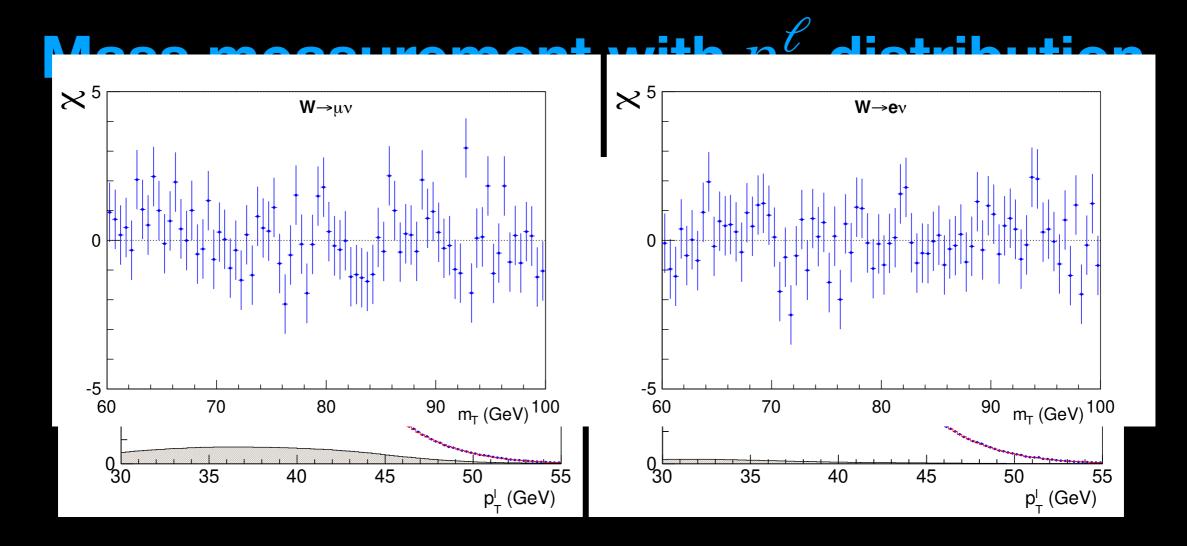


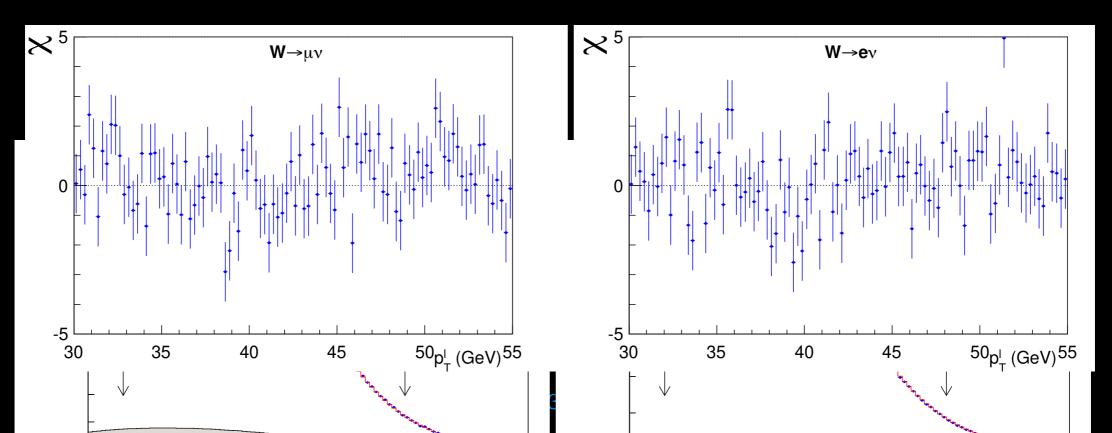
Uncertainty determined using a principal component analysis on the replica set

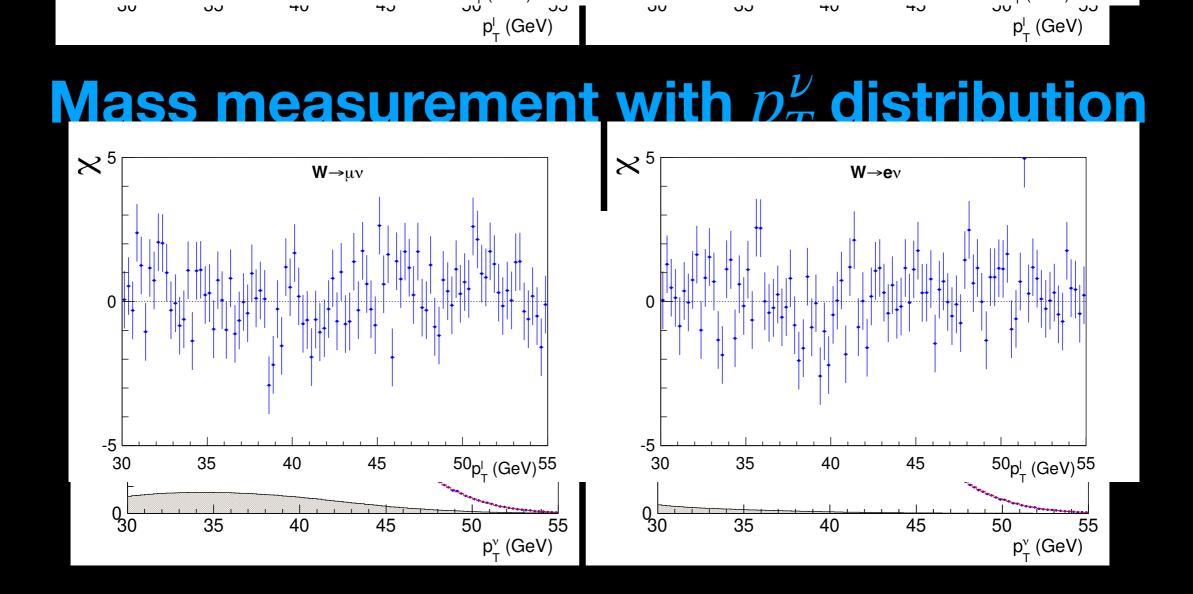
Measurement sensitive to ~15 eigenvectors Leading 25 eigenvectors used to estimate uncertainty (3.9 MeV) Three general NNLO PDF sets (NNPDF3.1, CT18, and MMHT14) have a range of ± 2.1 MeV from mean

