



Lepton and Flavour Anomalies: Starting from the Top

Imperial College London, Particle Physics Seminar

Jacob Kempster

26/06/2024





Jacob Kempster

7 years postdoctoral experience

ATLAS Member for 13 years

Research Interests

- Experimental particle physicist
- ATLAS Experiment, Large Hadron Collider (LHC)
- [Top quark physics and Effective Field Theory](#)
- [Flavour physics anomalies](#)

Relevant Roles of Responsibility

- LHC Effective Field Theory Working Group Convener (ATLAS Top)
- ATLAS Top Group EFT Contact
- ATLAS HTop Combination Contact
- British Science Association Community Partner
- (Former) Top+X Working Group Convener
- (Former) Top UK Convener

Contact

- jacob.julian.kempster@cern.ch

This talk

Overview of studies other people have done



discussion of something I did



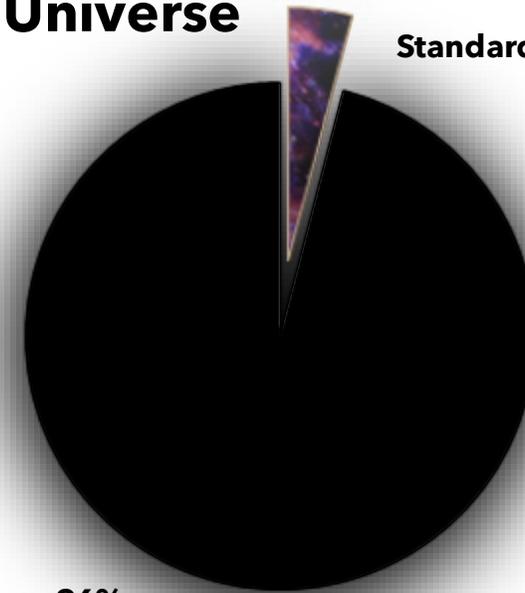
what I think we should do next

The Problem(s)

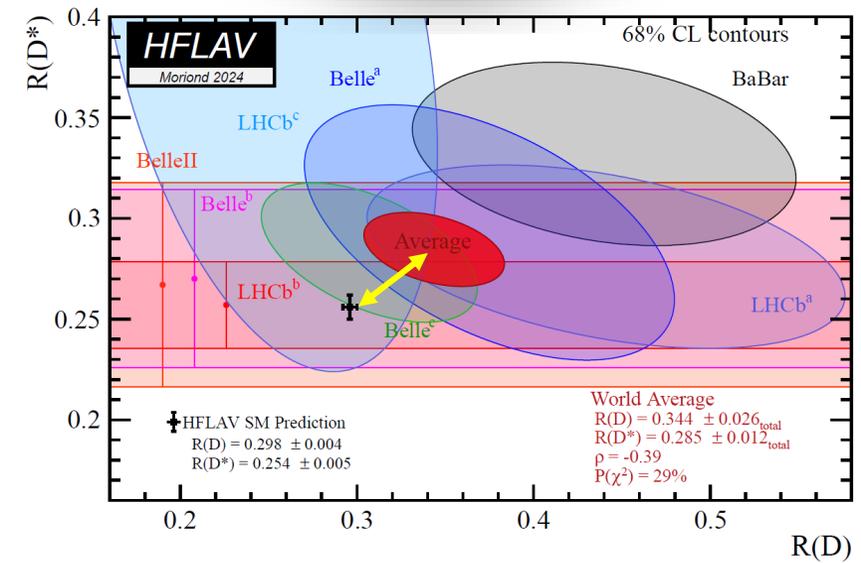
- New physics is elusive, but the Standard Model is incomplete!
- The next fundamental discovery may be outside of the direct energy reach of the Large Hadron Collider (LHC)
- We see hints of anomalous results in B -physics measurements, and now possibly beginning to appear in Top+X measurements

The Universe

Standard Model, 4%

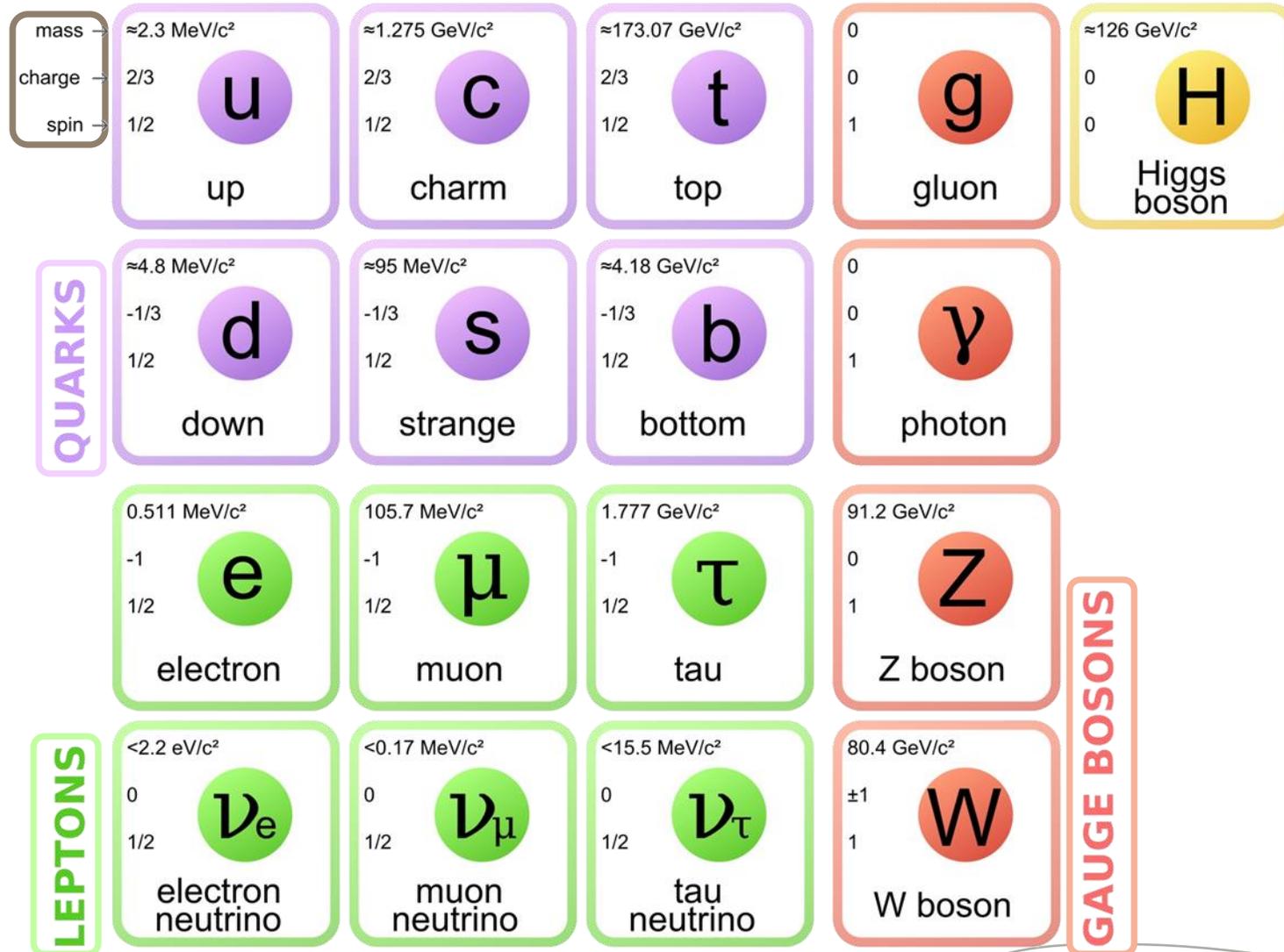


Unknown, 96%

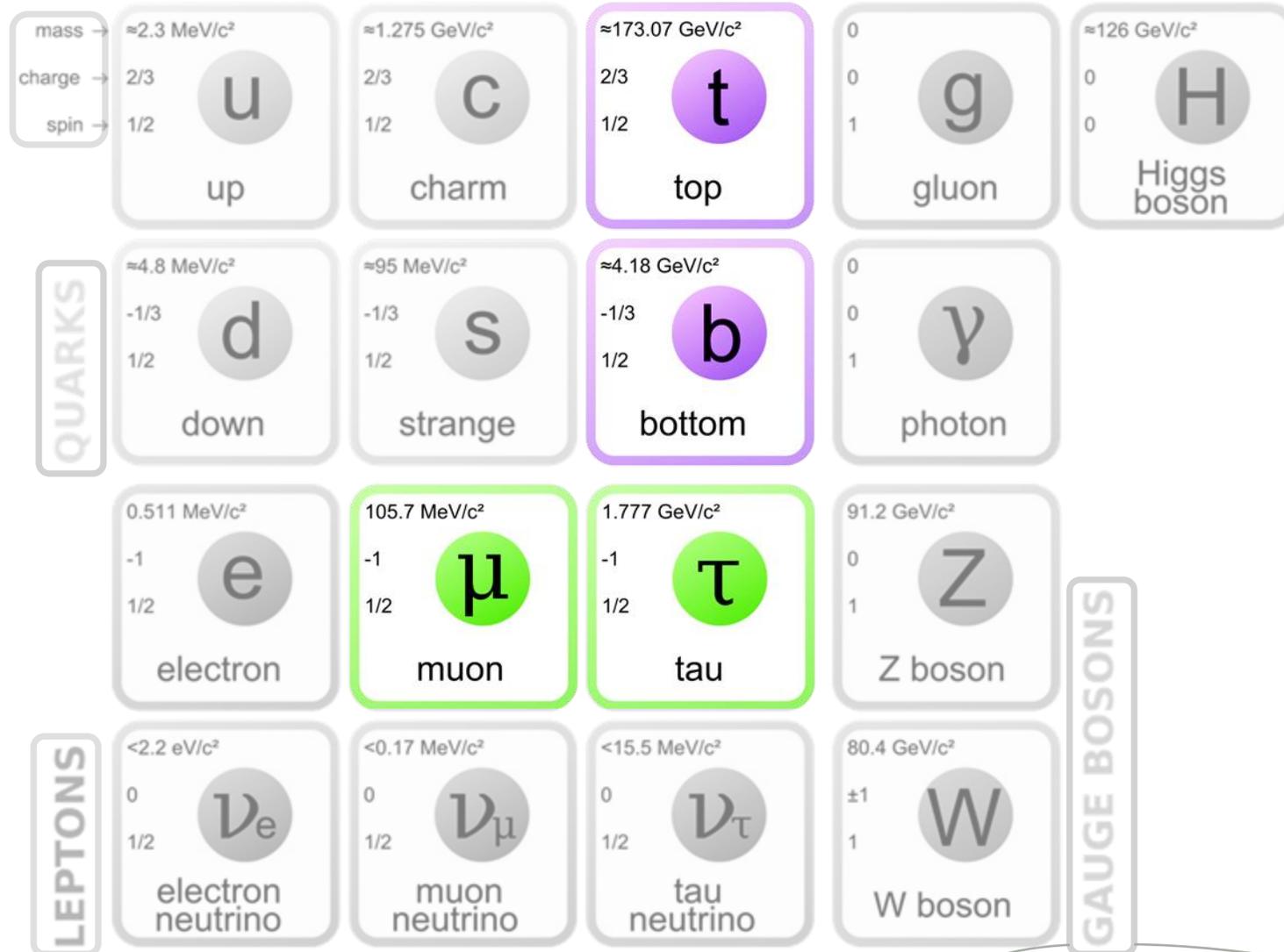


HFLAV

The Standard Model



The Standard Model



Muons behaving badly

D0 - Tevatron

Counting experiment - how many same-sign muon pairs?

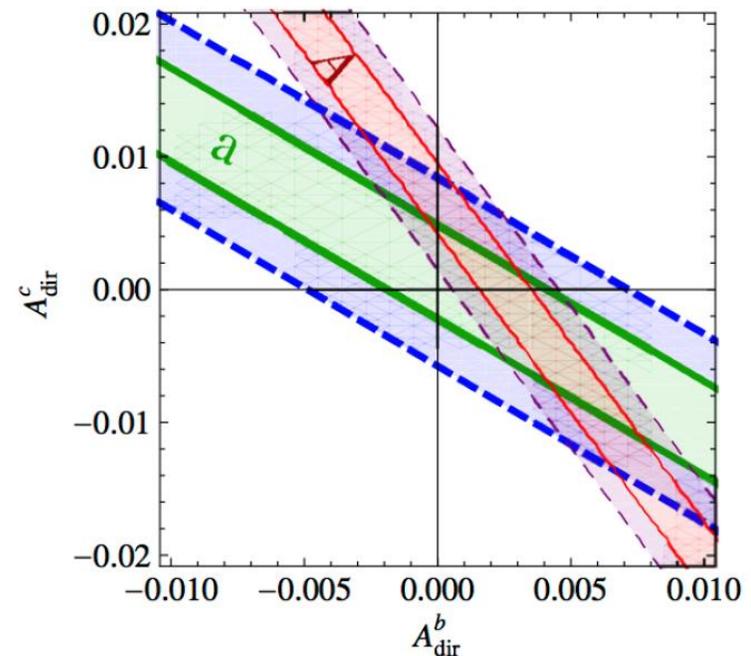
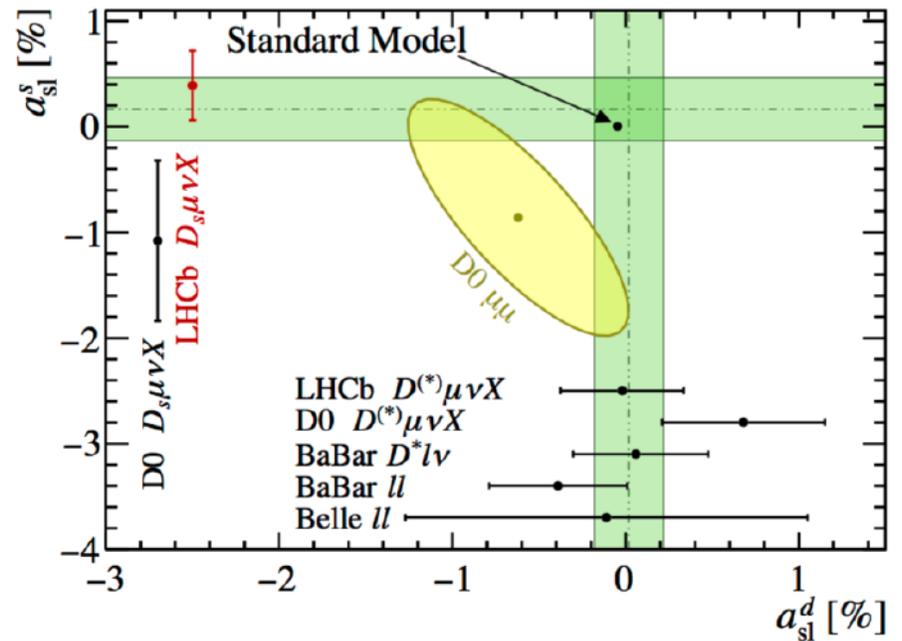
$$A = \frac{(N^{++} - N^{--})}{(N^{++} + N^{--})}$$

(2010-2013) Observed asymmetries up to **3.9σ** from SM expectation

- [PRD 105 \(2010\) 081801](#)
- [PRD 84 \(2011\) 052007](#)
- [PRD 87 \(2013\) 074020](#)

$$a_{sl}^q = \frac{\Gamma(\bar{B}_q^0 \rightarrow B_q^0 \rightarrow f) - \Gamma(B_q^0 \rightarrow \bar{B}_q^0 \rightarrow \bar{f})}{\Gamma(\bar{B}_q^0 \rightarrow B_q^0 \rightarrow f) + \Gamma(B_q^0 \rightarrow \bar{B}_q^0 \rightarrow \bar{f})},$$

$$a_{dir}^q = \frac{\Gamma(b \rightarrow \mu^- X) - \Gamma(\bar{b} \rightarrow \mu^+ X)}{\Gamma(b \rightarrow \mu^- X) + \Gamma(\bar{b} \rightarrow \mu^+ X)},$$



Muon g-2 - Fermilab

$$a_\mu = (g_\mu - 2)/2$$

g_μ = Muon gyromagnetic factor

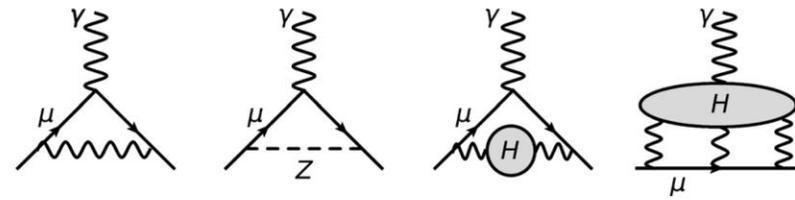
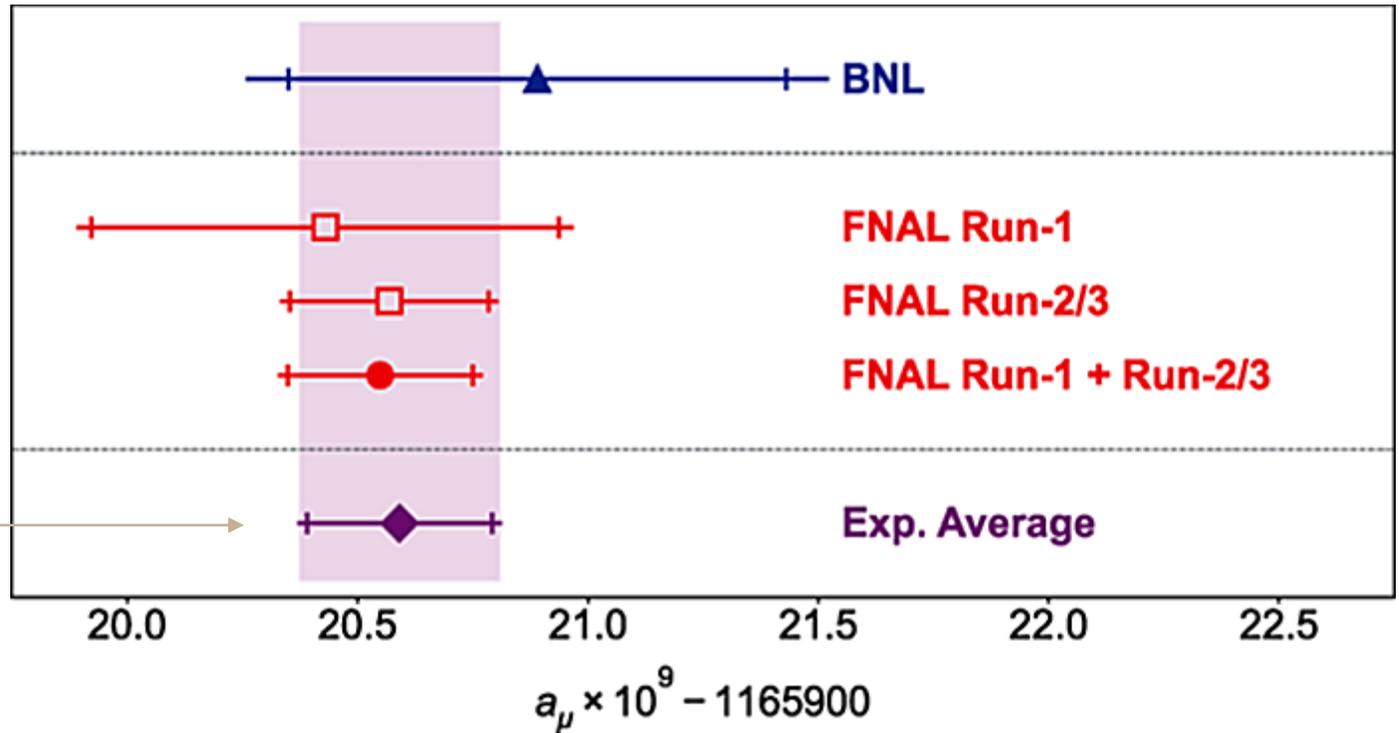


FIG. 1. Feynman diagrams of representative SM contributions to the muon anomaly. From left to right: first-order QED and weak processes, leading-order hadronic (H) vacuum polarization, and hadronic light-by-light contributions.

[PRL 131 \(2023\) 161802](#)

$$a_l^{SM} = a_l^{QED} + a_l^{EW} + a_l^{had}$$



SM Prediction

4.2 σ

[EPJC 80 \(2020\) 241](#)

Muon g-2 - Fermilab

$$a_\mu = (g_\mu - 2)/2$$

g_μ = Muon gyromagnetic factor

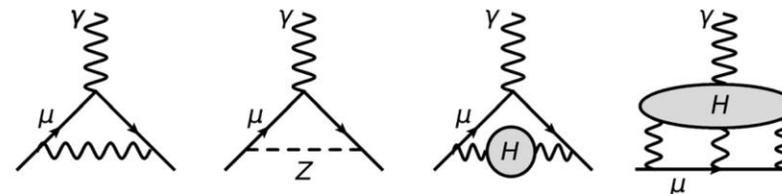
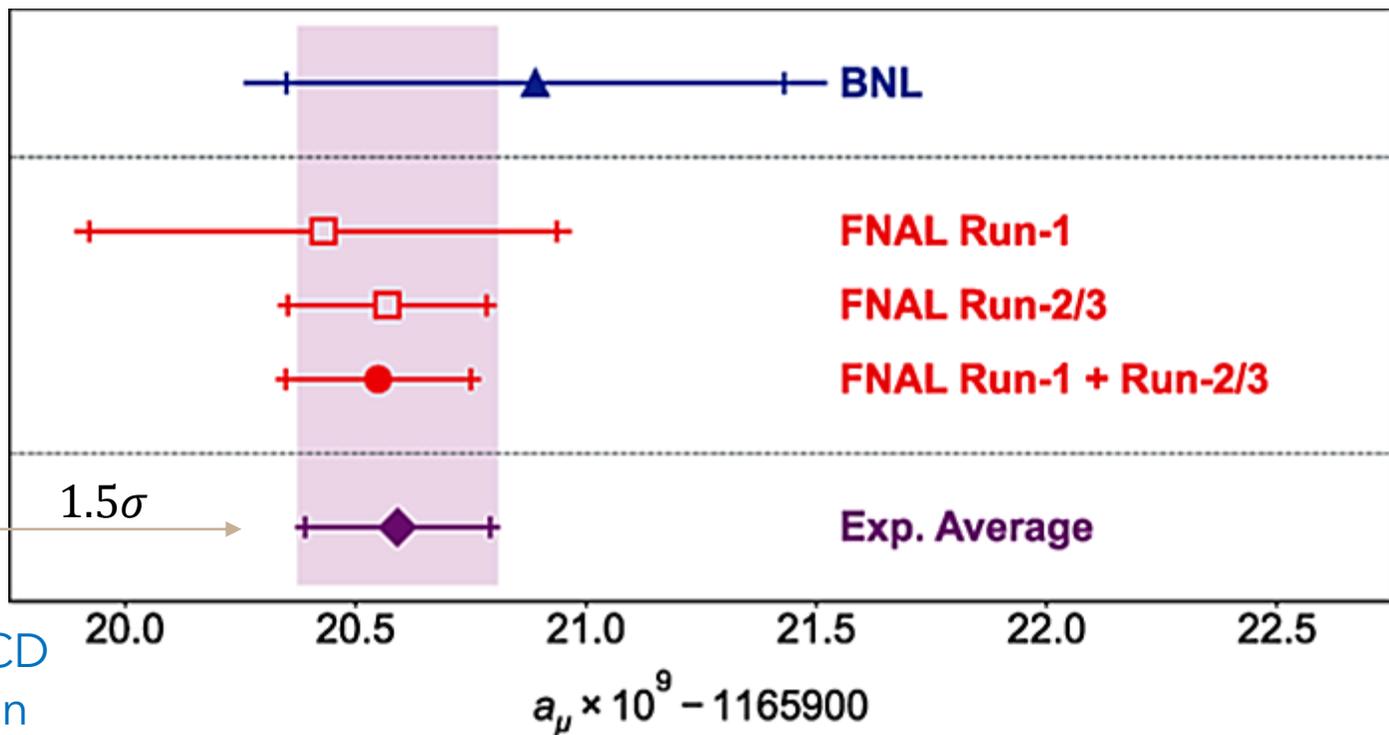


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[PRL 131 \(2023\) 161802](#)

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SM Prediction

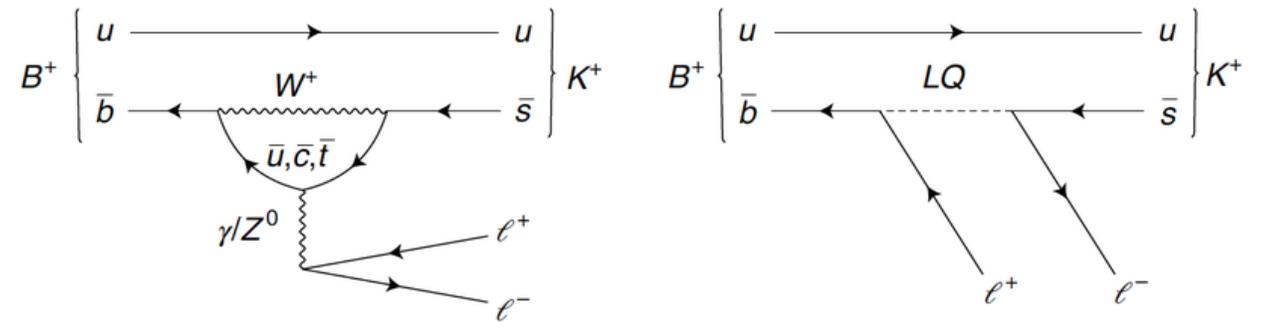
Lattice QCD Prediction

[EPJC 80 \(2020\) 241](#)

R(K^(*)) B → sμ⁺μ⁻

$$R_K = \frac{\text{BR}(B \rightarrow K\mu^+\mu^-)}{\text{BR}(B \rightarrow Ke^+e^-)},$$

$$R_{K^*} = \frac{\text{BR}(B \rightarrow K^*\mu^+\mu^-)}{\text{BR}(B \rightarrow K^*e^+e^-)}.$$

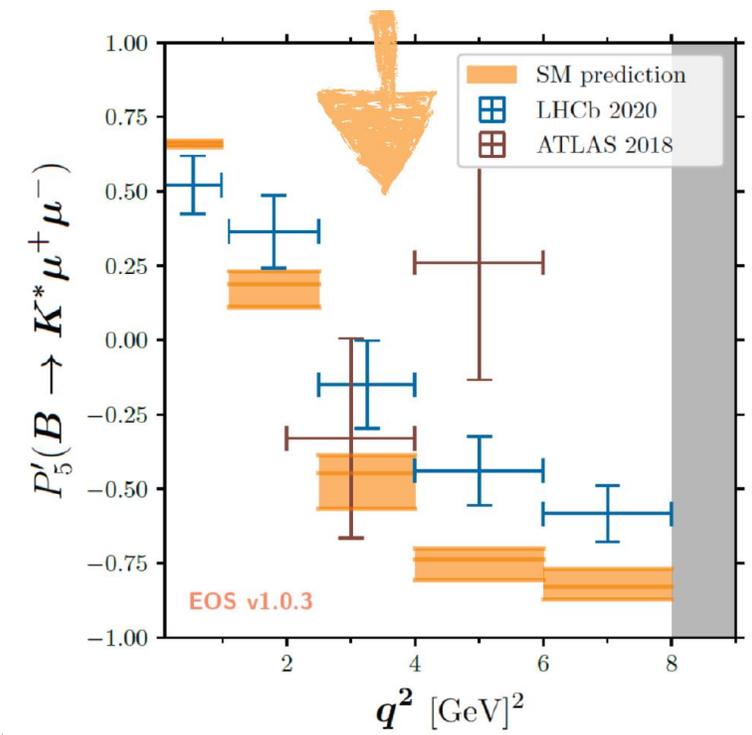
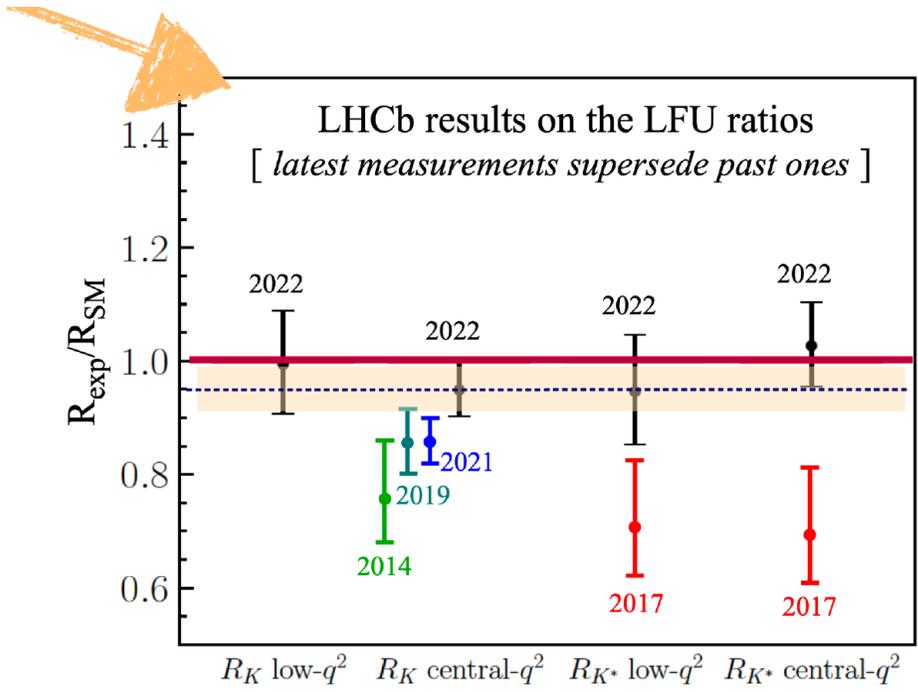


At one point this was up to 3.1σ away from the SM

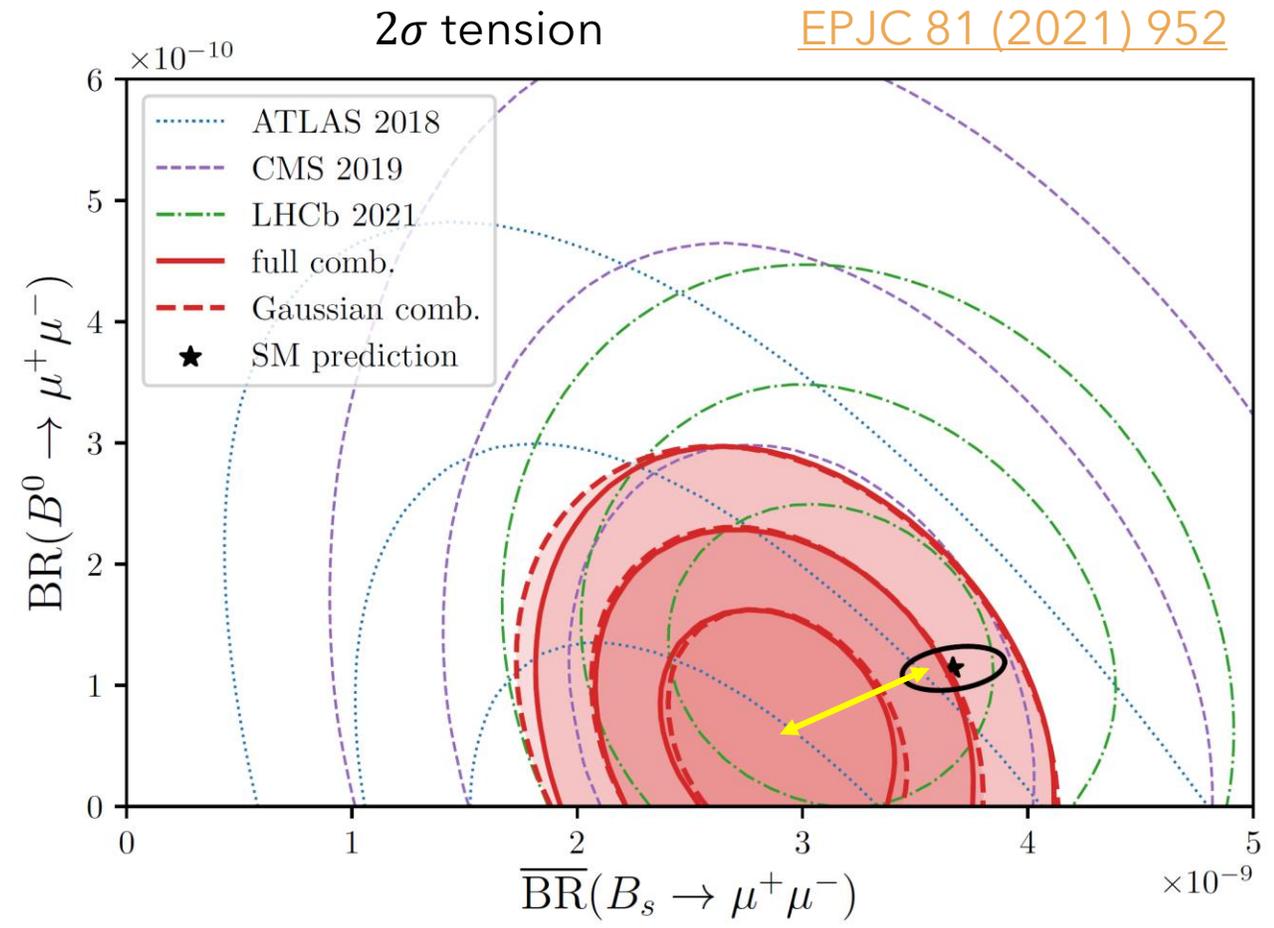
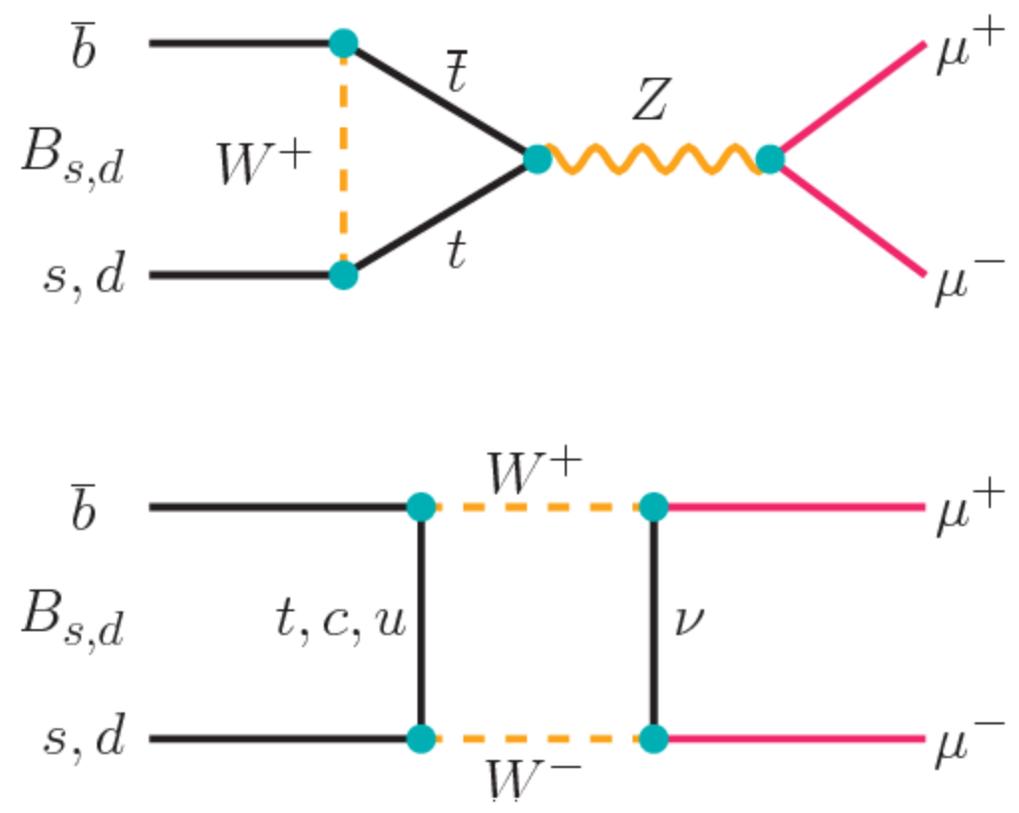
Now found to be in good agreement

[PRD 108 \(2023\) 032002](#)

(However, some angular discrepancies remain!)



$B_s \rightarrow \mu^+ \mu^-$

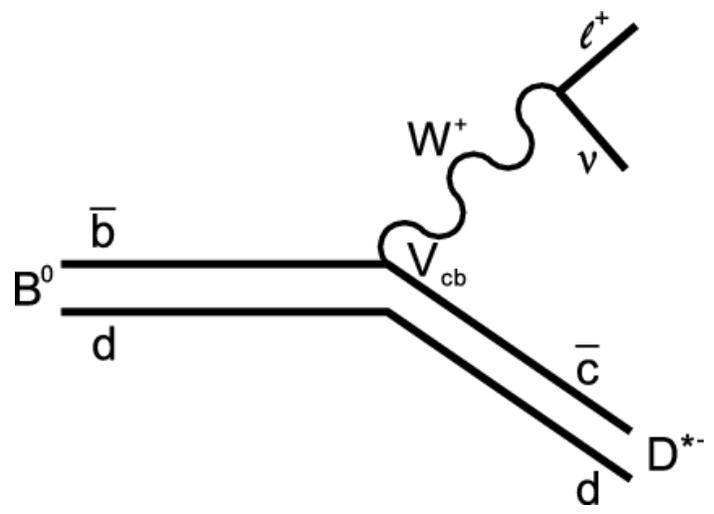


Taus behaving badly too?

R(D^(*))

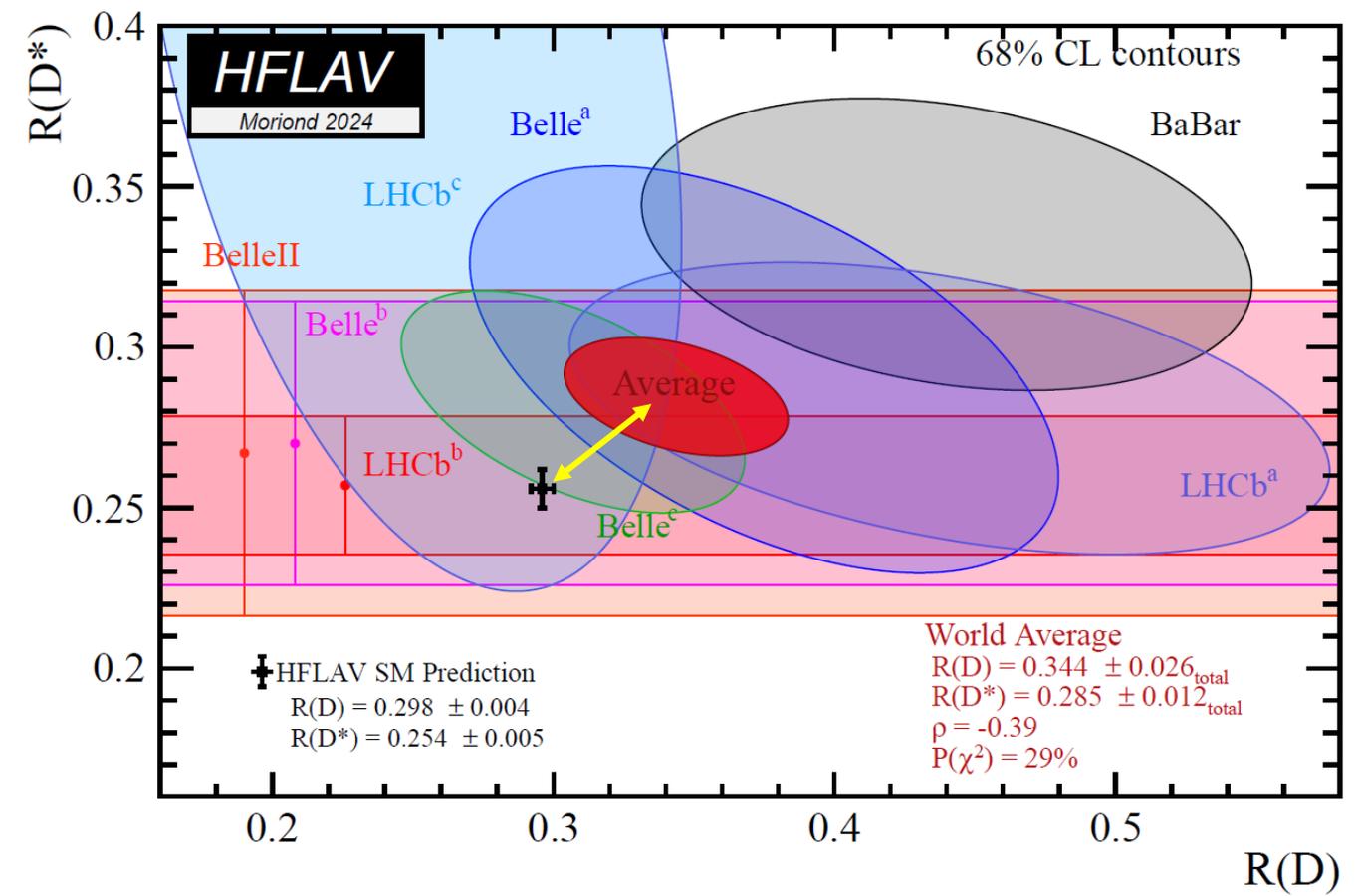
LHCb-PAPER-2024-007 (in preparation)

$$R(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} l^- \bar{\nu}_l)}$$



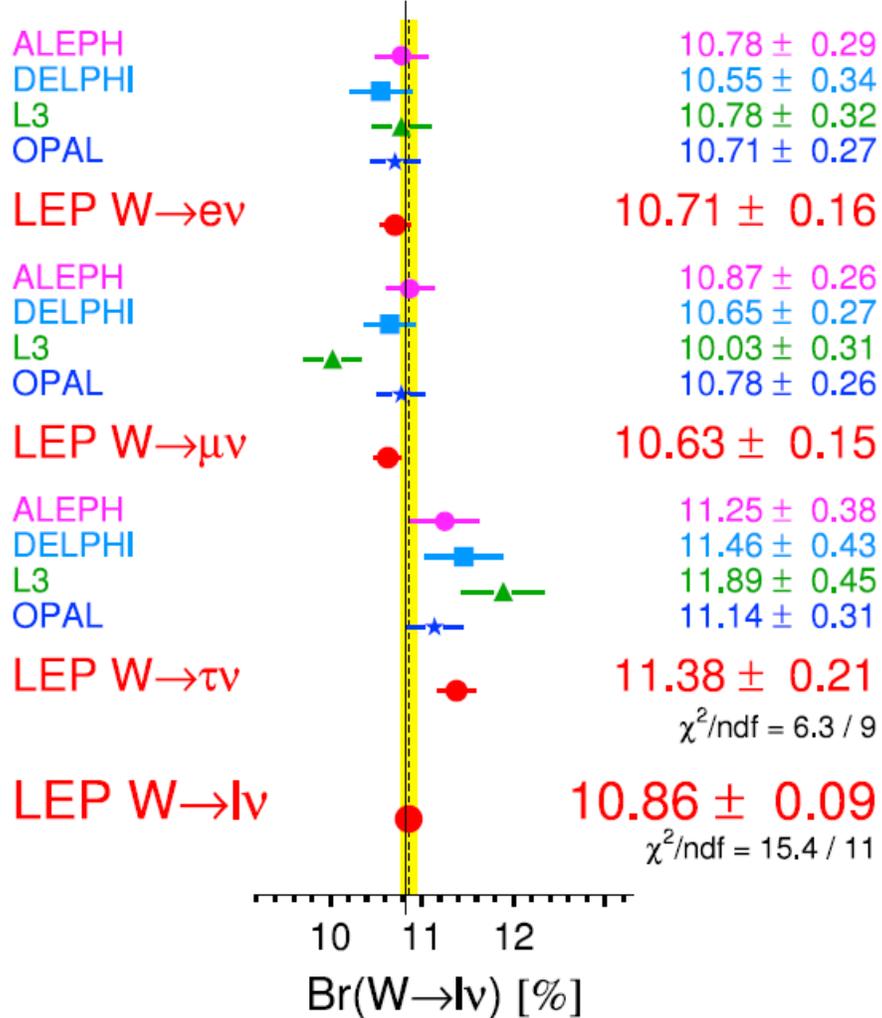
3.17σ tension

HFLAV (Moriond 2024)