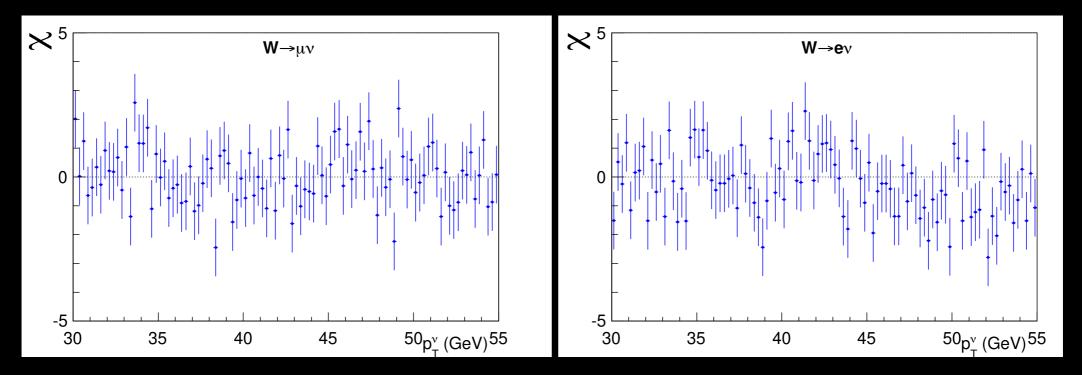
Photos resummation with ME corrections used to model final-state photon radiation validated by studying the average radiation in EM towers around the charged lepton, and with the Z mass measurement





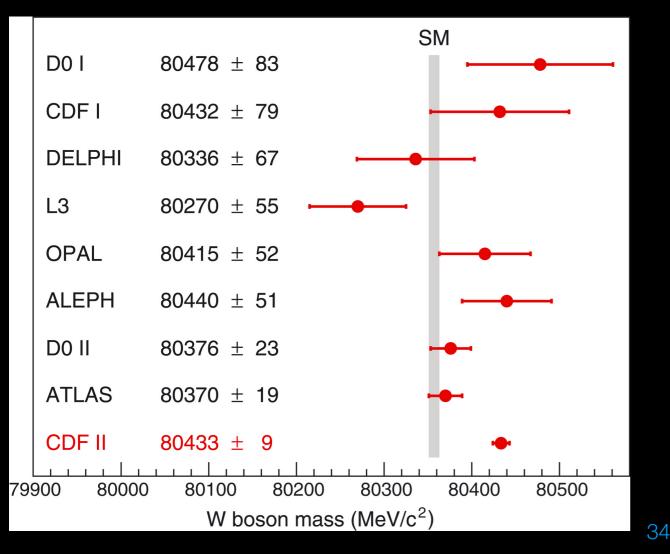


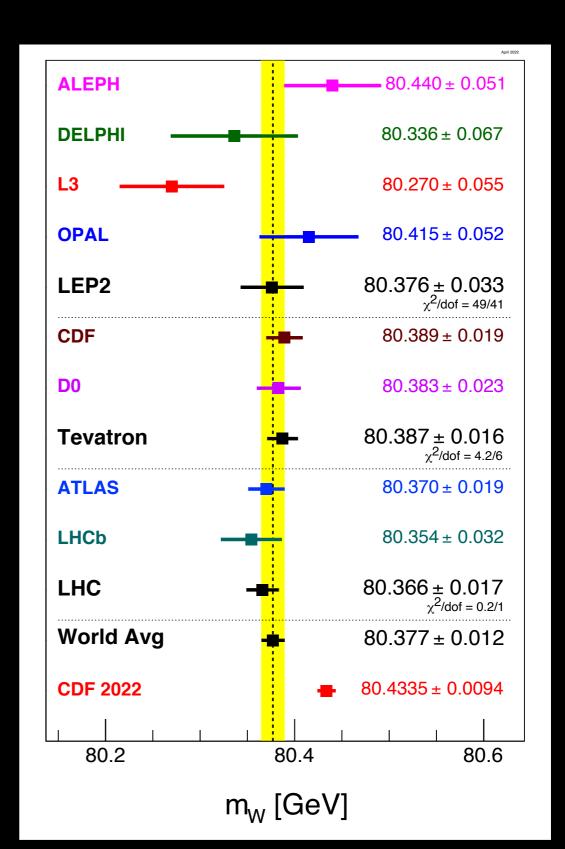




W boson mass measurements

Distribution	W-boson mass (MeV)	$\chi^2/{ m dof}$
$\overline{m_T(e, u)}$	$80~429.1 \pm 10.3_{\rm stat} \pm 8.5_{\rm syst}$	39/48
$p_T^\ell(e)$	$80~411.4 \pm 10.7_{\rm stat} \pm 11.8_{\rm syst}$	83/62
$p_T^ u(e)$	$80~426.3 \pm 14.5_{\rm stat} \pm 11.7_{\rm syst}$	69/62
$m_T(\mu, u)$	$80446.1 \pm 9.2_{\rm stat} \pm 7.3_{\rm syst}$	50/48
$p_T^\ell(\mu)$	$80~428.2 \pm 9.6_{\rm stat} \pm 10.3_{\rm syst}$	82/62
$p_T^ u(\mu)$	$80~428.9 \pm 13.1_{\rm stat} \pm 10.9_{\rm syst}$	63/62
combination	$80~433.5\pm6.4_{\rm stat}\pm6.9_{\rm syst}$	7.4/5





W boson mass measurements

Combination	m_T f	fit	p_T^ℓ f	it	$p_T^{ u}$ f	it	Value (MeV)	$\chi^2/{ m dof}$	Probability
	Electrons	Muons	Electrons	Muons	Electrons	Muons			(%)
m_T	\checkmark	\checkmark					$80\ 439.0\pm9.8$	1.2 / 1	28
p_T^ℓ			\checkmark	\checkmark			$80\ 421.2 \pm 11.9$	0.9 / 1	36
$p_T^{ u}$					\checkmark	\checkmark	$80\ 427.7 \pm 13.8$	0.0 / 1	91
Electrons	\checkmark		\checkmark		\checkmark		$80\ 424.6 \pm 13.2$	3.3 / 2	19
Muons		\checkmark		\checkmark		\checkmark	$80\ 437.9 \pm 11.0$	3.6 / 2	17
All	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	$80\ 433.5 \pm 9.4$	7.4 / 5	20

Fit difference	Muon channel	Electron channel
$M_W(\ell^+) - M_W(\ell^-)$	$-7.8\pm18.5_{\rm stat}\pm12.7_{\rm COT}$	$14.7 \pm 21.3_{\text{stat}} \pm 7.7_{\text{stat}}^{\text{E/p}} (0.4 \pm 21.3_{\text{stat}})$
$M_W(\phi_\ell > 0) - M_W(\phi_\ell < 0)$	$24.4\pm18.5_{\rm stat}$	$9.9 \pm 21.3_{\text{stat}} \pm 7.5_{\text{stat}}^{\text{E/p}} (-0.8 \pm 21.3_{\text{stat}})$
$M_Z(\text{run} > 271100) - M_Z(\text{run} < 271100)$	$5.2 \pm 12.2_{\mathrm{stat}}$	$63.2 \pm 29.9_{\text{stat}} \pm 8.2_{\text{stat}}^{\text{E/p}} (-16.0 \pm 29.9_{\text{stat}})$



The W boson mass is an important parameter in particle physics

Measurement of W boson mass with <10 MeV precision achieved with complete CDF data set

Result of >20 years of experience with the CDF II detector

0.01% precision required flexibility: all experimental aspects controlled by the analysis team *Reconstruction, alignment, calibration, simulation, analysis*