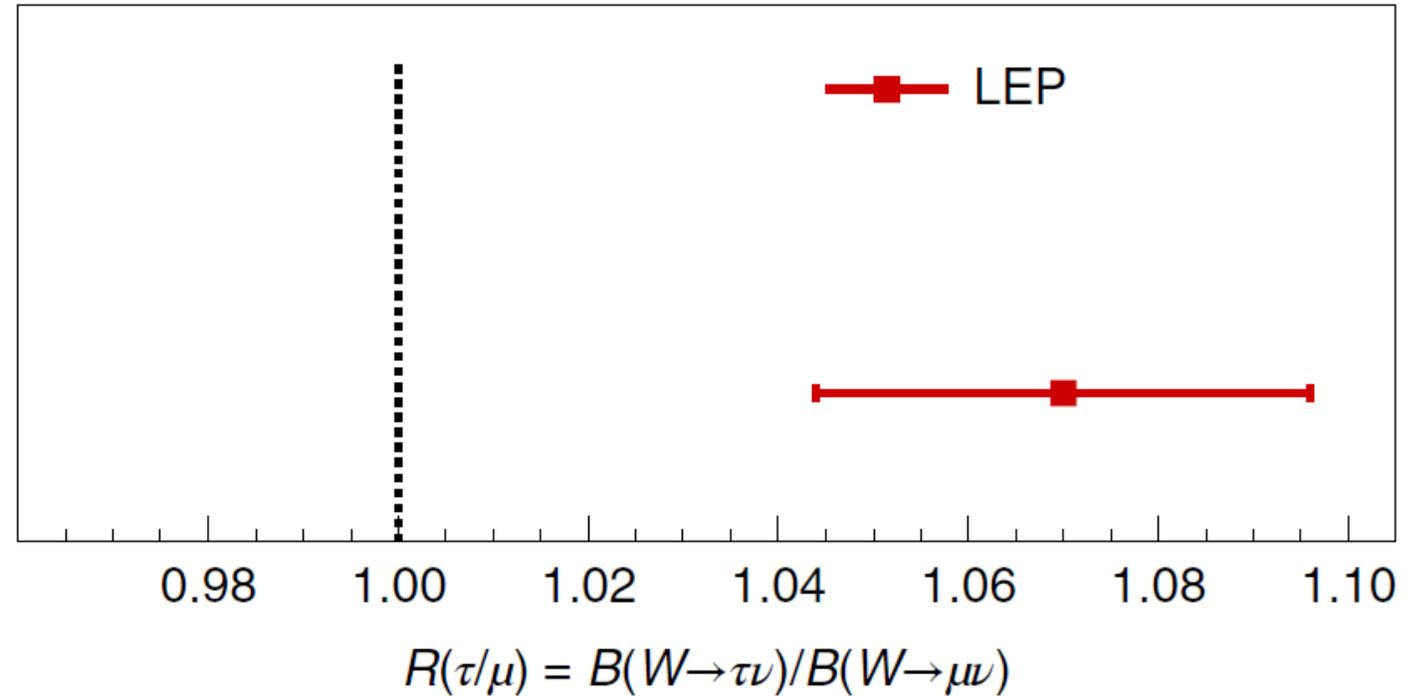
LEP (CERN) Lepton Flavour Universality

W Leptonic Branching Ratios

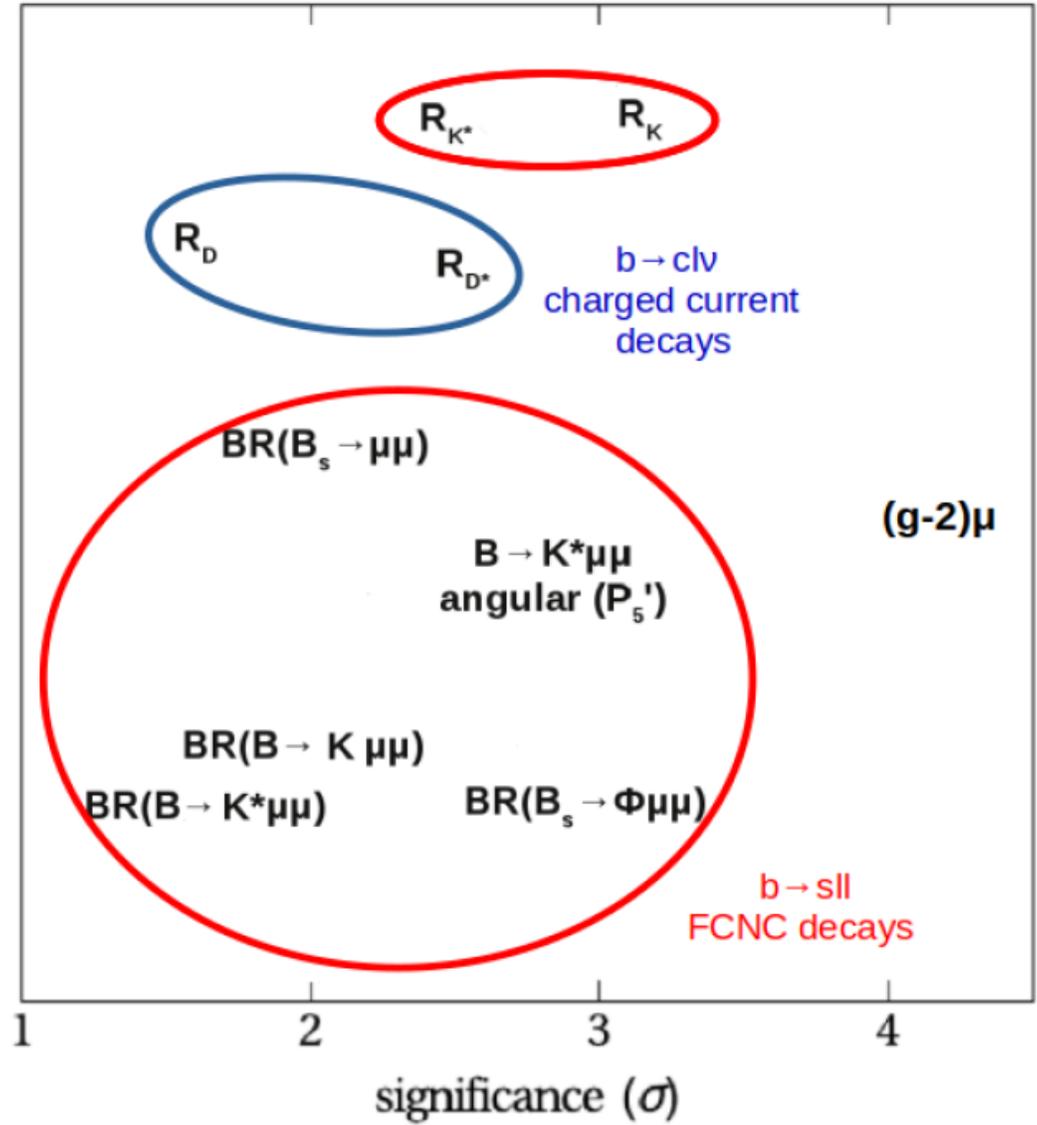


2.6 σ tension

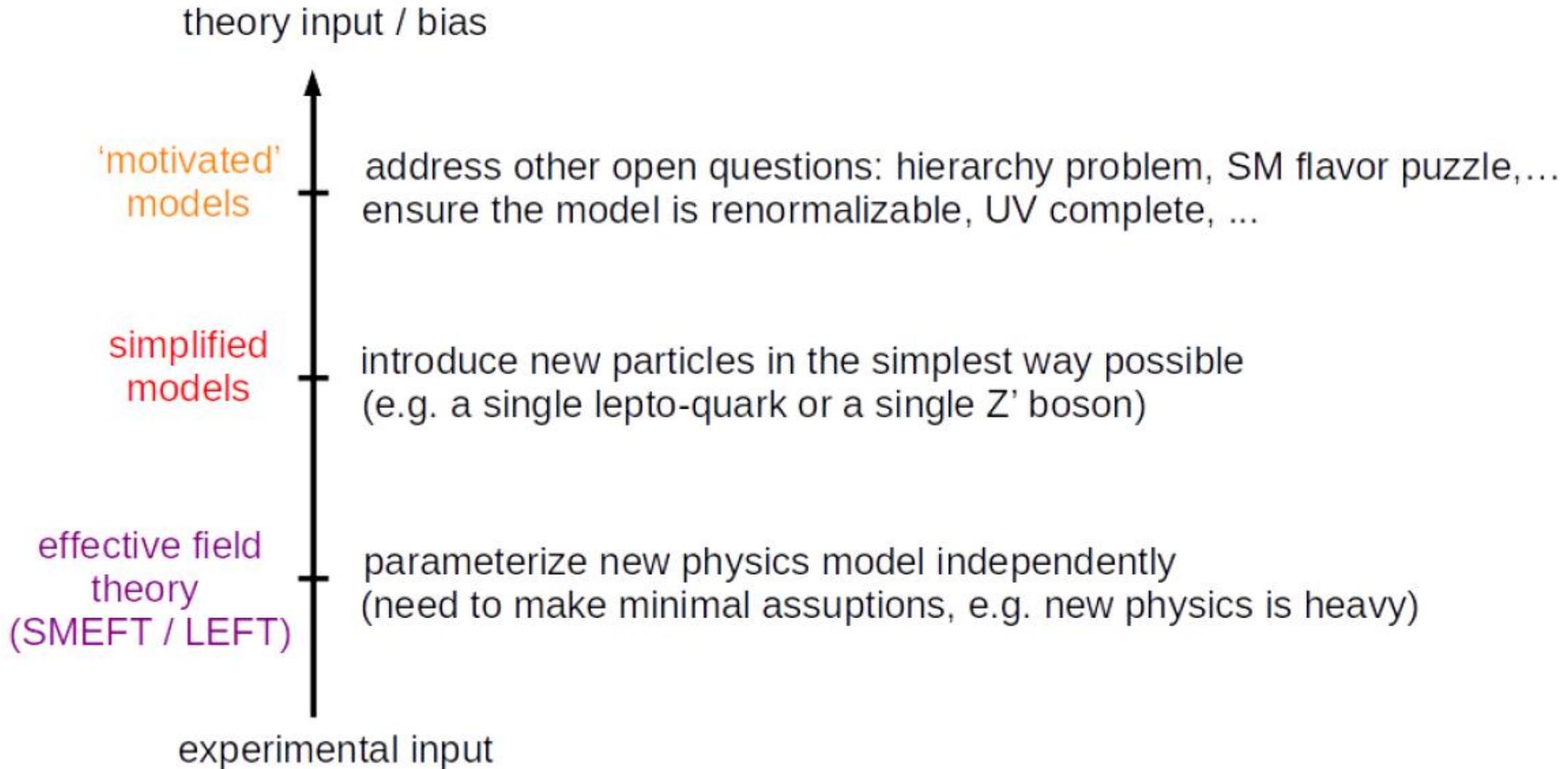
[J Phys Rep 532 \(2013\) 004](#)



(This is prompt lepton behaviour - i.e. unlikely to be same anomalous physics, but still interesting!)

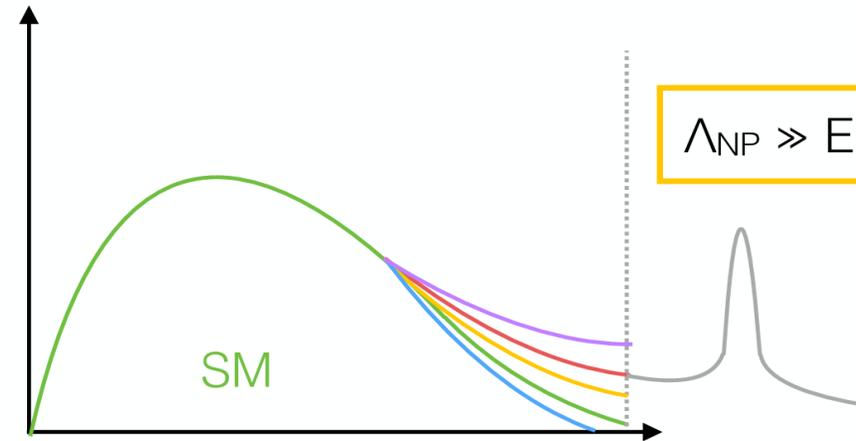


Effective Field Theory



Effective Field Theory (EFT)

Maybe New Physics (NP) exists at a significantly higher energy scale (Λ_{NP}) than LHC can reach...



[K. Mimasu, EFTforTop](#)

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{i,n} \frac{c_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)}$$

Standard
Model

Coupling
Strength

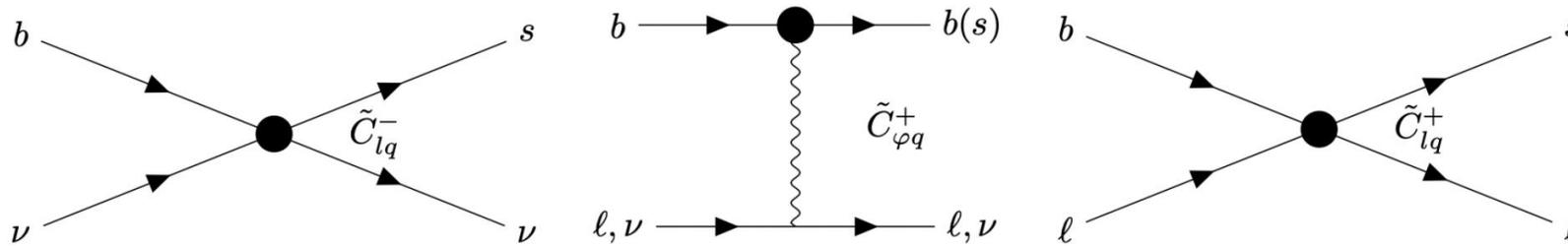
Operators introducing
new interactions



EFT and the B-anomalies

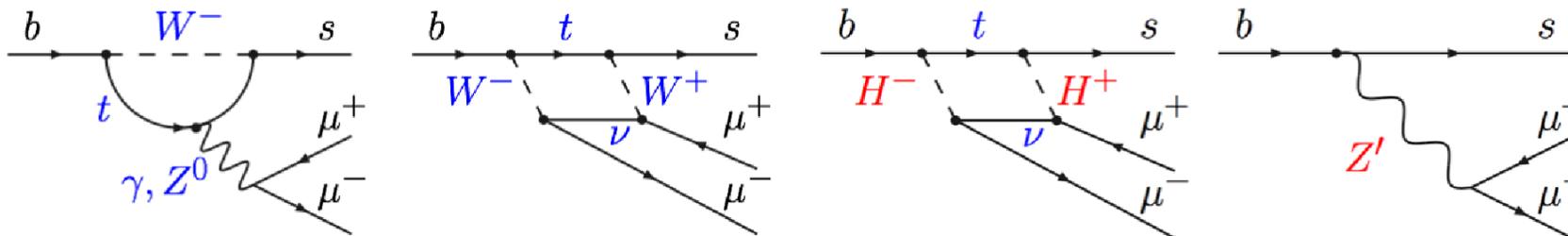
[JHEP 06 \(2021\) 010](#)

$$\bar{s}_L \gamma_\mu b_L \bar{\mu}_L \gamma^\mu \mu_L \quad \longrightarrow \quad \begin{aligned} O_{lq}^{(1)} &= \bar{Q} \gamma_\mu Q \bar{L} \gamma^\mu L, \\ O_{lq}^{(3)} &= \bar{Q} \gamma_\mu \tau^I Q \bar{L} \gamma^\mu \tau^I L \end{aligned}$$



$b \rightarrow sll$ transitions

- Flavour Changing Neutral Current (FCNC) $b \rightarrow s(d)l^+l^-$ decays, such as $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, are forbidden at tree level in the SM

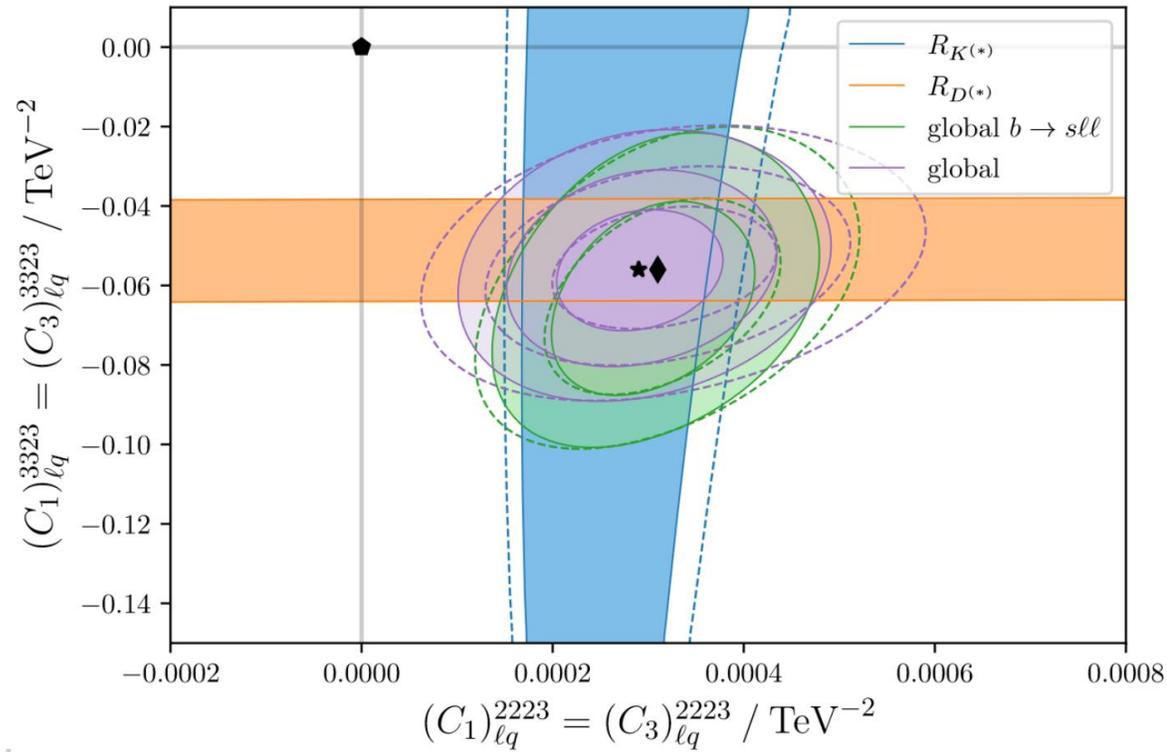


[P. Cartelle](#)



EFT and the B-anomalies

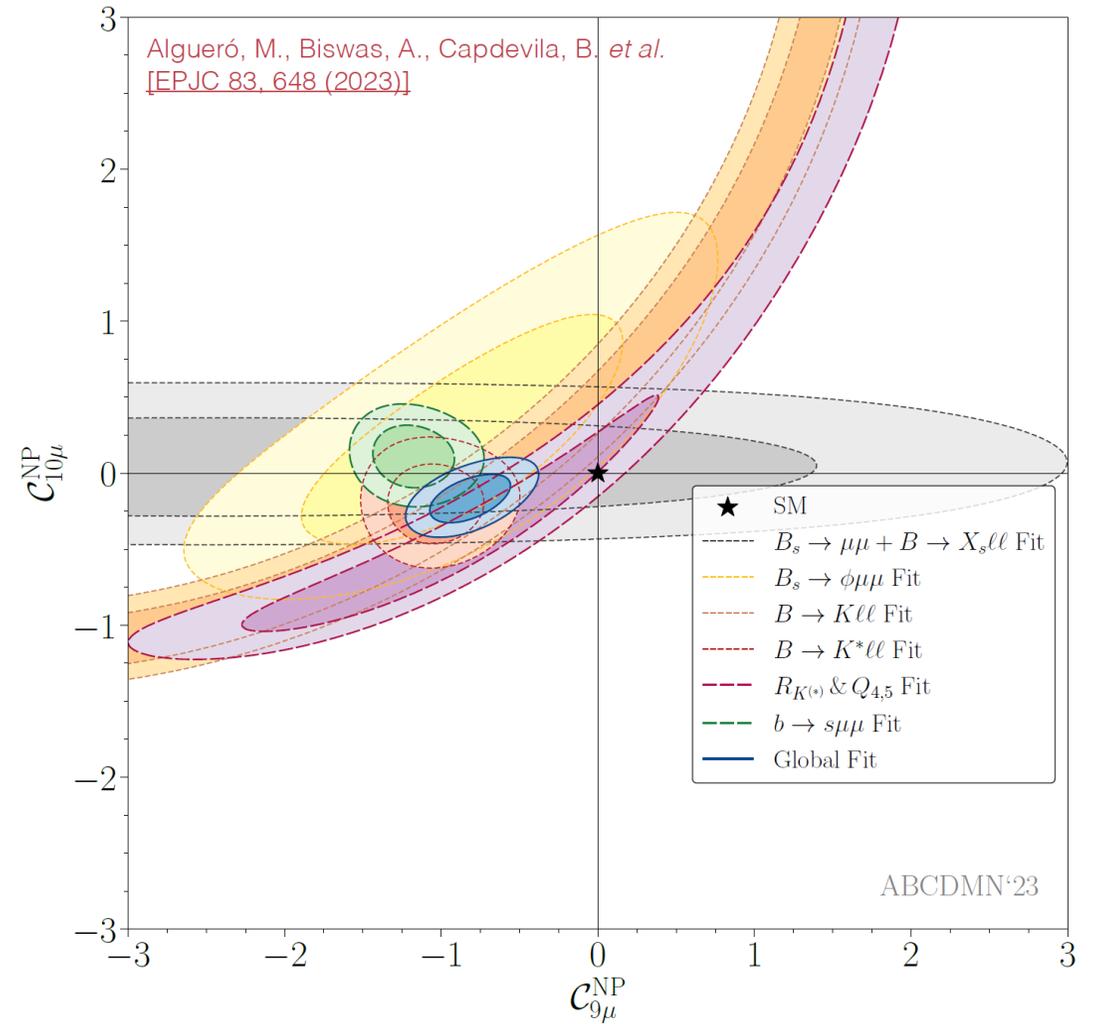
arXiv:2104.00015



◆ SM prediction

★ Best fit 2021 R_K (LHCb arXiv:2103.11769, 3.1σ)

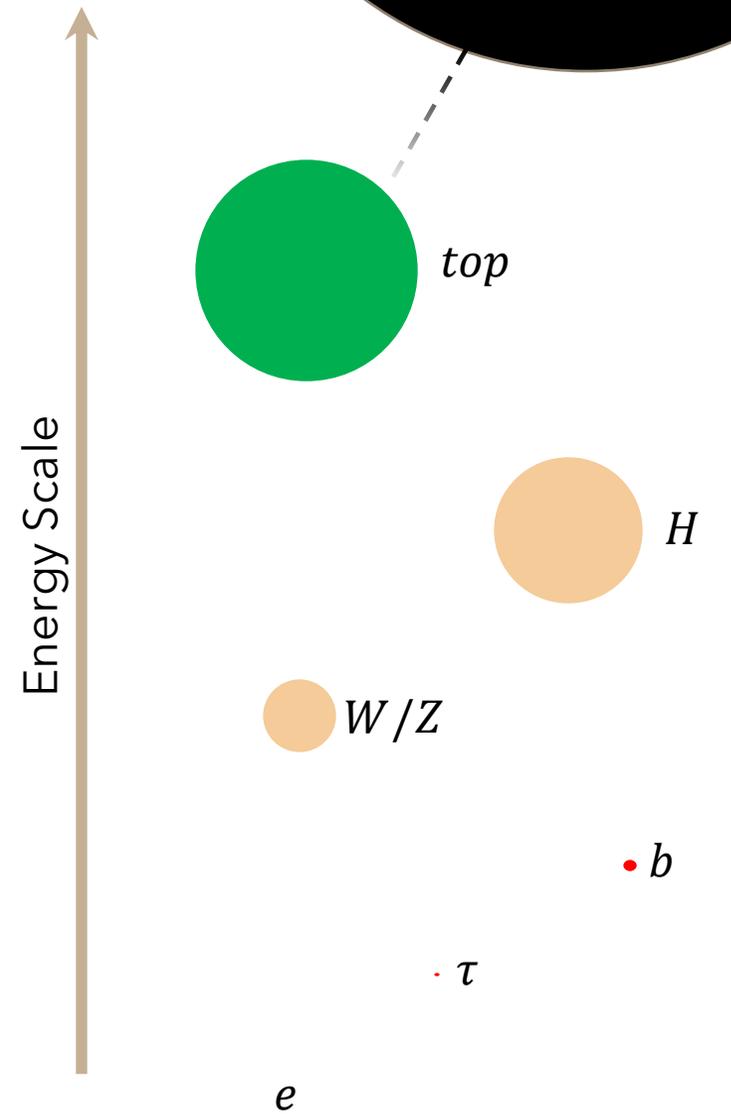
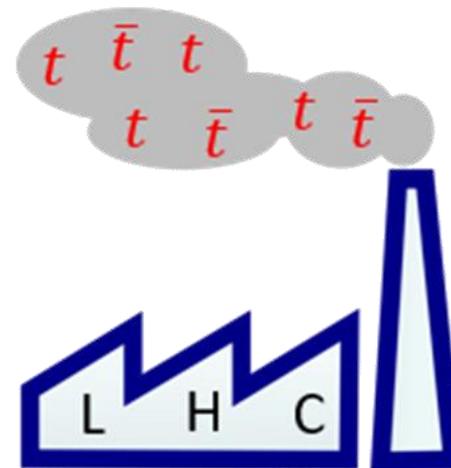
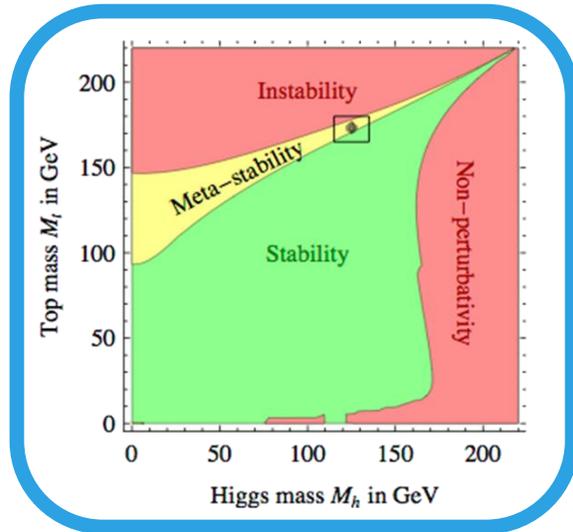
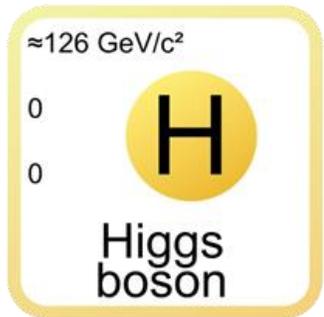
◆ Best fit pre-2021 R_K



Why Top quarks?