Analysis procedures approved pre-unblinding and frozen

Surprising 0.1% deviation from SM motivates expanded study of m_W measurements and procedures

Future possibilities

Recoil tuning

Fine-tune calorimeter response corrections in data Calibrate a shower Monte Carlo

Recoil validation

Compare W & Z & Υ response in events with a single lepton (remove any additional lepton) Compare W & Z energy flows Compare W & Z lepton removal energy distributions Check electron removal towers for e⁺ vs e⁻, validate muons with nearby towers

Event generation

Generate events using a higher-order calculation Validate p_T^W using high/low p_T^I asymmetry Validate PDF using low p_T^I region and rapidity-dependent mass fits

Event selection

Vary lepton id (add isolation)

Analysis updates

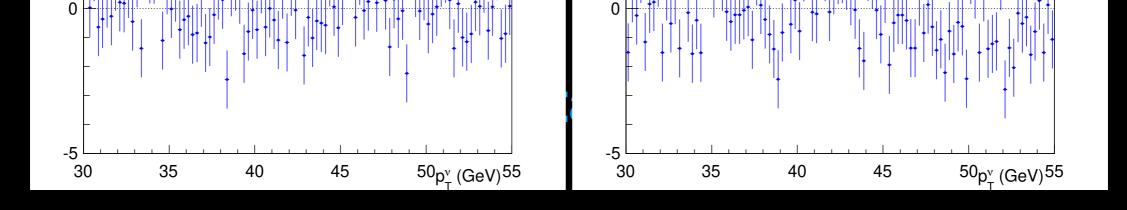
Identify the effect of each analysis change in the muon channel

Luminosity & time dependence

Fit mass in subsets in time or luminosity Perform pseudo-experiments to check KS probabilities

Muon resolution

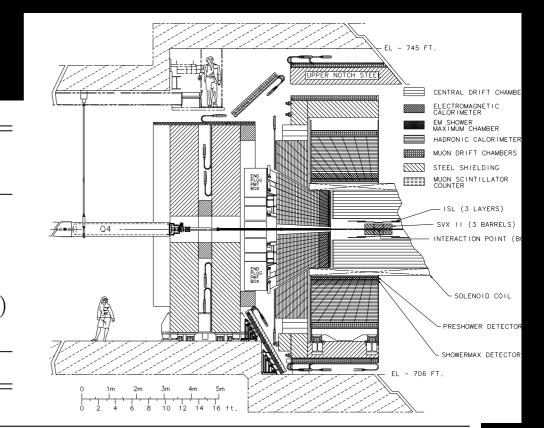
Implement beam spot size vs z and W vs Z z vertex distribution

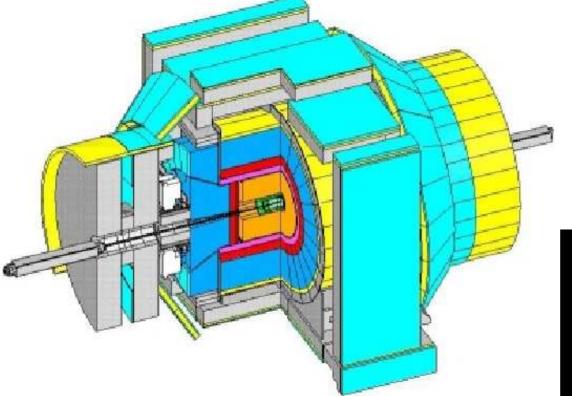


Source of systematic		m_T fit			p_T^ℓ fit			p_T^{ν} fit	
uncertainty	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton energy scale	5.8	2.1	1.8	5.8	2.1	1.8	5.8	2.1	1.8
Lepton energy resolution	0.9	0.3	-0.3	0.9	0.3	-0.3	0.9	0.3	-0.3
Recoil energy scale	1.8	1.8	1.8	3.5	3.5	3.5	0.7	0.7	0.7
Recoil energy resolution	1.8	1.8	1.8	3.6	3.6	3.6	5.2	5.2	5.2
Lepton $u_{ }$ efficiency	0.5	0.5	0	1.3	1.0	0	2.6	2.1	0
Lepton removal	1.0	1.7	0	0	0	0	2.0	3.4	0
Backgrounds	2.6	3.9	0	6.6	6.4	0	6.4	6.8	0
p_T^Z model	0.7	0.7	0.7	2.3	2.3	2.3	0.9	0.9	0.9
p_T^W/p_T^Z model	0.8	0.8	0.8	2.3	2.3	2.3	0.9	0.9	0.9
Parton distributions	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9
QED radiation	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7
Statistical	10.3	9.2	0	10.7	9.6	0	14.5	13.1	0
Total	13.5	11.8	5.8	16.0	14.1	7.9	18.8	17.1	7.4

Background fractions

	Fraction	δ	δM_W (MeV	7)
Source	(%)	m_T fit	p_T^{μ} fit	p_T^{ν} fit
$Z/\gamma^* \to \mu\mu$	7.37 ± 0.10	1.6(0.7)	3.6(0.3)	0.1(1.5)
$W \to \tau \nu$	0.880 ± 0.004	$0.1 \ (0.0)$	$0.1 \ (0.0)$	0.1(0.0)
Hadronic jets	0.01 ± 0.04	$0.1 \ (0.8)$	-0.6(0.8)	2.4(0.5)
Decays in flight	0.20 ± 0.14	1.3(3.1)	1.3(5.0)	-5.2(3.2)
Cosmic rays	0.01 ± 0.01	0.3(0.0)	0.5~(0.0)	0.3(0.3)
Total	8.47 ± 0.18	2.1(3.3)	3.9(5.1)	5.7(3.6)





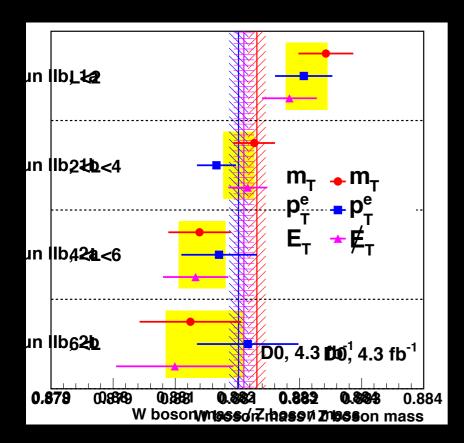
	Fraction	8	δM_W (Me	V)
Source	(%)	m_T fit	p_T^e fit	p_T^{ν} fit
$Z/\gamma^* \to ee$	0.134 ± 0.003	0.2(0.3)	0.3(0.0)	0.0(0.6)
$W \to \tau \nu$	0.94 ± 0.01	0.6(0.0)	0.6(0.0)	0.6~(0.0)
Hadronic jets	0.34 ± 0.08	2.2(1.2)	0.9(6.5)	6.2(-1.1)
Total	1.41 ± 0.08	2.3(1.2)	1.1 (6.5)	6.2(1.3)

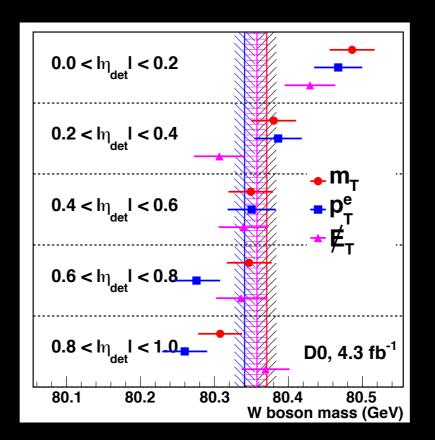
W boson mass measurements

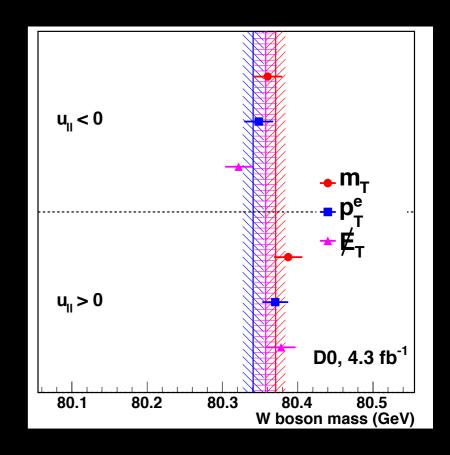
Data FAST MC

Data FAST MC

Subset LHCb	$\chi^2_{\rm tot}/{\rm ndf}$	$\delta m_W \; [\mathrm{MeV}]$
Polarity = -1	92.5/102	—
Polarity = +1	97.3/102	-57.5 ± 45.4
$\eta > 3.3$	115.4/102	_
$\eta < 3.3$	85.9/102	$+56.9\pm45.5$
Polarity $\times q = +1$	95.9/102	_
Polarity $\times q = -1$	98.2/102	$+16.1\pm45.4$
$ \phi > \pi/2$	98.8/102	_
$ \phi < \pi/2$	115.0/102	$+66.7\pm45.5$
$\phi < 0$	91.8/102	_
$\phi > 0$	103.0/102	-100.5 ± 45.3