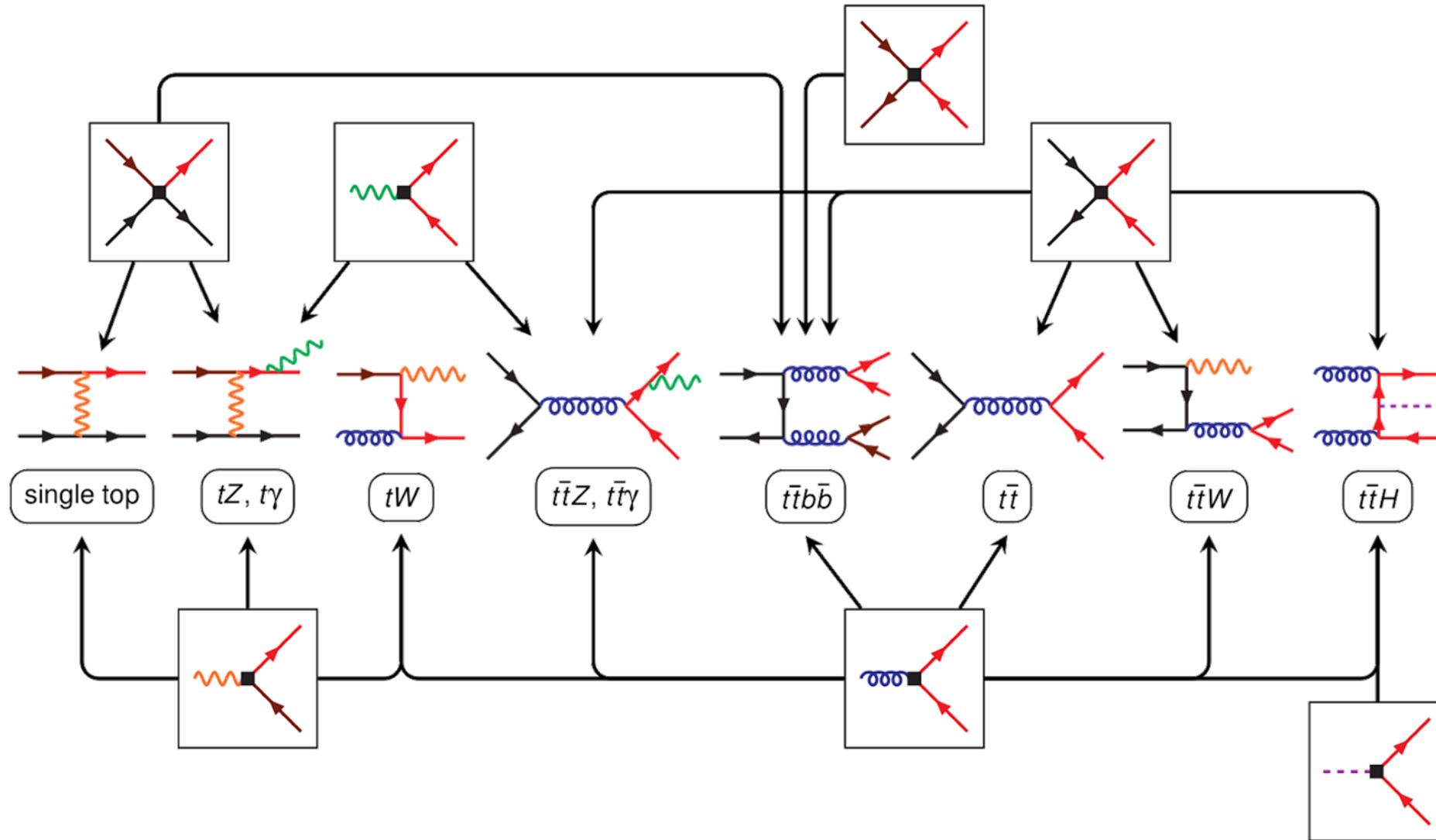
Top Methodology

- Use the top quark - it is the most massive particle and the closest to the scale of new physics - it's vulnerable!
- Very short lifetime (does not hadronise) - opportunity to study a 'bare' quark
- Very selective about decay channels $BR(t \rightarrow Wb) \sim 100\%$



Top EFT

[arXiv:1008.4484](https://arxiv.org/abs/1008.4484)

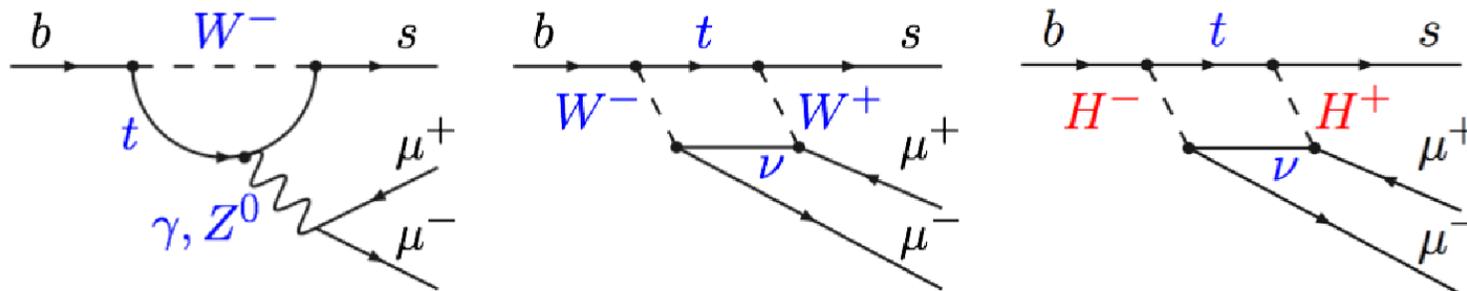
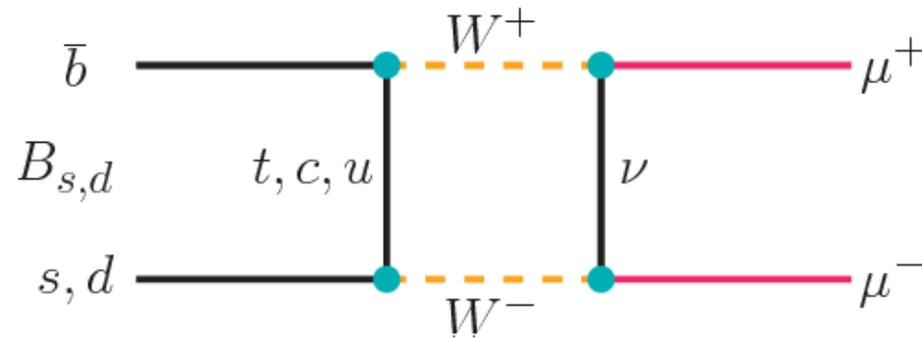
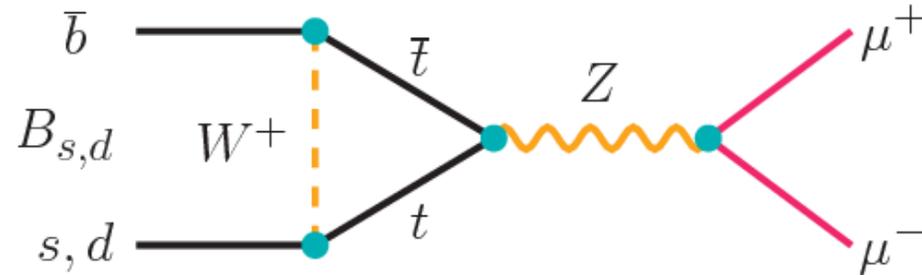


parameter	$t\bar{t}$	single t	tW	tZ	t decay	$t\bar{t}Z$	$t\bar{t}W$
$C_{Qq}^{1,8}$	Λ^{-2}	-	-	-	-	Λ^{-2}	Λ^{-2}
$C_{Qq}^{3,8}$	Λ^{-2}	$\Lambda^{-4} [\Lambda^{-2}]$	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$	Λ^{-2}	Λ^{-2}
C_{tu}^8, C_{td}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	-
$C_{Qq}^{1,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{Qq}^{3,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	Λ^{-2}	-	Λ^{-2}	Λ^{-2}	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
C_{tu}^1, C_{td}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	-
C_{Qu}^8, C_{Qd}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	-
C_{tq}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	Λ^{-2}
C_{Qu}^1, C_{Qd}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	-
C_{tq}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{\phi Q}^-$	-	-	-	Λ^{-2}	-	Λ^{-2}	-
$C_{\phi Q}^3$	-	Λ^{-2}	Λ^{-2}	Λ^{-2}	Λ^{-2}	Λ^{-2}	-
$C_{\phi t}$	-	-	-	Λ^{-2}	-	Λ^{-2}	-
$C_{\phi tb}$	-	Λ^{-4}	Λ^{-4}	Λ^{-4}	Λ^{-4}	-	-
C_{tZ}	-	-	-	Λ^{-2}	-	Λ^{-2}	-
C_{tW}	-	Λ^{-2}	Λ^{-2}	Λ^{-2}	Λ^{-2}	-	-
C_{bW}	-	Λ^{-4}	Λ^{-4}	Λ^{-4}	Λ^{-4}	-	-
C_{tG}	Λ^{-2}	$[\Lambda^{-2}]$	Λ^{-2}	-	$[\Lambda^{-2}]$	Λ^{-2}	Λ^{-2}

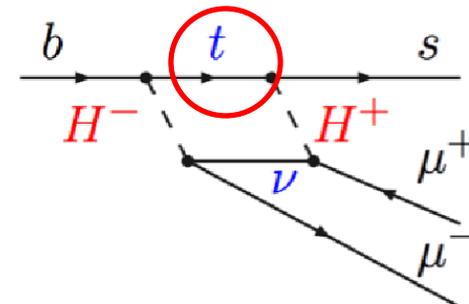
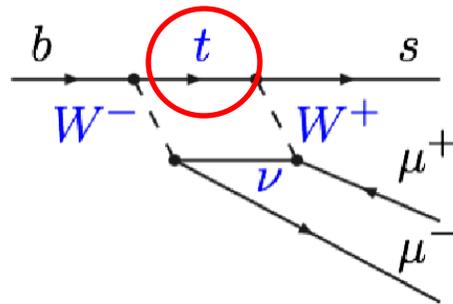
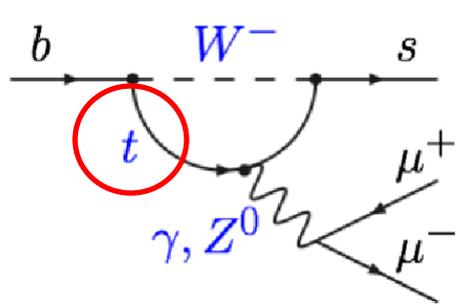
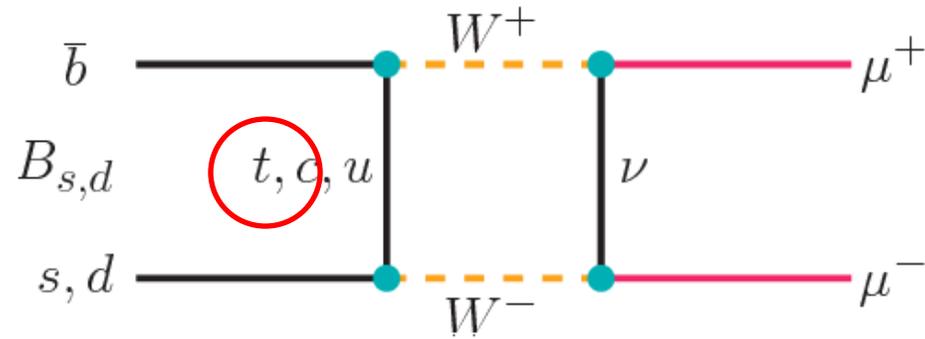
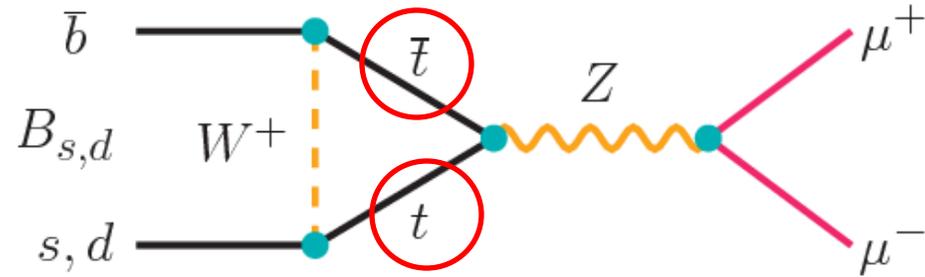
Example contributions of Wilson coefficients to top-quark observables via SM-interference (Λ^{-2}) and via dimension-6 squared terms only (Λ^{-4})



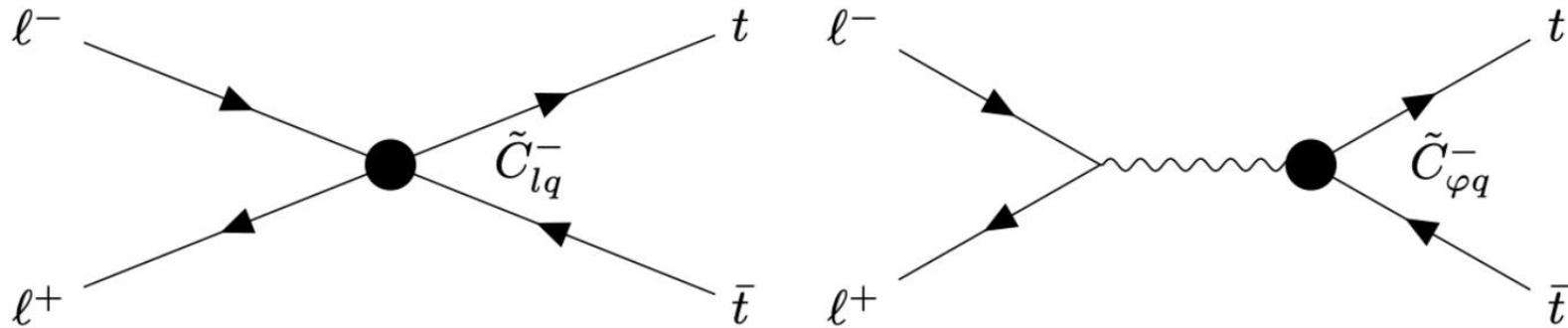
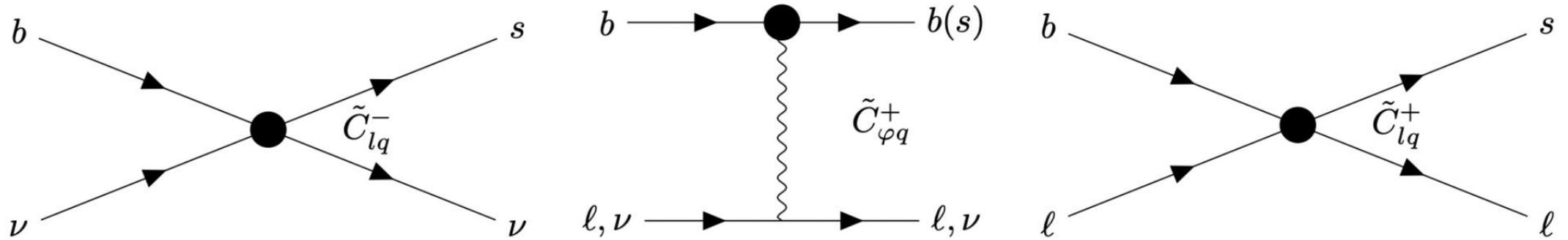
Top EFT and the B-anomalies



Top EFT and the B-anomalies



Top EFT and the B-anomalies



Four-fermion operators

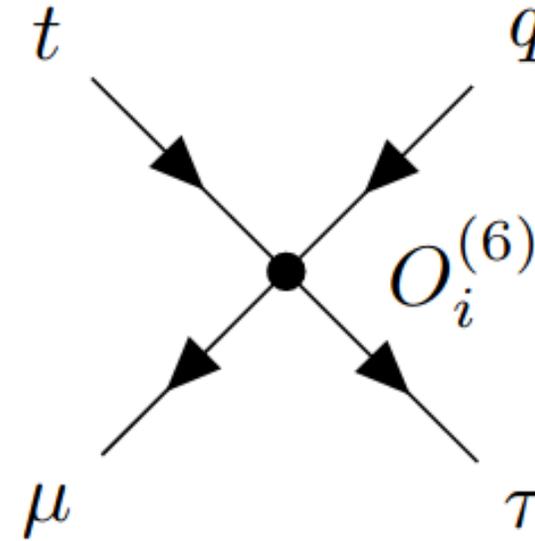
Four-fermion / 2-quark-2-lepton (2Q2L) operator ‘family’ in context

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	Q_{qqq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	Q_{dqu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				



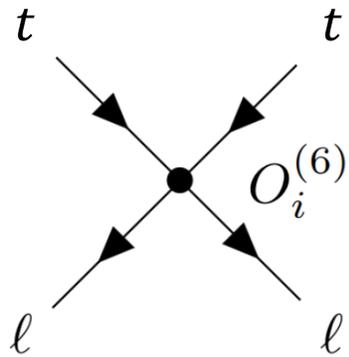
2Q2L EFT operators

Operator	Interaction	Lorentz Structure
$O_{lq}^{1(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lq}^{3(ijkl)}$	$(\bar{l}_i \gamma^\mu \sigma^I l_j)(\bar{q}_k \gamma_\mu \sigma_I q_l)$	Vector
$O_{eq}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lu}^{(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$O_{eu}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$O_{lequ}^{1(ijkl)}$	$(\bar{l}_i e_j) \varepsilon (\bar{q}_k u_l)$	Scalar
$O_{lequ}^{3(ijkl)}$	$(\bar{l}_i \sigma^{\mu\nu} e_j) \varepsilon (\bar{q}_k \sigma_{\mu\nu} u_l)$	Tensor



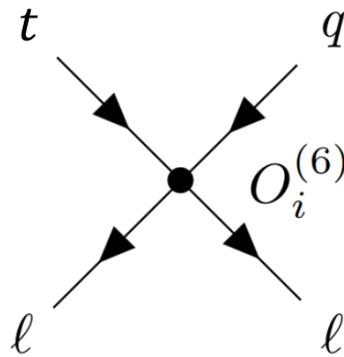
Top 2Q2L operator effects

$t\bar{t}Z$ -like (diagonal)



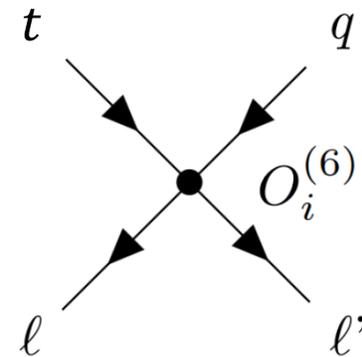
$t\bar{t}ll$

FCNC (semi-diagonal)

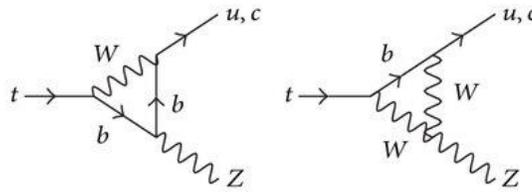
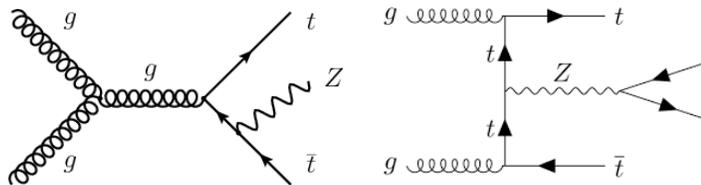