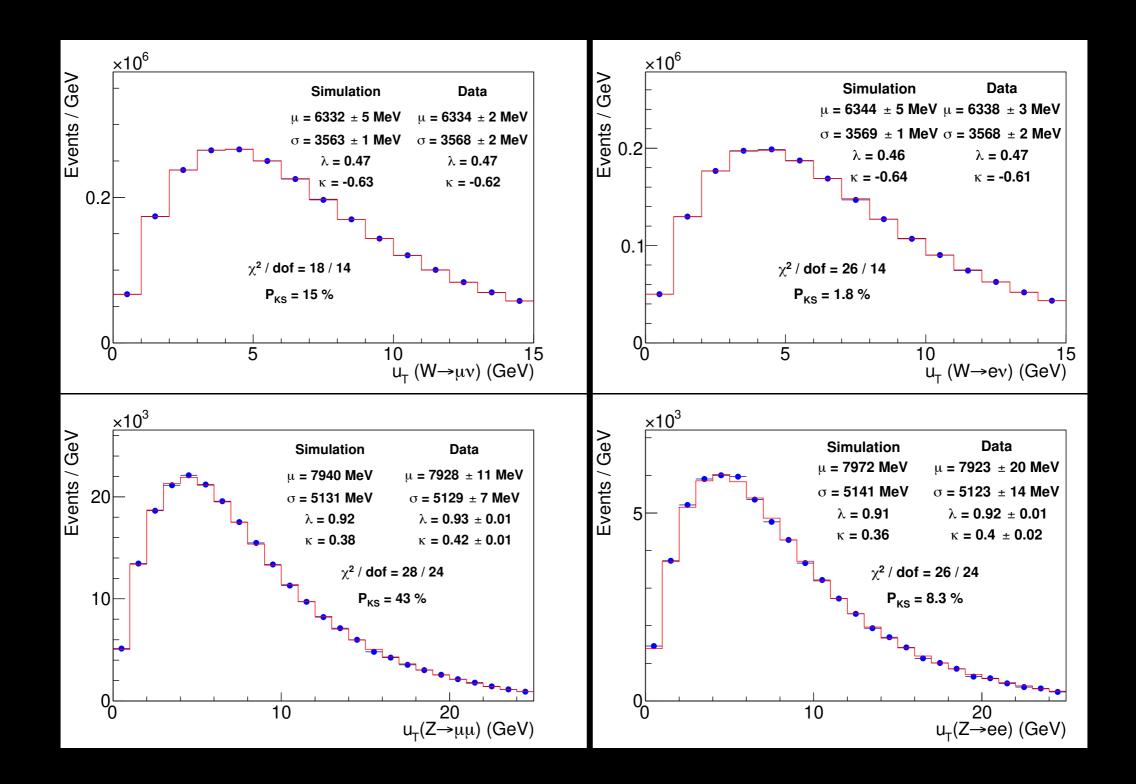




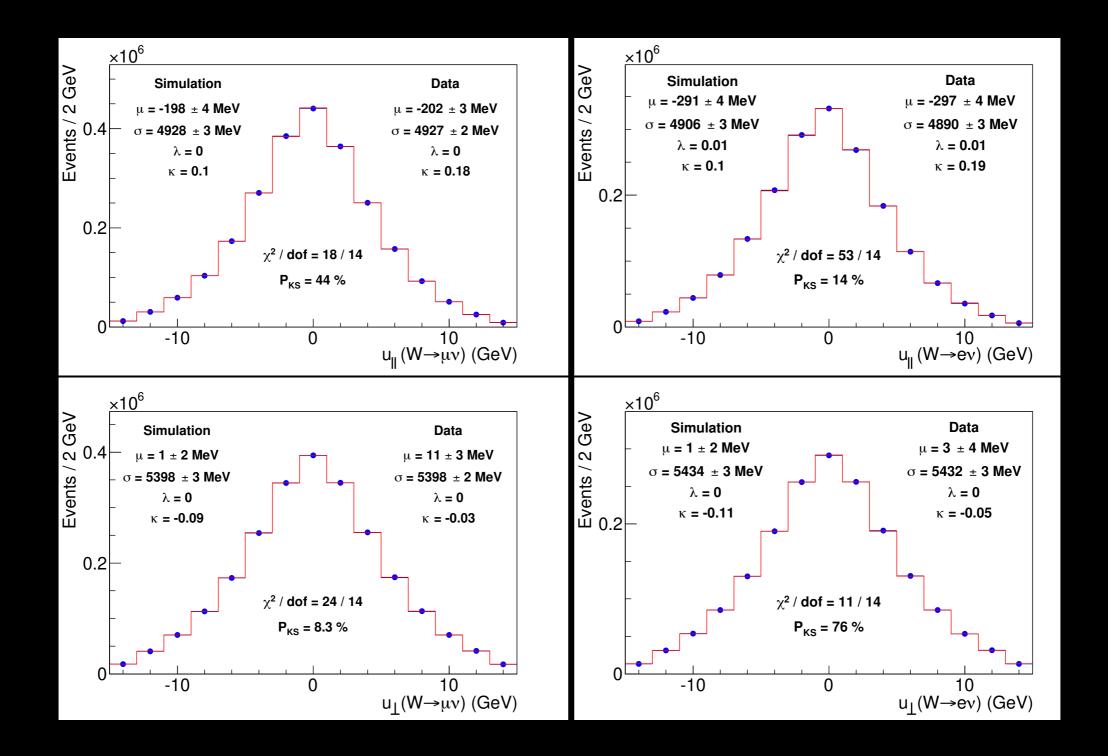
Initial state LO & NLO

W+ initial	Туре	Pythia LO	Madgraph LO	Madgraph NLO
u dbar	V-V	81.7%	82.0%	82.7%
dbar u	S-S	8.9%	9.0%	8.8%
u sbar	V-S	1.6%	1.9%	1.8%
sbar u	S-S	0.3%	0.3%	0.3%
c sbar	S-S	2.9%	2.9%	-
sbar c	S-S	2.9%	2.9%	-
c dbar	S-V	0.7%	0.7%	_
dbar c	S-S	0.2%	0.2%	-
u g	v-g		-	3.7%
g dbar	g-v		-	1.8%
g u	g-s		-	0.4%
dbar g	s-g		-	0.5%
g sbar	g-s		_	0.02%
sbar g	s-g		-	0.02%