$tqll$

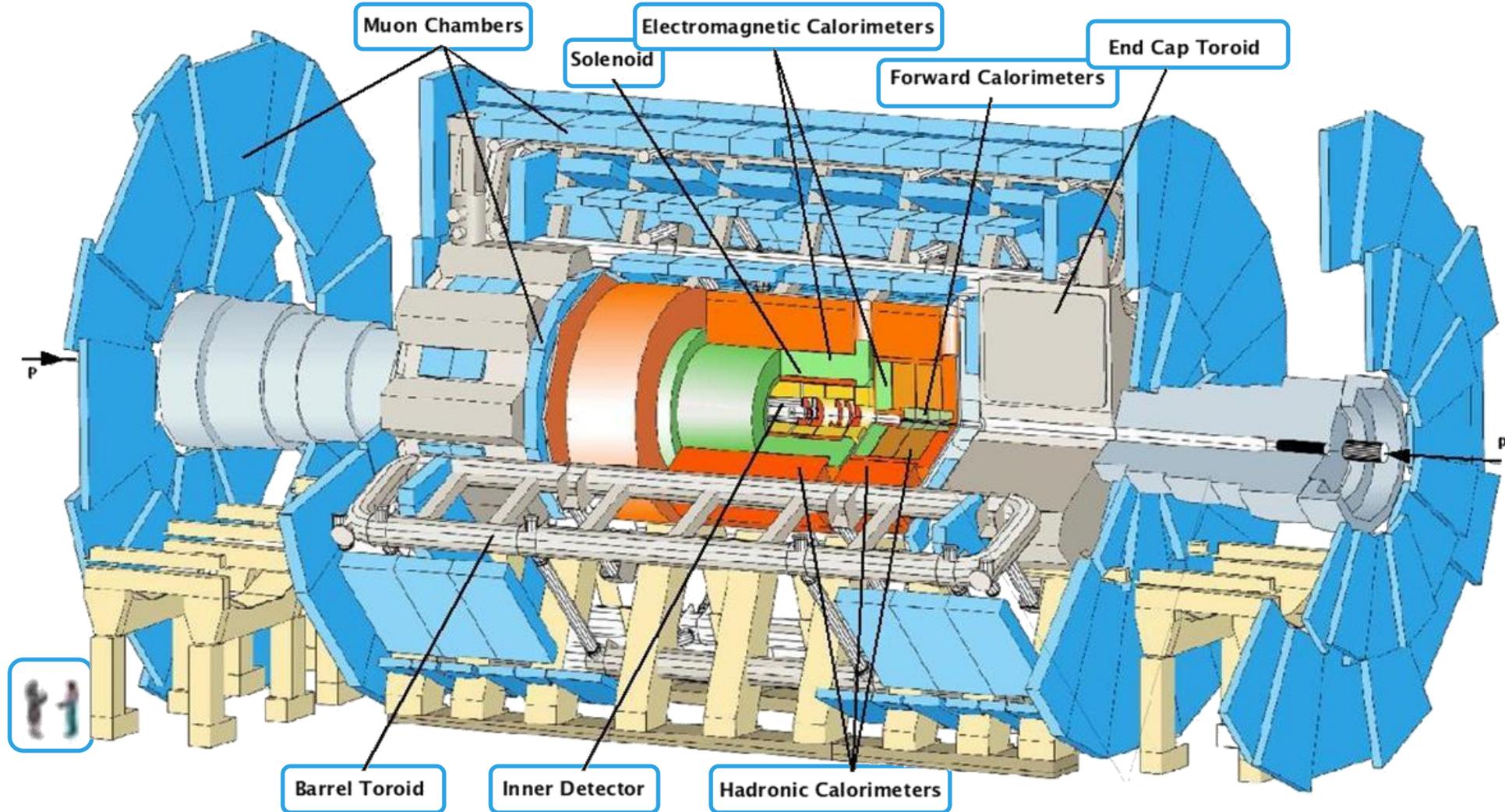
CLFV (fully off-diagonal)

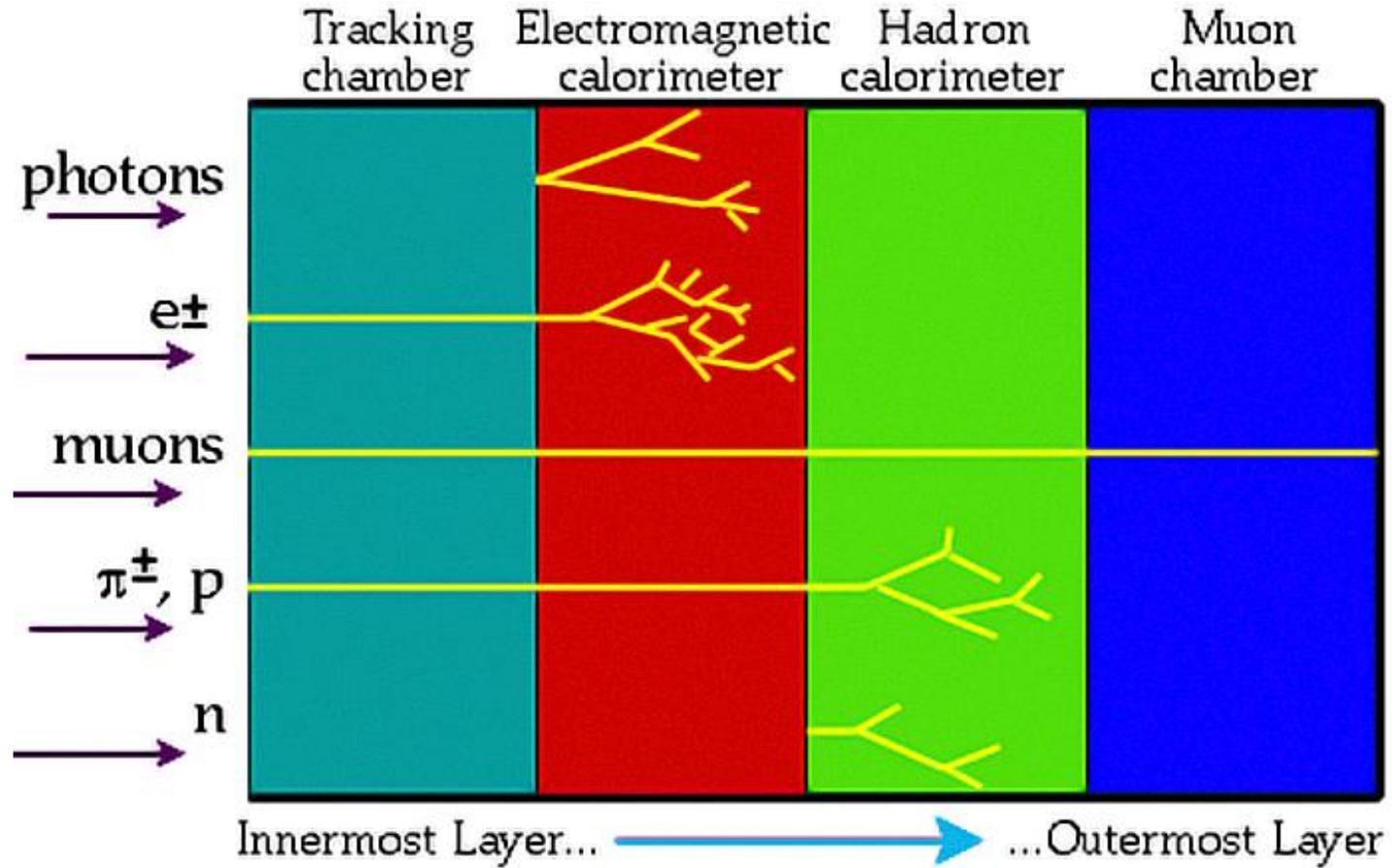


$tqll'$



ATLAS and Top





Analyses

- B-physics CP violation with Soft Muon Tagging [JHEP 02 \(2017\) 071](#)
- Lepton Flavour Universality in Top decays [Nat. Phys. 17 \(2021\) 813-818](#)
- Top FCNC $t \rightarrow qH(\rightarrow \tau\tau)$ [JHEP 06 \(2023\) 155](#)
- Top CLFV $\mu\tau qt$ (Accepted by PRD) [arXiv:2403.06742](#)

What's in the future?

B-physics CP violation with Soft Muon Tagging

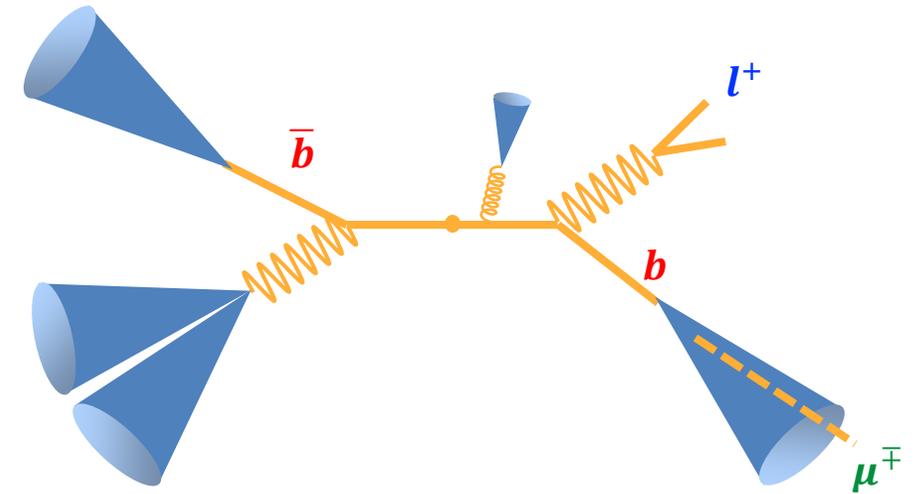
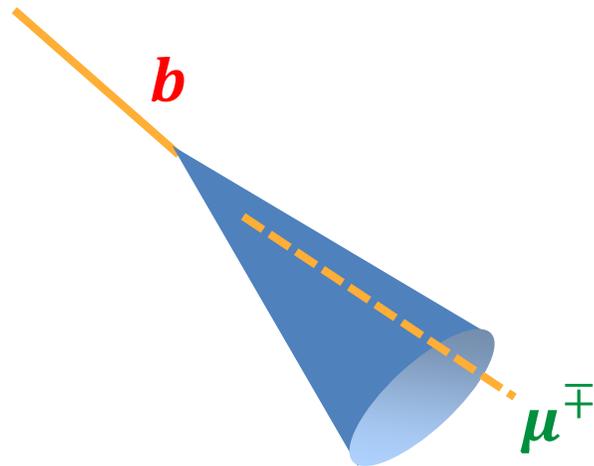
(vs D0 dimuon asymmetry)

Unlike $gg \rightarrow b\bar{b}$, we know which b we are dealing with!

The charge of the W , tagged with a lepton, tells you the charge of the associated b -quark at **production**

$$l^+ \Rightarrow b$$

$$l^- \Rightarrow \bar{b}$$

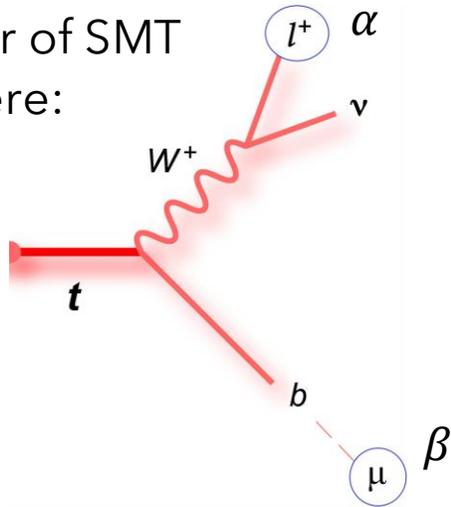


$$\text{BR}(b \rightarrow (\dots) \rightarrow \mu) \sim 20\%$$

The charge of the soft muon, tells you the charge of the associated b -quark at **decay**

Charge asymmetries

Consider number of SMT
muons, $N^{\alpha\beta}$, where:



$$A^{ss} = \frac{P(b \rightarrow l^+) - P(\bar{b} \rightarrow l^-)}{P(b \rightarrow l^+) + P(\bar{b} \rightarrow l^-)} = \frac{\left(\frac{N^{++}}{N^+}\right) - \left(\frac{N^{--}}{N^-}\right)}{\left(\frac{N^{++}}{N^+}\right) + \left(\frac{N^{--}}{N^-}\right)}$$

$$A^{os} = \frac{P(b \rightarrow l^-) - P(\bar{b} \rightarrow l^+)}{P(b \rightarrow l^-) + P(\bar{b} \rightarrow l^+)} = \frac{\left(\frac{N^{+-}}{N^+}\right) - \left(\frac{N^{-+}}{N^-}\right)}{\left(\frac{N^{+-}}{N^+}\right) + \left(\frac{N^{-+}}{N^-}\right)}$$

CP asymmetries

- CP asymmetries can be extracted from A^{SS}, A^{OS}
- As defined in **PRL 110,232002 (2013)**:

$$A^{SS} = r_b A_{\text{mix}}^{bl} + r_{c\bar{c}} A_{\text{mix}}^{bc} + r_c A_{\text{dir}}^{bc} - (r_c + r_{c\bar{c}}) A_{\text{dir}}^{cl}$$

$$A^{OS} = \tilde{r}_c A_{\text{mix}}^{bc} + \tilde{r}_b A_{\text{dir}}^{bl} + (\tilde{r}_c + \tilde{r}_{c\bar{c}}) A_{\text{dir}}^{cl}$$

$$A_{\text{mix}}^{bl} = \frac{\Gamma(b \rightarrow \bar{b} \rightarrow l^+ X) - \Gamma(\bar{b} \rightarrow b \rightarrow l^- X)}{\Gamma(b \rightarrow \bar{b} \rightarrow l^+ X) + \Gamma(\bar{b} \rightarrow b \rightarrow l^- X)} \xleftrightarrow{A_{\text{mix}}^b} A_{\text{mix}}^{bc} = \frac{\Gamma(b \rightarrow \bar{b} \rightarrow \bar{c} X) - \Gamma(\bar{b} \rightarrow b \rightarrow c X)}{\Gamma(b \rightarrow \bar{b} \rightarrow c X) + \Gamma(\bar{b} \rightarrow b \rightarrow c X)}$$

$$A_{\text{dir}}^{bl} = \frac{\Gamma(b \rightarrow l^- X) - \Gamma(\bar{b} \rightarrow l^+ X)}{\Gamma(b \rightarrow l^- X) + \Gamma(\bar{b} \rightarrow l^+ X)}$$

$$A_{\text{dir}}^{cl} = \frac{\Gamma(\bar{c} \rightarrow l^- X_L) - \Gamma(c \rightarrow l^+ X_L)}{\Gamma(\bar{c} \rightarrow l^- X_L) + \Gamma(c \rightarrow l^+ X_L)}$$

$$A_{\text{dir}}^{bc} = \frac{\Gamma(b \rightarrow c X_L) - \Gamma(\bar{b} \rightarrow \bar{c} X_L)}{\Gamma(b \rightarrow c X_L) + \Gamma(\bar{b} \rightarrow \bar{c} X_L)}$$

Results	Data (10^{-2})	Existing limits (2σ) (10^{-2})	SM (10^{-2})
A^{SS}	-0.7 ± 0.8	—	$< 10^{-2}$ [1]
A^{oS}	0.4 ± 0.5	—	$< 10^{-2}$ [1]
A_{mix}^b	-2.5 ± 2.8	< 0.1 [3]	$< 10^{-3}$ [2,3]
A_{dir}^{bl}	0.5 ± 0.5	< 1.2 [4]	$< 10^{-5}$ [1]
A_{dir}^{cl}	1.0 ± 1.0	< 6.0 [4]	$< 10^{-9}$ [1]
A_{dir}^{bc}	-1.0 ± 1.1	—	$< 10^{-7}$ [5]

At 2σ the constraints made by this analysis are stronger than the existing limit on A_{dir}^{cl}

This the first direct experimental constraint on A_{dir}^{bc} .

[1] PRL 110, 232002 (2013) [2] arXiv:1511.09466v1 [3] arXiv:1412.7515v1 (HFAG) [4] PRD 87, 074036 (2015) [5] PLB 694, 374 (2011)

Lepton Flavour Universality with Tops

(vs LEP LFU)

Lepton Flavour Universality

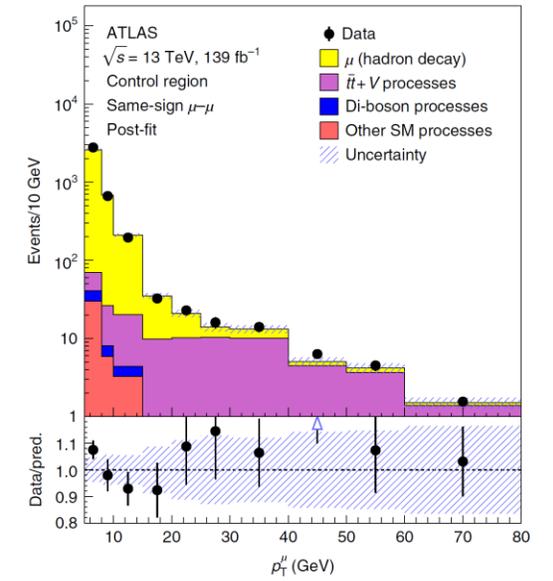
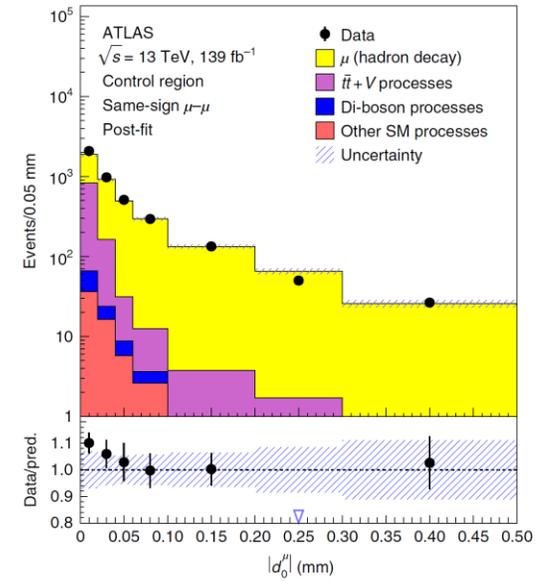
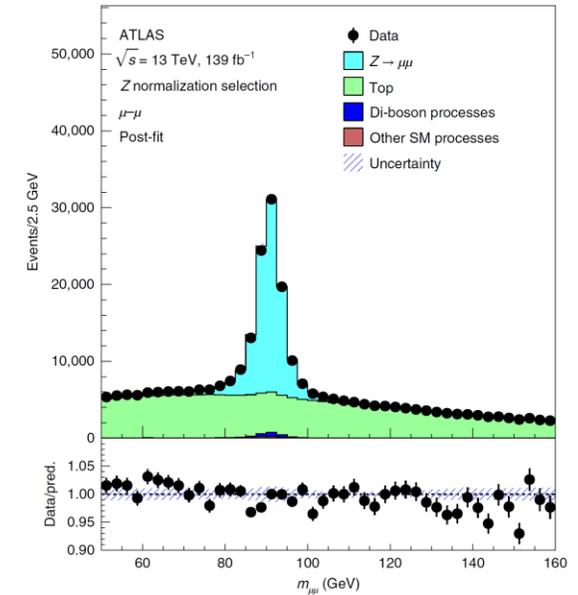
$$R(\tau/\mu) = \frac{\mathcal{B}(t \rightarrow bW(\rightarrow \tau\nu))}{\mathcal{B}(t \rightarrow bW(\rightarrow \mu\nu))}$$