Recoil in W & Z events

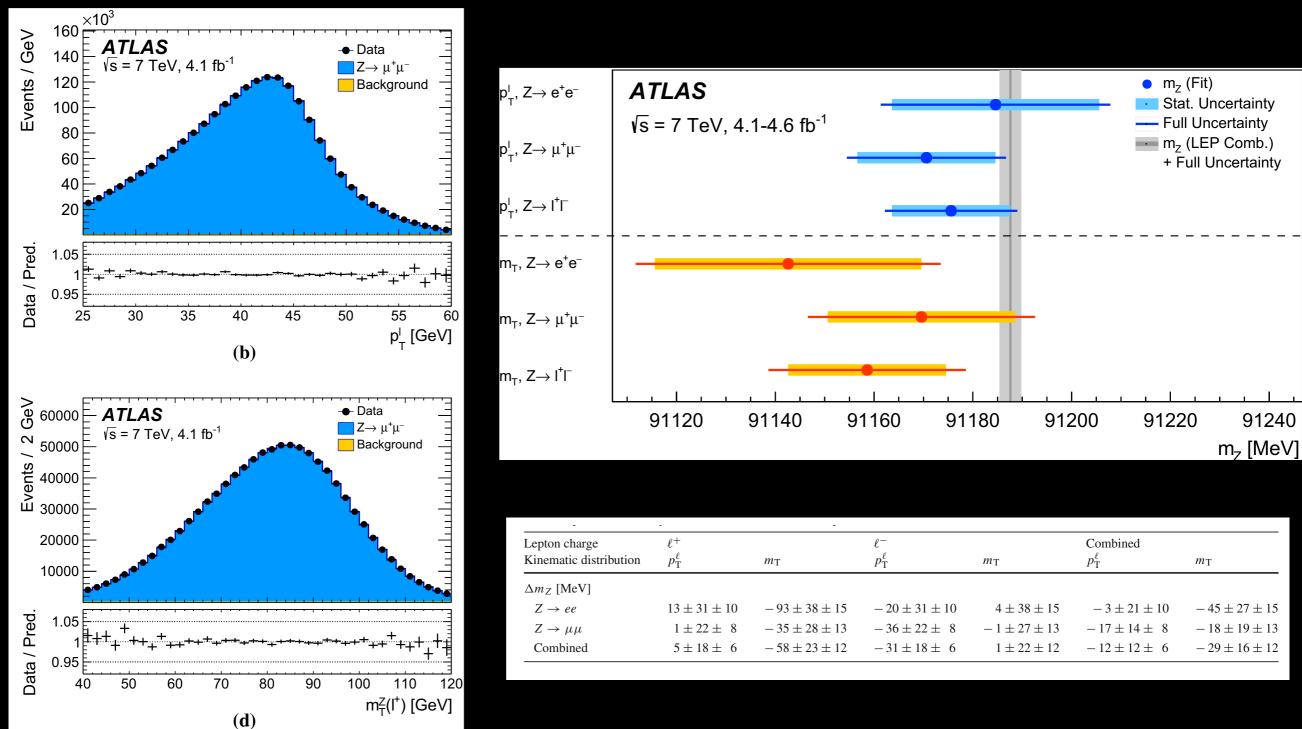


Recoil projections in W events



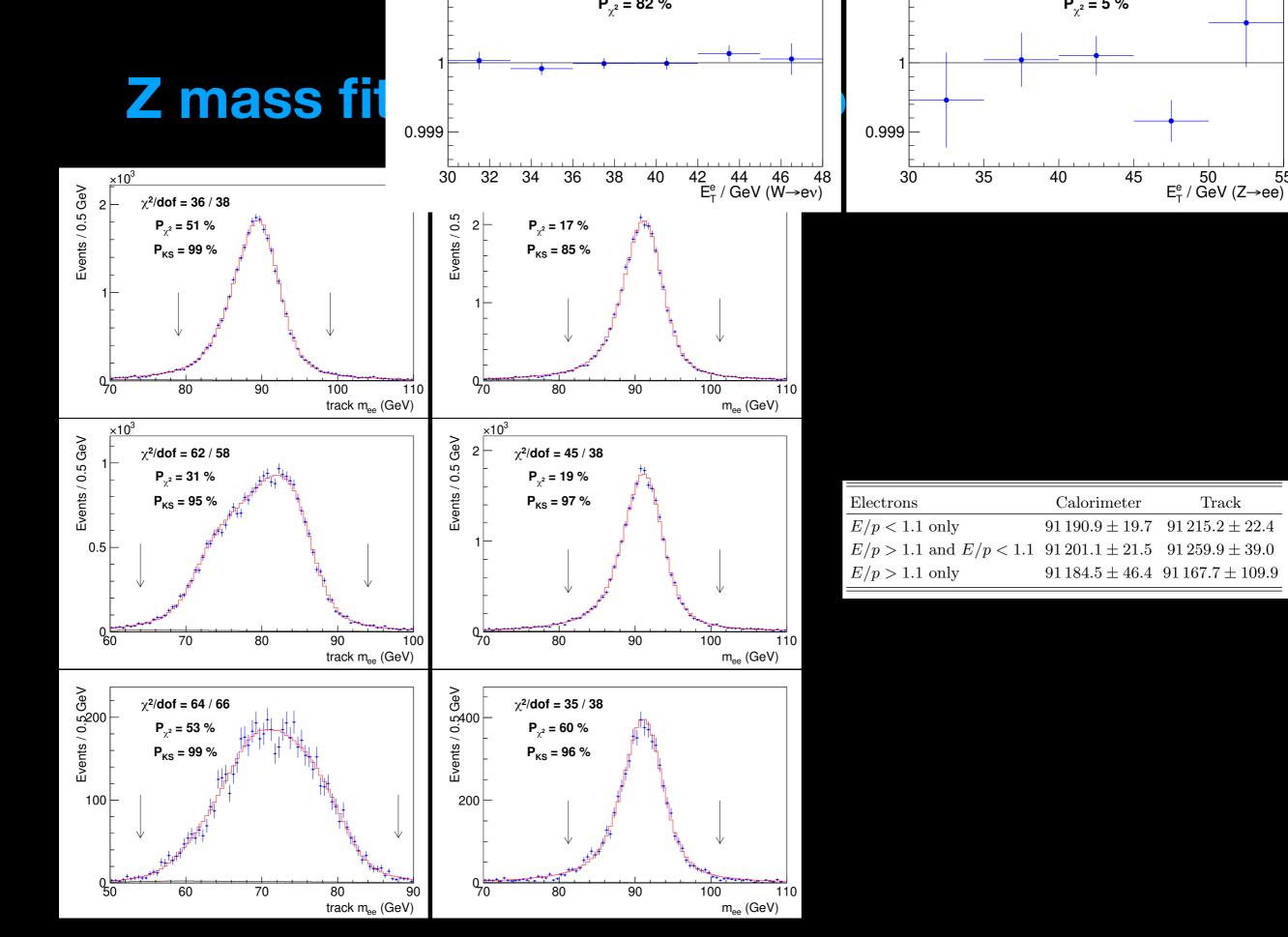
Recoil momentum validation

ATLAS validates the recoil model with single-lepton Z boson mass measurements



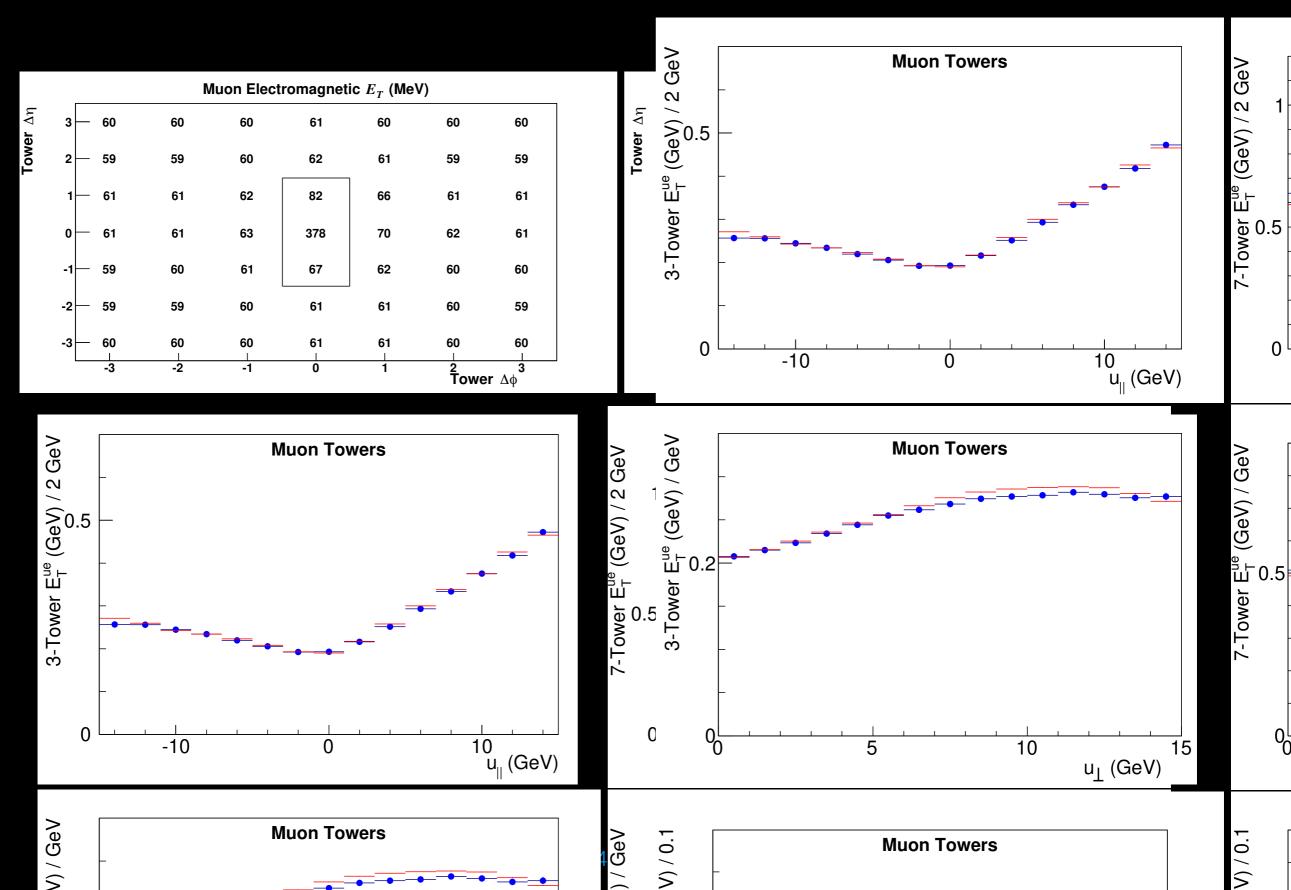
Recoil model parameters

Parameter	Description	Source	m_T	p_T^ℓ	p_T^{ν}
a	average response	Fig. S23	-1.6	-2.9	-0.2
b	response non-linearity	Fig. S23	-0.8	-2.0	0.7
Response			1.8	3.5	0.7
N_V	spectator interactions	Fig. S24	0.5	-3.2	3.6
$s_{ m had}$	sampling resolution	Fig. S24	0.3	0.3	0.8
$f_{\pi^0}^4$	EM fluctuations at low u_T	Fig. S25	-0.3	-0.2	-1.0
$f_{\pi^0}^{15}$	EM fluctuations at high u_T	Fig. S25	-0.3	-0.3	-0.2
α	angular resolution at low u_T	Fig. S26	1.4	0.1	2.5
β	angular resolution at intermediate u_T	Fig. S26	0.2	0.1	0.7
γ	angular resolution at high u_T	Fig. S26	0.3	0.3	0.7
f_2^a	average dijet component	Fig. S27	0.1	-1.1	0.8
f_2^s	variation of dijet component with u_T	Fig. S27	-0.1	-0.2	-0.1
k_{ξ}	average dijet resolution	Fig. S28	-0.1	0.1	-0.3
δ_{ξ}	fluctuations in dijet resolution	Fig. S28	-0.2	0.2	-1.1
A_{ξ}	higher-order term in dijet resolution	Fig. S28	0.1	-1.0	0.7
μ_{ξ}		Fig. S28	-0.5	-0.4	-0.9
ϵ_{ξ}		Fig. S28	0.1	-0.2	0.4
S_{ξ}^+		Fig. S28	0.5	-0.4	1.4
S_{ξ}^{-}	11	Fig. S28	-0.3	-0.2	-0.5
q_{ξ}	11	Fig. S28	-0.2	0.0	0.2
Resolution			1.8	3.6	5.2