Opposite-sign dimuon events

- Big backgrounds from $Z \rightarrow \mu\mu$

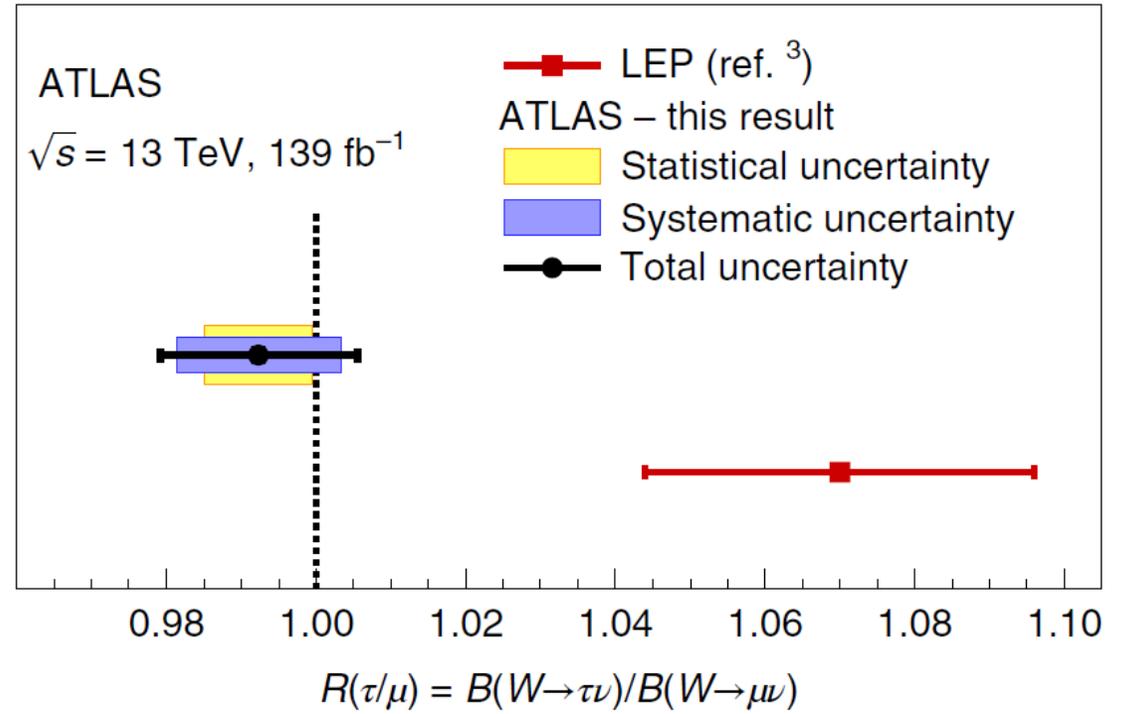
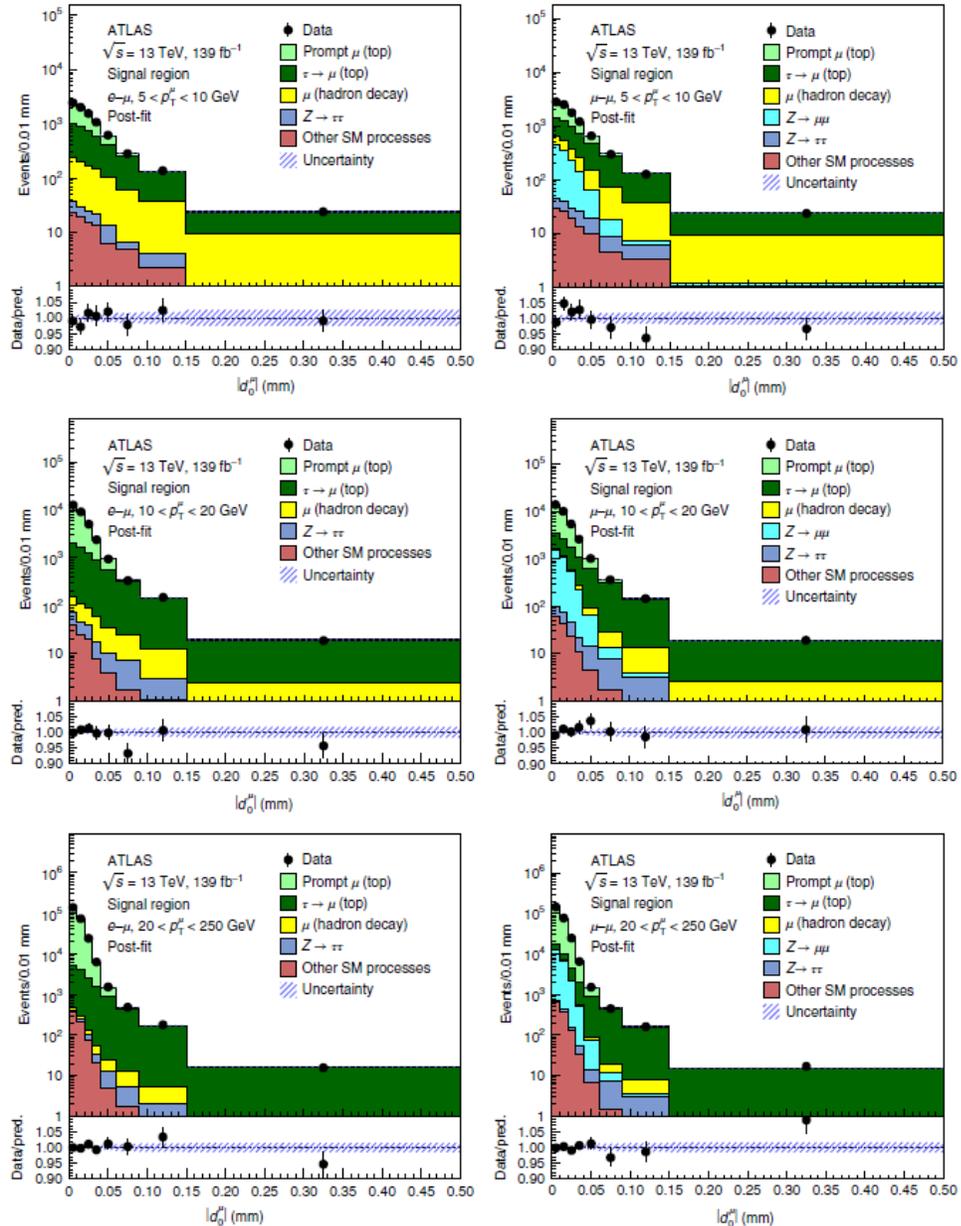
Using leptonic $\tau \rightarrow \mu$ decays = big challenge!

- Difficult to separate from soft muons (hadron decays)



(This is prompt lepton behaviour - i.e. unlikely to be same anomalous physics, but still interesting!)

Lepton Flavour Universality



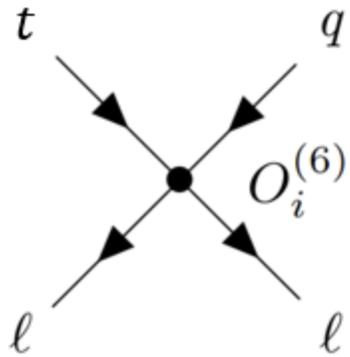
Top FCNC

(vs $b \rightarrow sll$)

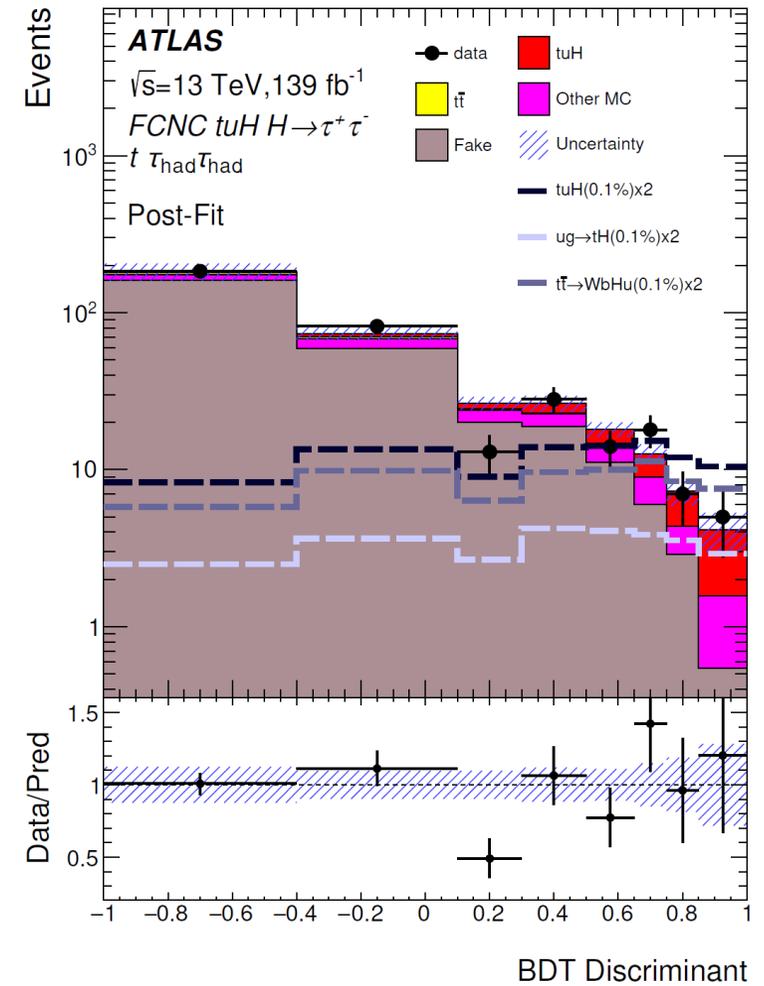
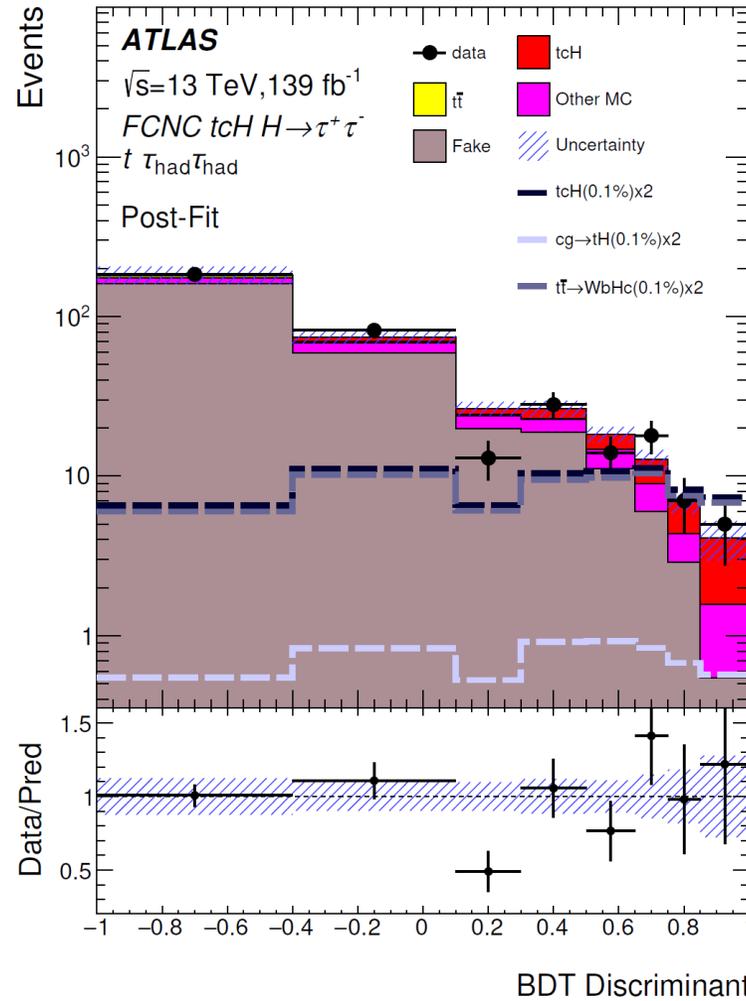
Top FCNC $t \rightarrow qH(\rightarrow \tau\tau)$

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FCNC (semi-diagonal)



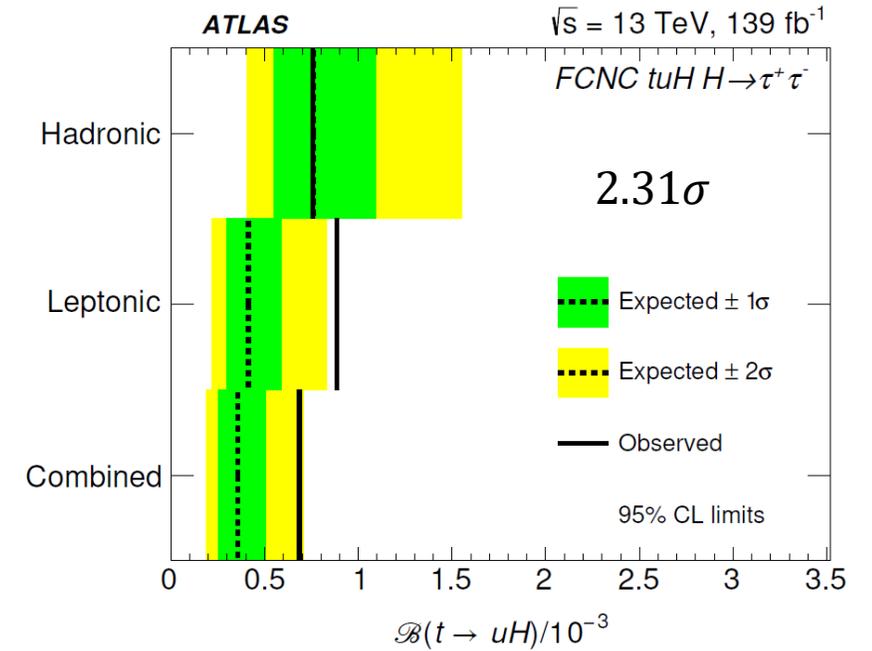
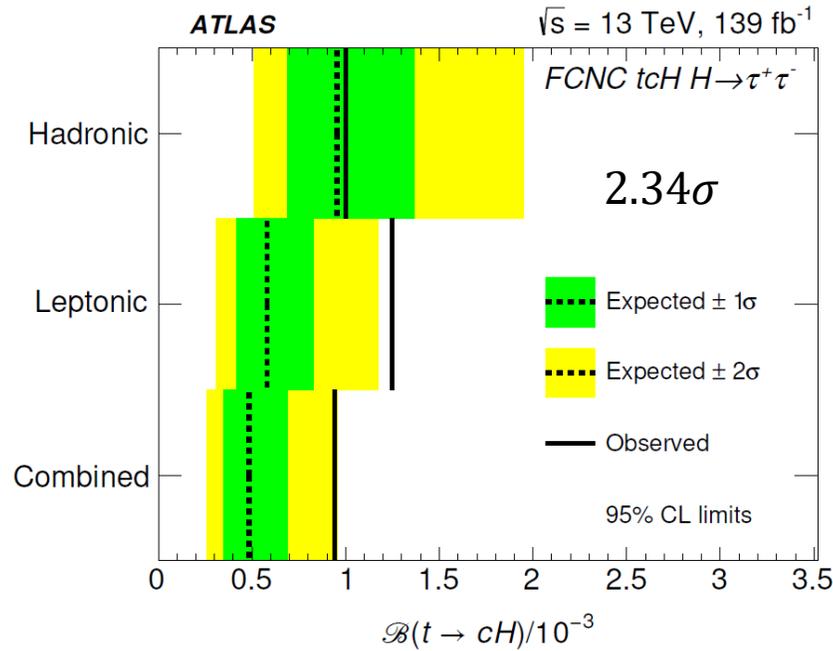
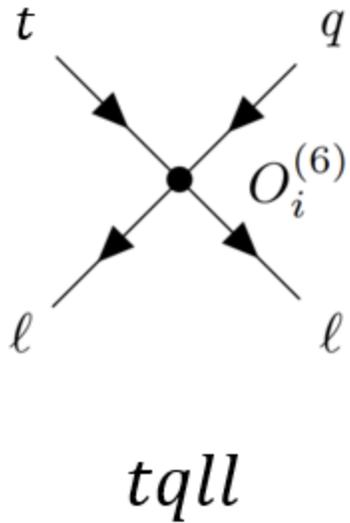
$tqll$



Top FCNC $t \rightarrow qH(\rightarrow \tau\tau)$

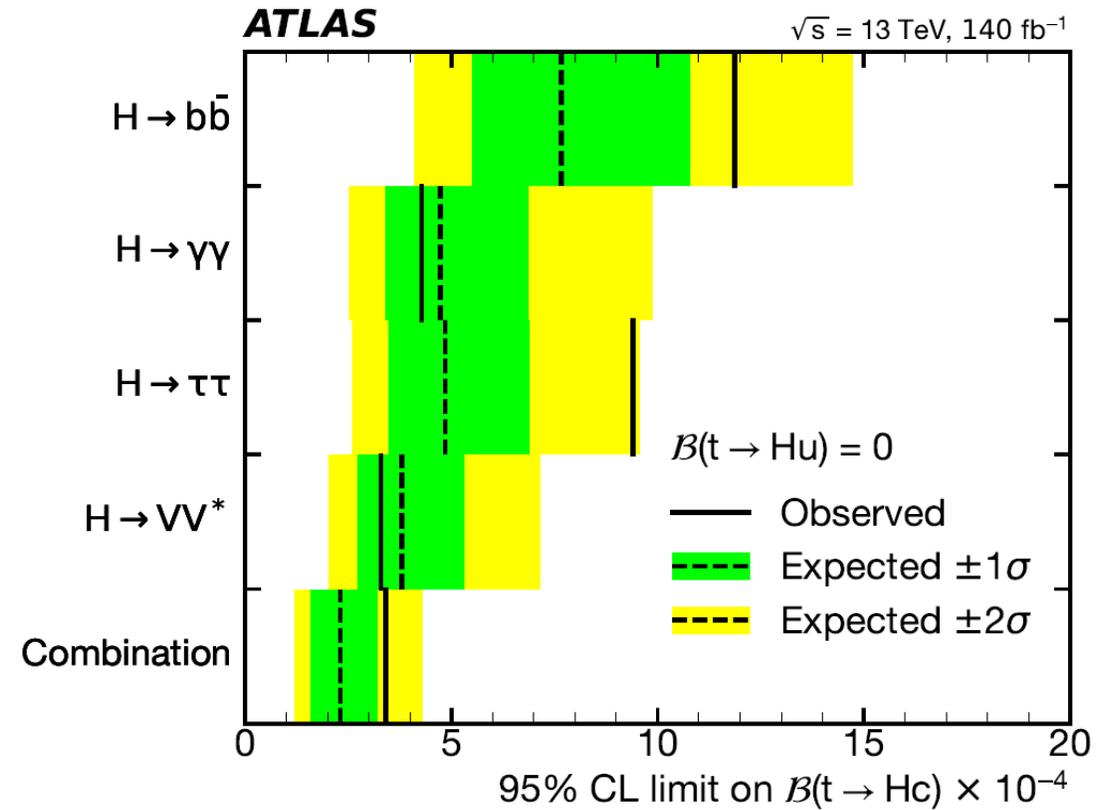
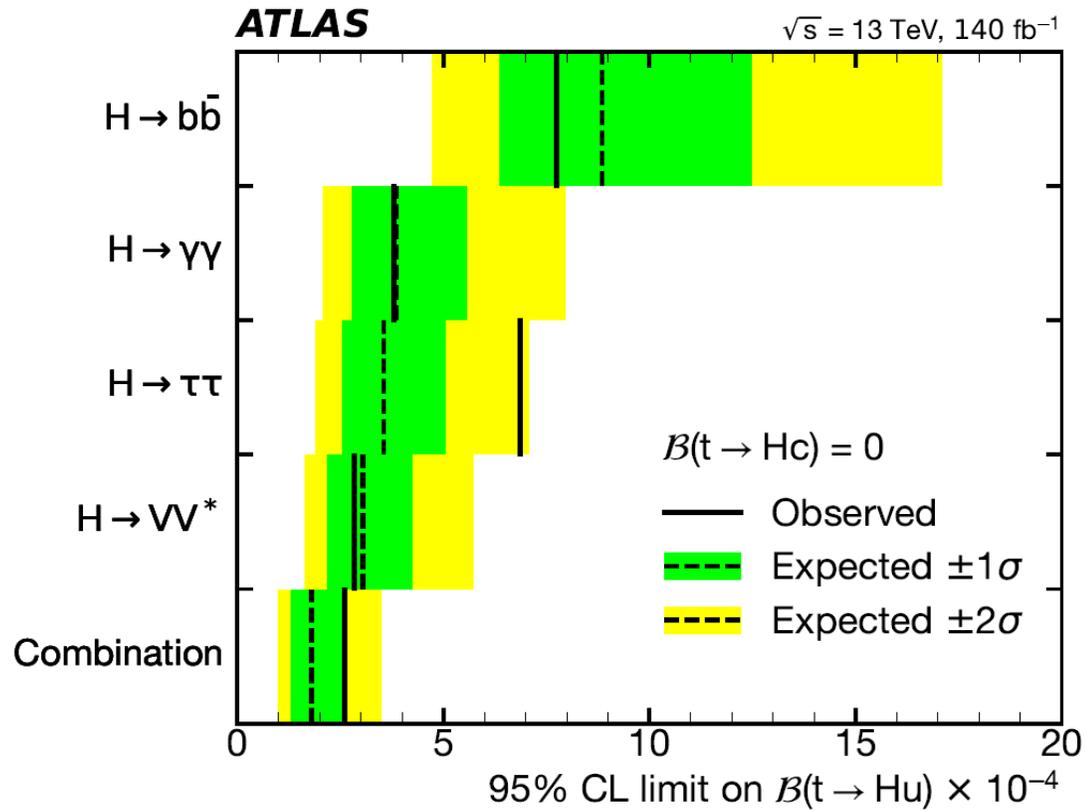
[JHEP 06 \(2023\) 155](#)

FCNC (semi-diagonal)



Top FCNC $t \rightarrow qH(\rightarrow XX)$

[arXiv:2404.02123](https://arxiv.org/abs/2404.02123)



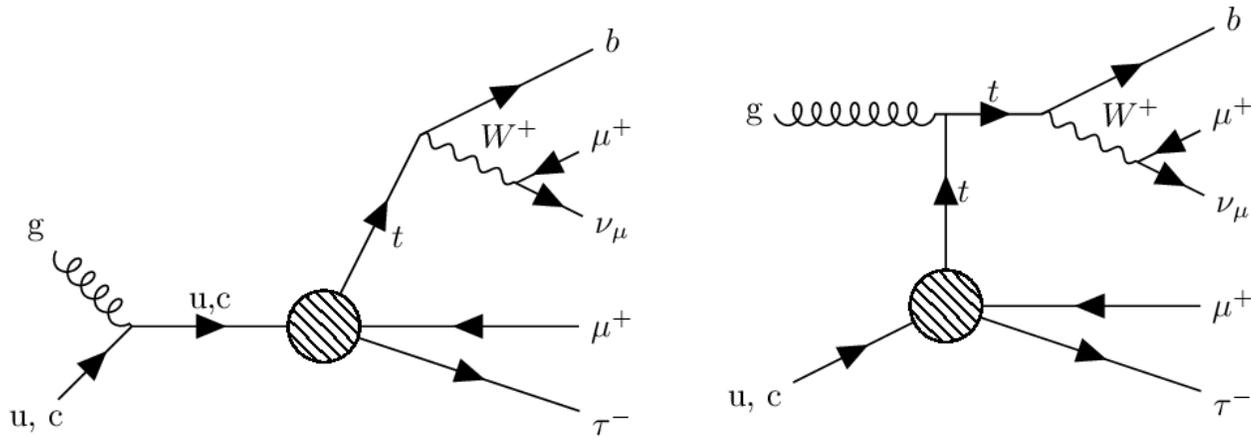
Top Charged-Lepton Flavour-Violation

(vs B / Lep flavour anomalies)

Top CLFV

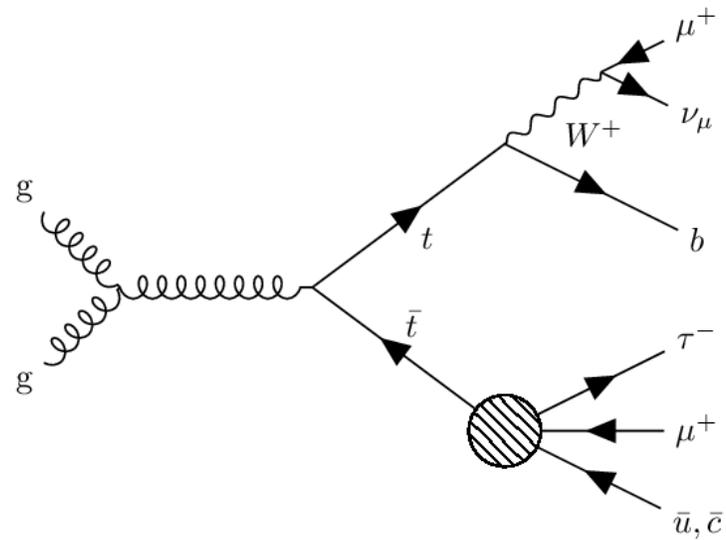
Production

$$qg \rightarrow tll'$$



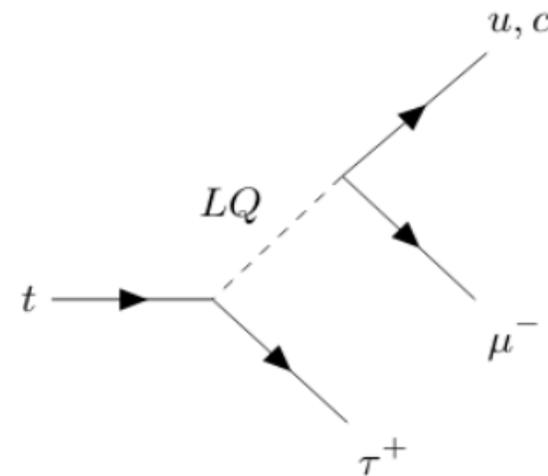
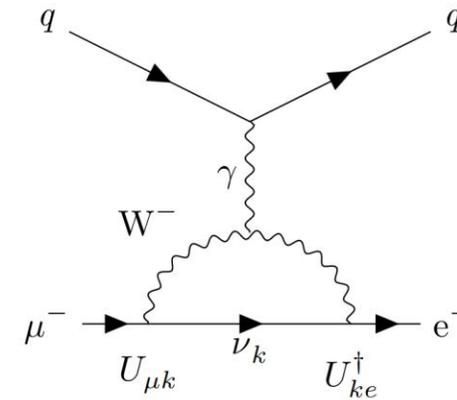
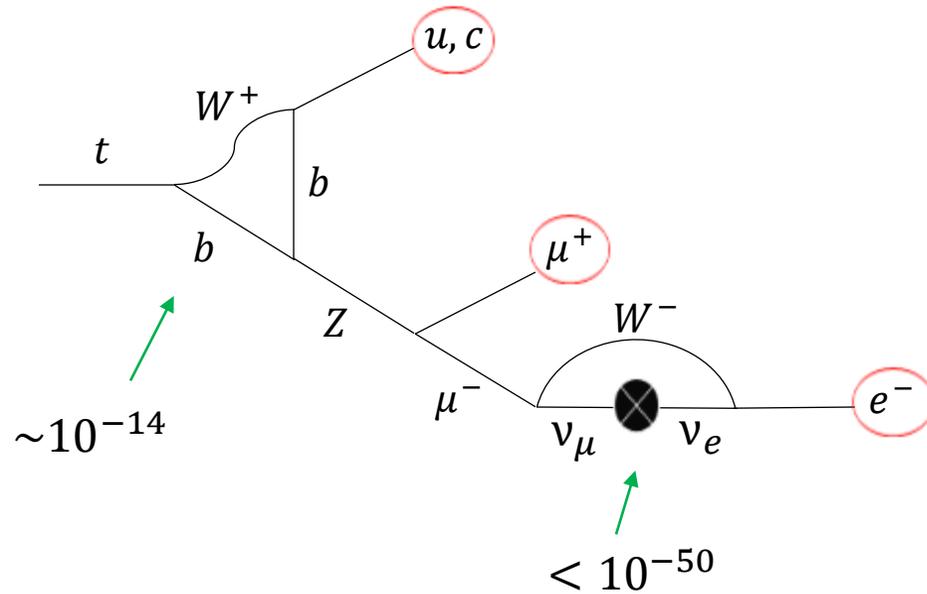
Decay

$$t\bar{t} \rightarrow (ll'q)(lvb)$$



CLFV and Neutrino Oscillations / New Physics

Neutrino oscillations \rightarrow LFV in lepton sector but far beyond any experimental sensitivity

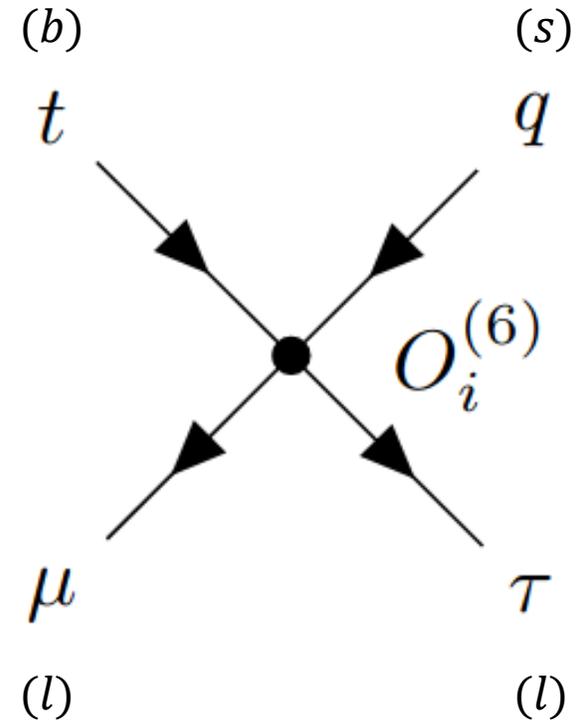


New physics which introduces additional terms involving lepton fields in Lagrangian can lead to LFV, e.g. SUSY, leptoquarks, 2HDMs



2Q2L EFT operators

Operator	Interaction	Lorentz Structure
$O_{lq}^{1(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lq}^{3(ijkl)}$	$(\bar{l}_i \gamma^\mu \sigma^I l_j)(\bar{q}_k \gamma_\mu \sigma_I q_l)$	Vector
$O_{eq}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lu}^{(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$O_{eu}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$O_{lequ}^{1(ijkl)}$	$(\bar{l}_i e_j) \varepsilon (\bar{q}_k u_l)$	Scalar
$O_{lequ}^{3(ijkl)}$	$(\bar{l}_i \sigma^{\mu\nu} e_j) \varepsilon (\bar{q}_k \sigma_{\mu\nu} u_l)$	Tensor



Recent history

Limits on CLFV branching ratio of top (95% CL):

$$B(t \rightarrow ll'q) < 1.86 \times 10^{-5}$$

[ATLAS-CONF-2018-044](#)

(3-lepton final state, 80 fb⁻¹)

$$B(t \rightarrow e\mu q) < 6.6 \times 10^{-6}$$

$$B(t \rightarrow e\mu q) < 0.009 - 0.258 \times 10^{-6}$$

[CMS-PAS-TOP-22-005](#)

(3-lepton final state, 138 fb⁻¹)

This analysis is first direct search for CLFV $\mu\tau qt$ coupling.

BSM models predicting CLFV with electrons/muons also apply to taus, often additionally enhanced due to larger mass



Charged Lepton Flavour Violation

Using [dim6top](#), found to agree with [SMEFTsim 3.0](#)

	Cross-section $\sigma_{-scale}^{+scale} \pm \text{PDF}$ [fb]		
	$c_{\text{vector}}^{(ijk3)}$	$c_{\text{lequ}}^{1(ijk3)}$	$c_{\text{lequ}}^{3(ijk3)}$
Production $\ell\ell' ut$	$118_{-19}^{+24} \pm 1$	$101_{-16}^{+21} \pm 1$	$2150_{-320}^{+410} \pm 20$
Production $\ell\ell' ct$	$7.9_{-1.0}^{+1.2} \pm 1.6$	$6.1_{-0.8}^{+1.0} \pm 1.5$	$153_{-18}^{+21} \pm 29$
Decay $\ell\ell' q_k t$	$6.9_{-1.3}^{+1.8} \pm 0.1$	$3.46_{-0.66}^{+0.90} \pm 0.03$	$166_{-32}^{+43} \pm 2$

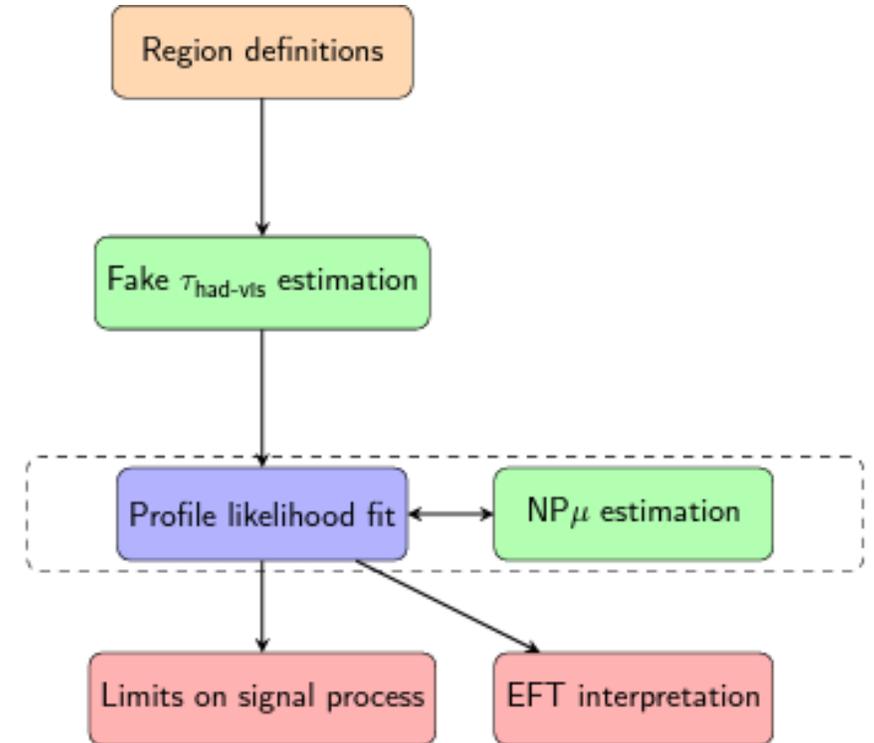
$$\Gamma(t \rightarrow \ell_i^+ \ell_j^- q_k) = \frac{m_t}{6144\pi^3} \left(\frac{m_t}{\Lambda}\right)^4 \left\{ 4|c_{\text{lq}}^{-(ijk3)}|^2 + 4|c_{\text{eq}}^{(ijk3)}|^2 + 4|c_{\text{lu}}^{(ijk3)}|^2 + 4|c_{\text{eu}}^{(ijk3)}|^2 + 2|c_{\text{lequ}}^{1(ijk3)}|^2 + 96|c_{\text{lequ}}^{3(ijk3)}|^2 \right\}$$

[JHEP04\(2019\)014](#)



Charged Lepton Flavour Violation

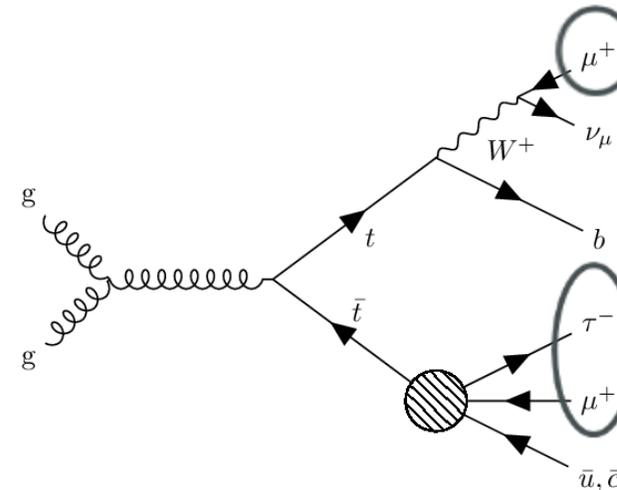
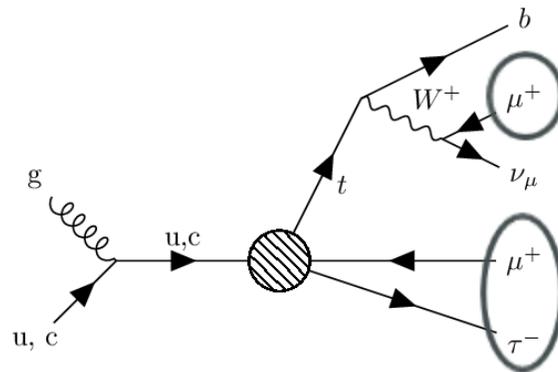
- Single lepton triggers
- Definition of analysis regions including dedicated CRs for fake backgrounds
 - Select events with electrons, muons and *hadronically-decaying* tau leptons ($\tau_{\text{had-vis}}$)
 - **Trilepton** selection: $\mu\mu\tau_{\text{had-vis}} / e\mu\mu$
- Prompt/real backgrounds estimated in MC ($t\bar{t}V$, diboson, tW)
- Data-driven estimation of fake lepton backgrounds
 - Fake $\tau_{\text{had-vis}}$ (+ 2 prompt μ): scale factor method
 - Non-prompt muons: template fit method (*takes place in PL fit*)
- Profile likelihood fit to SRs and non-prompt muon CR
- EFT interpretation



Event selection with 139 fb^{-1}

- Top quark decay and production diagrams differ by 1-jet
- Trilepton event selection including hadronic taus
- Same-sign muons produce significant background reduction

	SR	CR τ	CR $t\bar{t}\mu$
Lepton flavour	$2\mu 1\tau_{\text{had}}$		$2\mu 1e (\ell_3 = \mu)$
N_{jets}	≥ 1	≥ 2	≥ 1
$N_{b\text{-tags}}$	1	1	≤ 2
$\tau_{\text{had}} p_{\text{T}}$	$> 20 \text{ GeV}$	$> 20 \text{ GeV}$	–
Muon p_{T}	$> 15 \text{ GeV}$	$> 15 \text{ GeV}$	$> 10 \text{ GeV}$
Higher p_{T} muon	Tight	Tight	Tight
Lower p_{T} muon	Tight	Tight	Loose
Muon charges	SS	OS	–
$m_{\mu\mu}^{\text{OS}}$	–	–	$> 15 \text{ GeV}$
$ m_{\mu\mu}^{\text{OS}} - M_Z $	–	$< 10 \text{ GeV}$	$> 10 \text{ GeV}$
$3p_{\text{T}}^{\mu_1} + \sum m_{\ell\ell}^{\text{OS}}$	–	–	$< 400 \text{ GeV}$



Yields

Process	SR			CR $t\bar{t}\mu$		
$t\bar{t} + \text{NP } \mu$	7.9	\pm	3.4	164	\pm	14
$t\bar{t}W$	3.5	\pm	1.8	1.2	\pm	0.6
$t\bar{t}H$	3.1	\pm	0.4	1.26	\pm	0.14
$t\bar{t}Z$	2.9	\pm	0.5	0.88	\pm	0.33
$t+X$	2.48	\pm	0.18		–	
WZ	3.6	\pm	1.3	7.3	\pm	2.4
ZZ	0.59	\pm	0.22	1.8	\pm	0.6
VVV	0.01	\pm	0.05	0.47	\pm	0.24
Fake electron		–		7	\pm	4
Fake τ	3.3	\pm	0.4		–	
Fake $\tau + \text{NP } \mu$	3.7	\pm	2.7		–	
$t+X + \text{NP } \mu$	0.29	\pm	0.31	15	\pm	5
$Z + \text{NP } \mu$	0.192	\pm	0.010	1.8	\pm	1.0
Other NP μ	0.051	\pm	0.010		–	
Other	0.23	\pm	0.11	1.1	\pm	0.6
Signal ($t\bar{t}$)	0.19	\pm	0.14	0.025	\pm	0.019
Signal (single-top)	6	\pm	4	0.022	\pm	0.023
Total	38	\pm	5	201	\pm	14
Data	37			202		



Fake-tau estimation

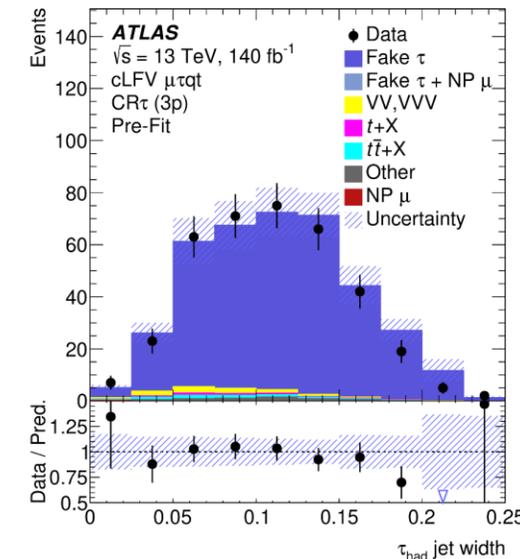
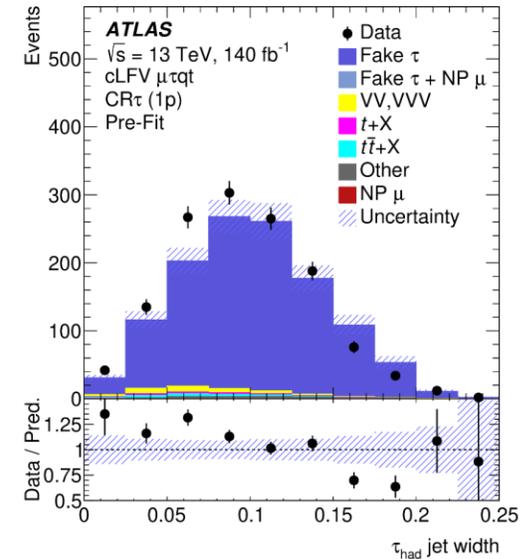
Fakes are usually due to mis-identified jets

Dedicated CR (does not enter the fit)

Scale factors (SF) are used to correct the rate of the fake-tau background

SFs are parameterised by:

- Track multiplicity (1-prong / 3-prong)
- Tau-jet width
 - This is a good proxy for the quark-gluon fractions which may differ slightly between SR/CR and between data and MC
- Systematics for SM backgrounds are propagated to the SFs and correlated appropriately in the fits

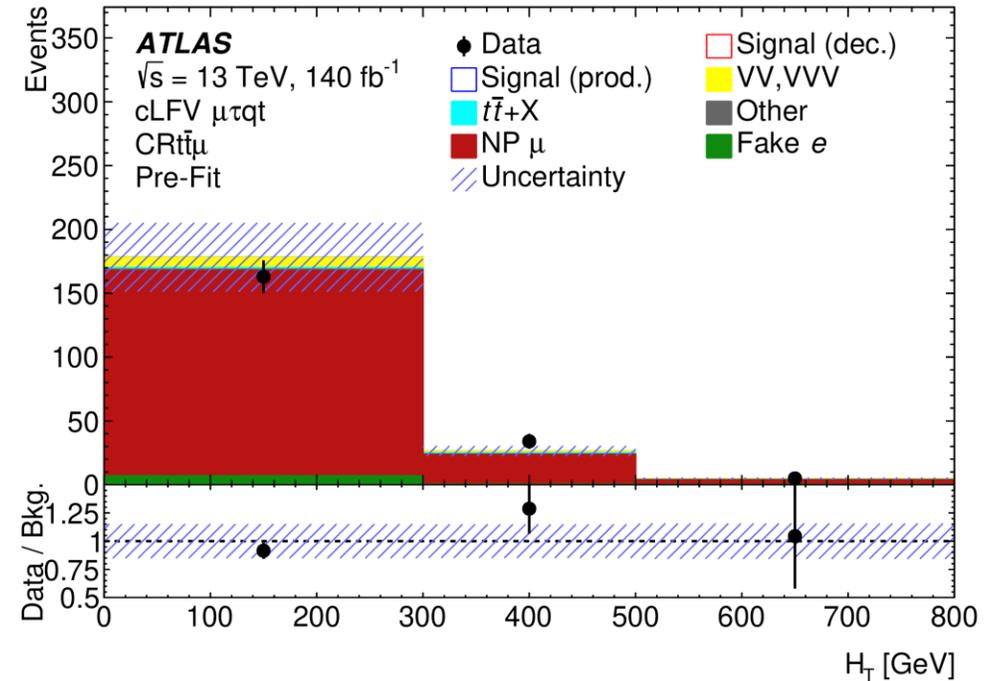


Fake/Non-prompt (NP) muon estimation

Dedicated CR (enters the fit)

Targeting non-prompt muons from b -jets in $t\bar{t}$ events

Normalisation is controlled by a profile-likelihood fit (next slides)