Track

Recoil reconstruction in muon channel

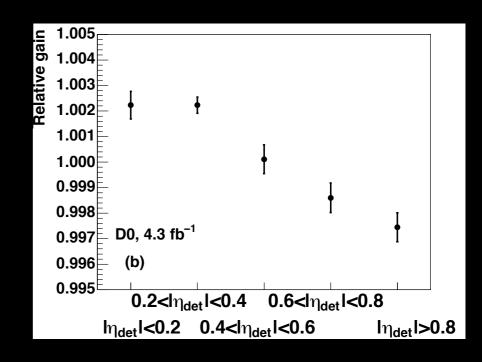


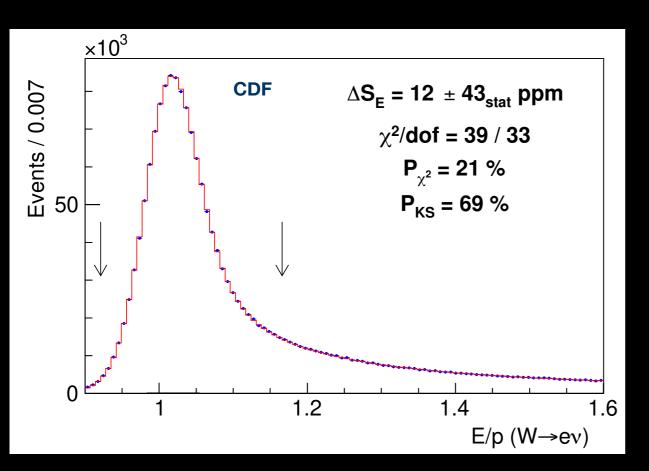
Electron momentum calibration

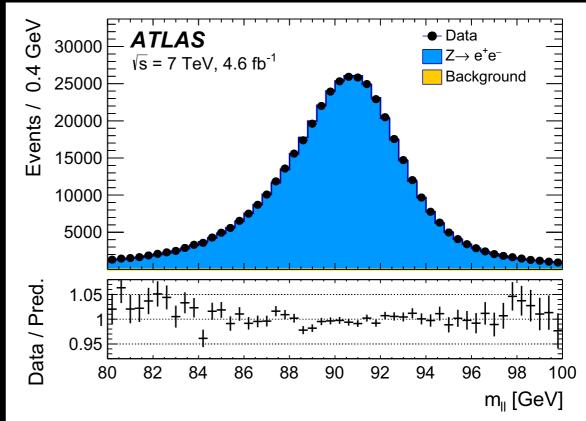
Third step is to calibrate the response

CDF: Transfer track momentum calibration to calorimeter using (E/p) distribution, combine with calibration from $Z \rightarrow ee$ decays

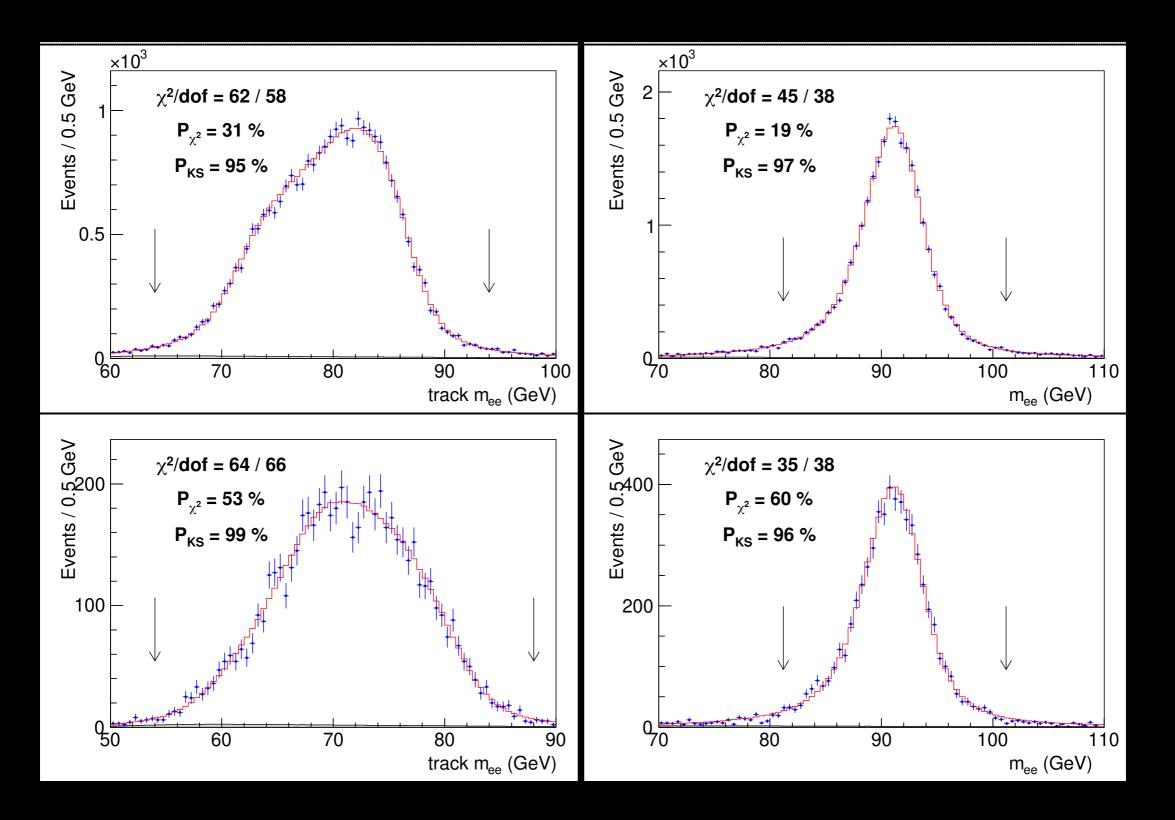
ATLAS & DO: Calibrate energy as a function of pseudorapidity using $Z \rightarrow ee$ decays







Electron momentum calibration



Muon momentum calibration

Source	J/ψ (ppm)	Υ (ppm)	Correlation $(\%)$
QED	1	1	100
Magnetic field non-uniformity	13	13	100
Ionizing material correction	11	8	100
Resolution model	10	1	100
Background model	7	6	0
COT alignment correction	4	8	0
Trigger efficiency	18	9	100
Fit range	2	1	100
$\Delta p/p$ step size	2	2	0
World-average mass value	4	27	0
Total systematic	29	34	16 ppm
Statistical NBC (BC)	2	13(10)	0
Total	29	36	16 ppm

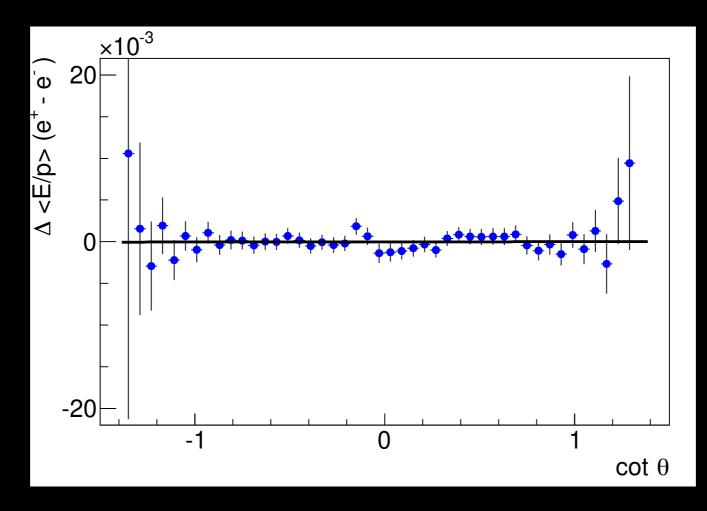
Track momentum calibration

Residual tracker misalignments studied using difference in E/p between electrons and positrons

Correction as a function of polar angle applied to measured tracks from W and Z decays

Linear dependence on cot theta would cause a bias in the m_W mass fit

No linear correction required, statistical precision from E/p constrains the bias to <0.8 MeV



Measurement updates

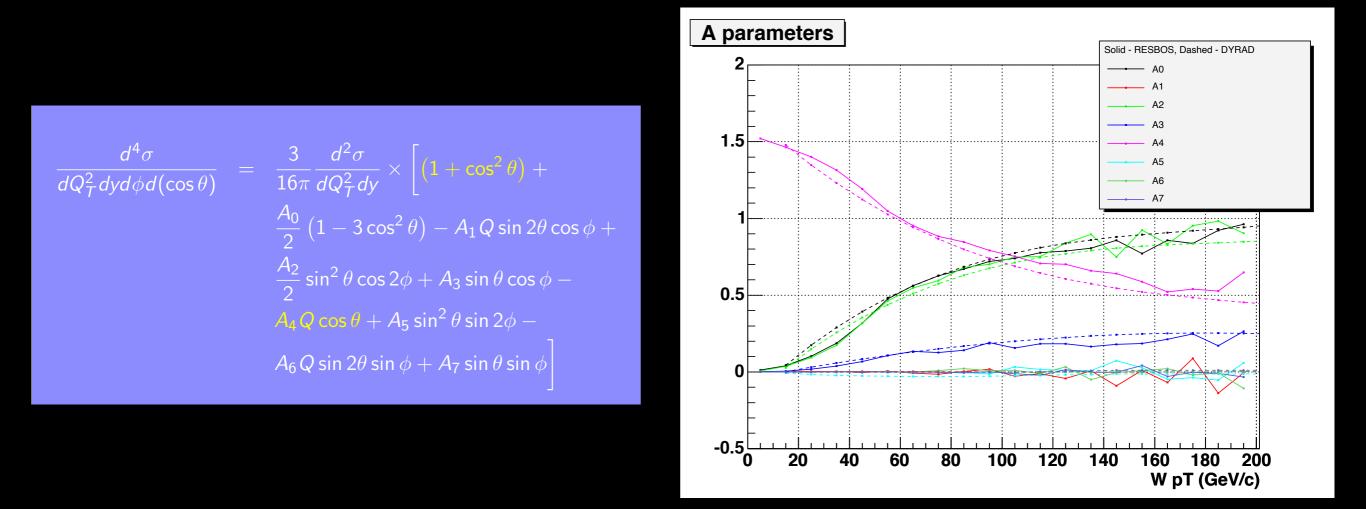
Method or technique	impact
Detailed treatment of parton distribution functions	+3.5 MeV
Resolved beam-constraining bias in CDF reconstruction	+10 MeV
Improved COT alignment and drift model [65]	uniformity
Improved modeling of calorimeter tower resolution	uniformity
Temporal uniformity calibration of CEM towers	uniformity
Lepton removal procedure corrected for luminosity	uniformity
Higher-order calculation of QED radiation in J/ψ and Υ decays	accuracy
Modeling kurtosis of hadronic recoil energy resolution	accuracy
Improved modeling of hadronic recoil angular resolution	accuracy
Modeling dijet contribution to recoil resolution	accuracy
Explicit luminosity matching of pileup	accuracy
Modeling kurtosis of pileup resolution	accuracy
Theory model of p_T^W/p_T^Z spectrum ratio	accuracy
Constraint from p_T^W data spectrum	robustness
Cross-check of p_T^Z tuning	robustness

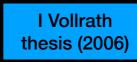
W boson mass fit results

Distribution	W-boson mass (MeV)	$\chi^2/{ m dof}$
$m_T(e, u)$	$80~429.1 \pm 10.3_{\rm stat} \pm 8.5_{\rm syst}$	39/48
$p_T^\ell(e)$	$80~411.4 \pm 10.7_{\rm stat} \pm 11.8_{\rm syst}$	83/62
$p_T^{ u}(e)$	$80\ 426.3 \pm 14.5_{\rm stat} \pm 11.7_{\rm syst}$	69/62
$m_T(\mu, u)$	$80\ 446.1 \pm 9.2_{\rm stat} \pm 7.3_{\rm syst}$	50/48
$p_T^\ell(\mu)$	$80~428.2 \pm 9.6_{\rm stat} \pm 10.3_{\rm syst}$	82/62
$p_T^ u(\mu)$	$80\ 428.9 \pm 13.1_{\rm stat} \pm 10.9_{\rm syst}$	63/62
combination	$80\ 433.5 \pm 6.4_{\rm stat} \pm 6.9_{\rm syst}$	7.4/5

Distribution	M_W (MeV)	$\chi^2/d.o.f.$
$W \rightarrow e\nu$		
m_T	80408 ± 19	52/48
$p_T^{\hat{\ell}}$	80393 ± 21	60/62
p_T^{ν}	80431 ± 25	71/62
$W \to \mu\nu$,
m_T	80379 ± 16	57/48
$p_T^{\hat{\ell}}$	80348 ± 18	58/62
p_T^{ν}	80406 ± 22	82/62

Angular coefficients in decay





Muon momentum calibration

Third step is to calibrate the momentum scale using J/ψ , Υ , and Z decays to muons

CDF: Calibration uses all three resonances and includes a measurement of the Z mass prior to combining

ATLAS: Calibration uses the Z resonance in bins of pseudorapidity and azimuthal angle

 $p_{\mathrm{T}}^{\mathrm{MC, corr}} = p_{\mathrm{T}}^{\mathrm{MC}} \times [1 + \alpha(\eta, \phi)] \\ \times \left[1 + \beta_{\mathrm{curv}}(\eta) \cdot G(0, 1) \cdot p_{\mathrm{T}}^{\mathrm{MC}}\right]$

LHCb: Calibration uses all three resonances