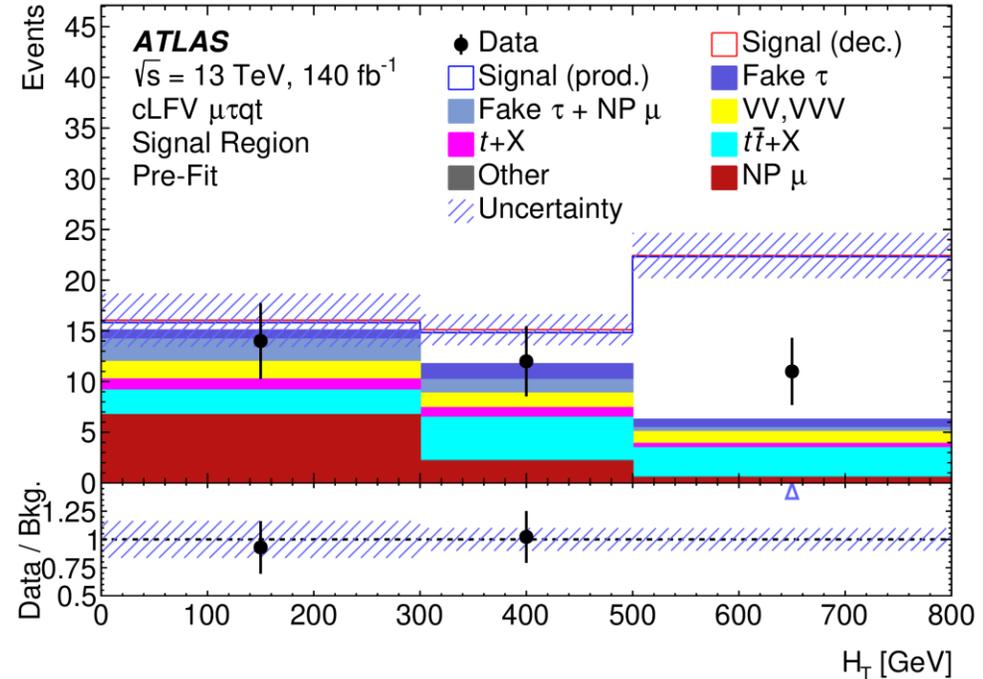
Signal region

Binned in HT to capture energy growth behaviour of EFT operators

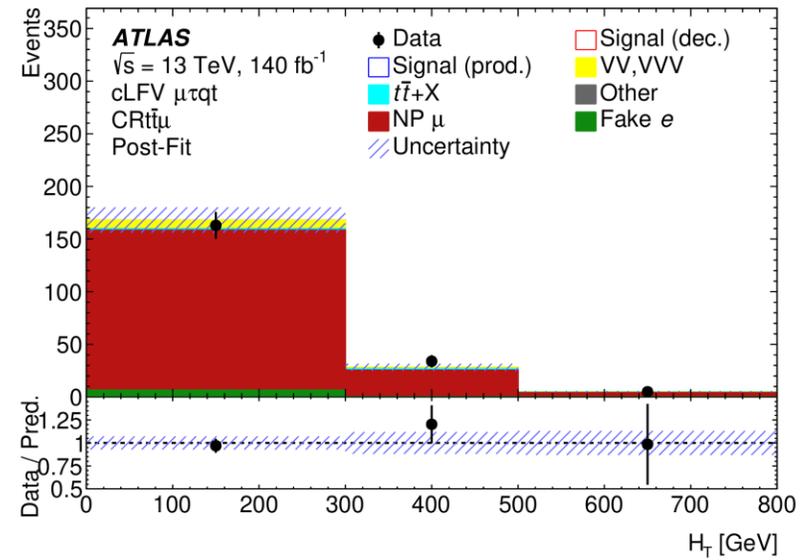
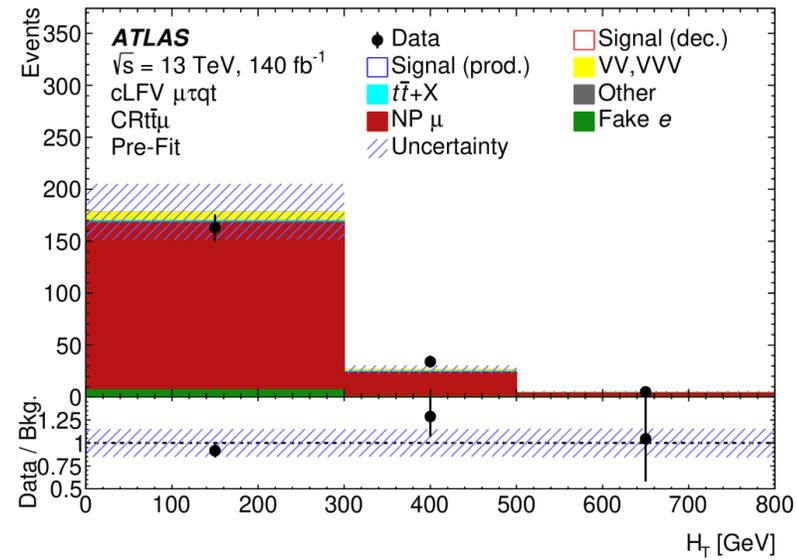
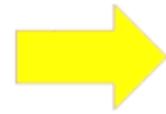
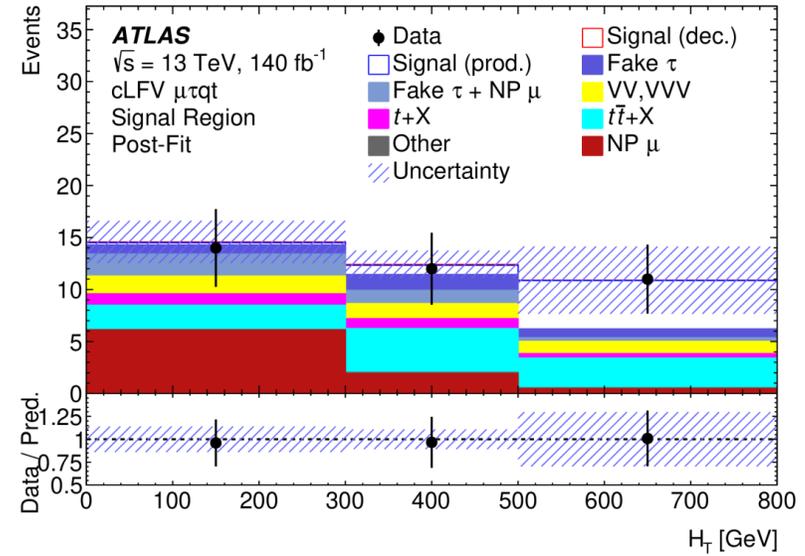
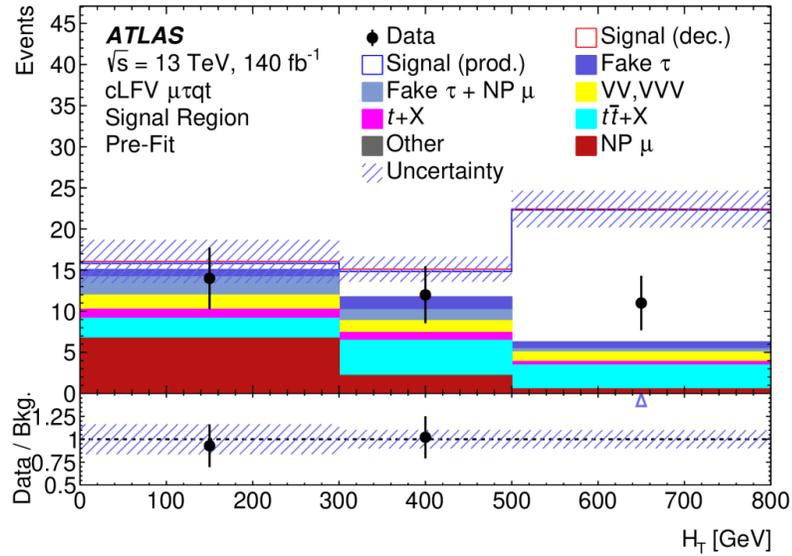
Signal shown is inclusive EFT (up-initiated, charm-initiated, all operators)

For up-quark operators, the production mode (blue) dominates the cross-section and sensitivity

For charm-quark operators, the production and decay modes are more balanced



Profile-likelihood fit



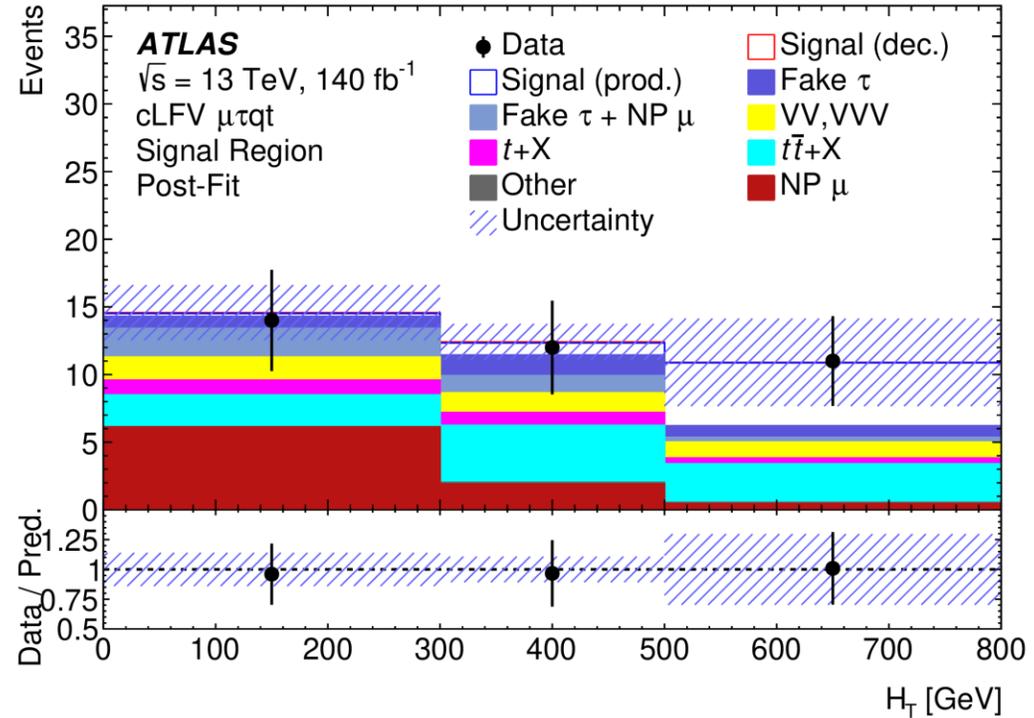
Profile-likelihood fit

Good agreement between data and background-only model

Statistically limited result

Largest systematics are signal, $t\bar{t}W$ and diboson modelling

1.6σ tension



'Inclusive' BR limits set assuming all EFT operators are of equal magnitude

	95% CL upper limits on $\mathcal{B}(t \rightarrow \mu\tau q)$	
	Stat. uncertainty	Stat.+syst. uncertainties
Expected	4.6×10^{-7}	5.0×10^{-7}
Observed	8.2×10^{-7}	8.7×10^{-7}



EFT Result breakdown

	95% CL upper limits on $\mathcal{B}(t \rightarrow \mu\tau q)$ ($\times 10^{-7}$)					
	$c_{lq}^{-(ijk3)}$	$c_{eq}^{(ijk3)}$	$c_{lu}^{(ijk3)}$	$c_{eu}^{(ijk3)}$	$c_{lequ}^{1(ijk3)}$	$c_{lequ}^{3(ijk3)}$
Expected (u)	2.3	2.0	1.9	2.2	1.2	3.0
Observed (u)	4.0	3.6	3.3	3.8	2.0	5.2
Expected (c)	33	32	32	33	20	41
Observed (c)	56	54	53	54	34	67

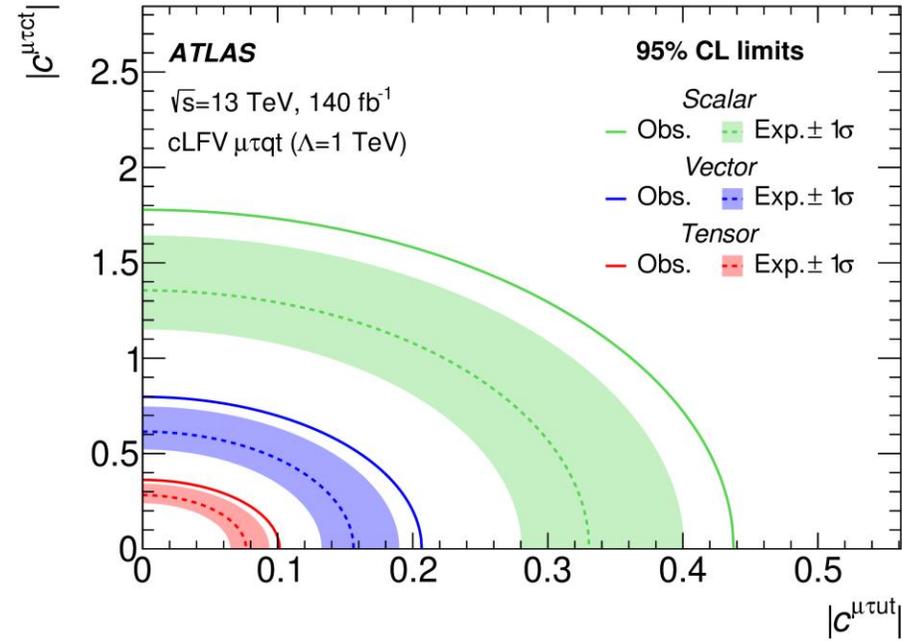
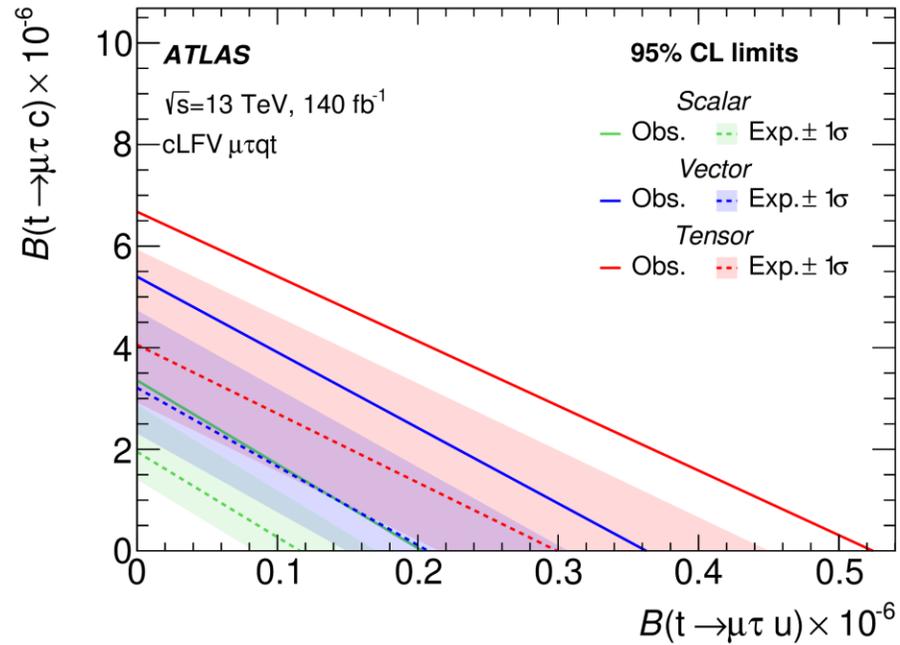
	95% CL upper limits on $ c /\Lambda^2$ [TeV $^{-2}$]					
	$c_{lq}^{-(ijk3)}$	$c_{eq}^{(ijk3)}$	$c_{lu}^{(ijk3)}$	$c_{eu}^{(ijk3)}$	$c_{lequ}^{1(ijk3)}$	$c_{lequ}^{3(ijk3)}$
Previous (u)	12	12	12	12	18	2.4
Expected (u)	0.33	0.31	0.3	0.32	0.33	0.08
Observed (u)	0.43	0.41	0.4	0.42	0.44	0.10
Previous (c)	14	14	14	14	21	2.6
Expected (c)	1.3	1.2	1.2	1.2	1.4	0.28
Observed (c)	1.6	1.6	1.6	1.6	1.8	0.36

EFT limits improve upon previous results ([re-interpretation of ATLAS FCNC \$tZq\$ analysis](#)):

- From factors of 7.2 for $c_{lequ}^{3(2323)}$ (for $\mu\tau ct$) to 41 for $c_{lequ}^{1(2313)}$ (for $\mu\tau ut$).



EFT Result breakdown

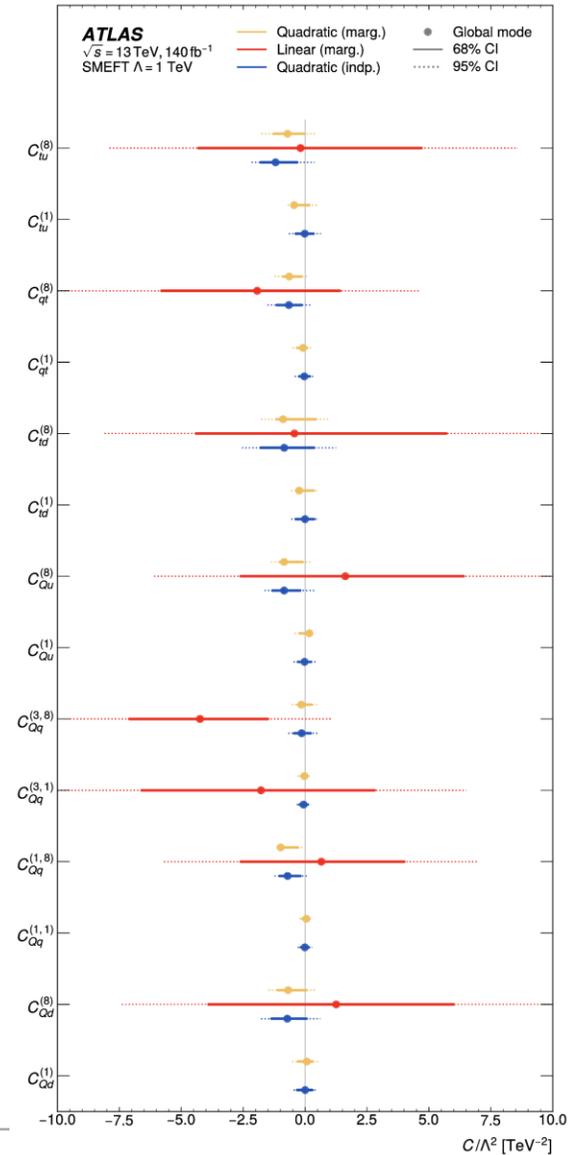
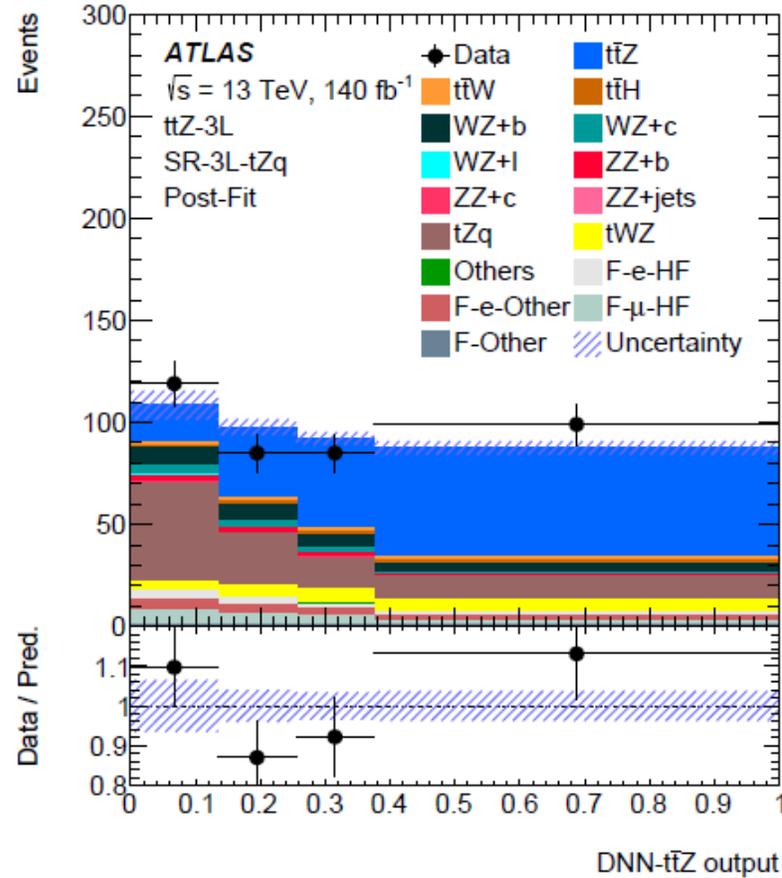
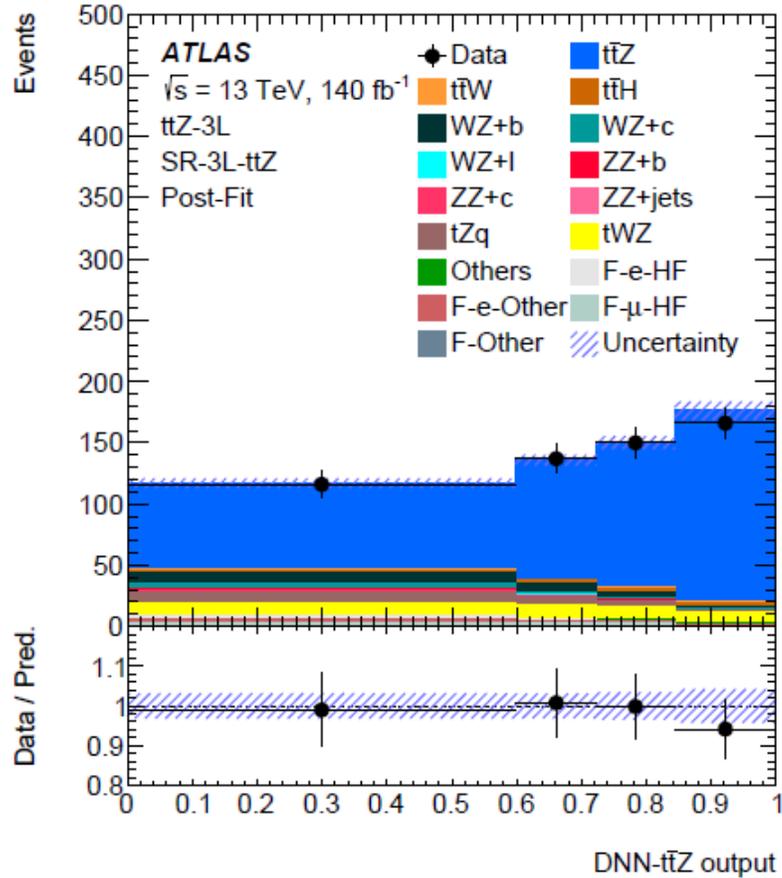


What's next?

Off-shell $t\bar{t}Z$ ($t\bar{t}ll$) and tZq ($tqll$)

Going off-shell

arXiv:2312.04450

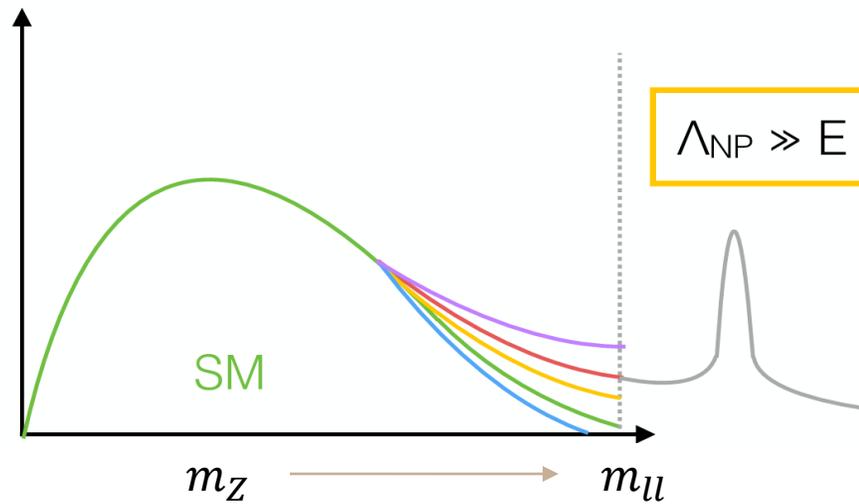


Going off-shell

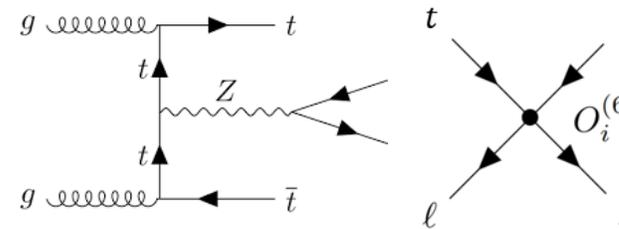
arXiv:2312.04450

Taking a $t\bar{t}Z$ style analysis and going off shell has benefits for NP searches:

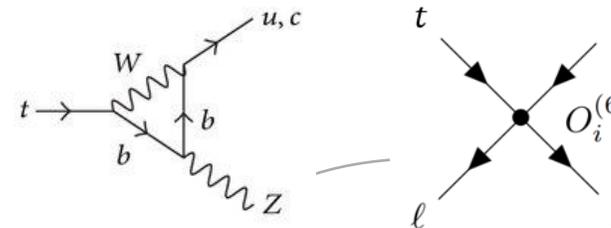
- Massively reduce SM backgrounds
- Enhance sensitivity to EFT operators (which exhibit energy growth)



$t\bar{t}Z$ search becomes $t\bar{t}ll$ search above Z peak



tZq search becomes tql search above Z peak

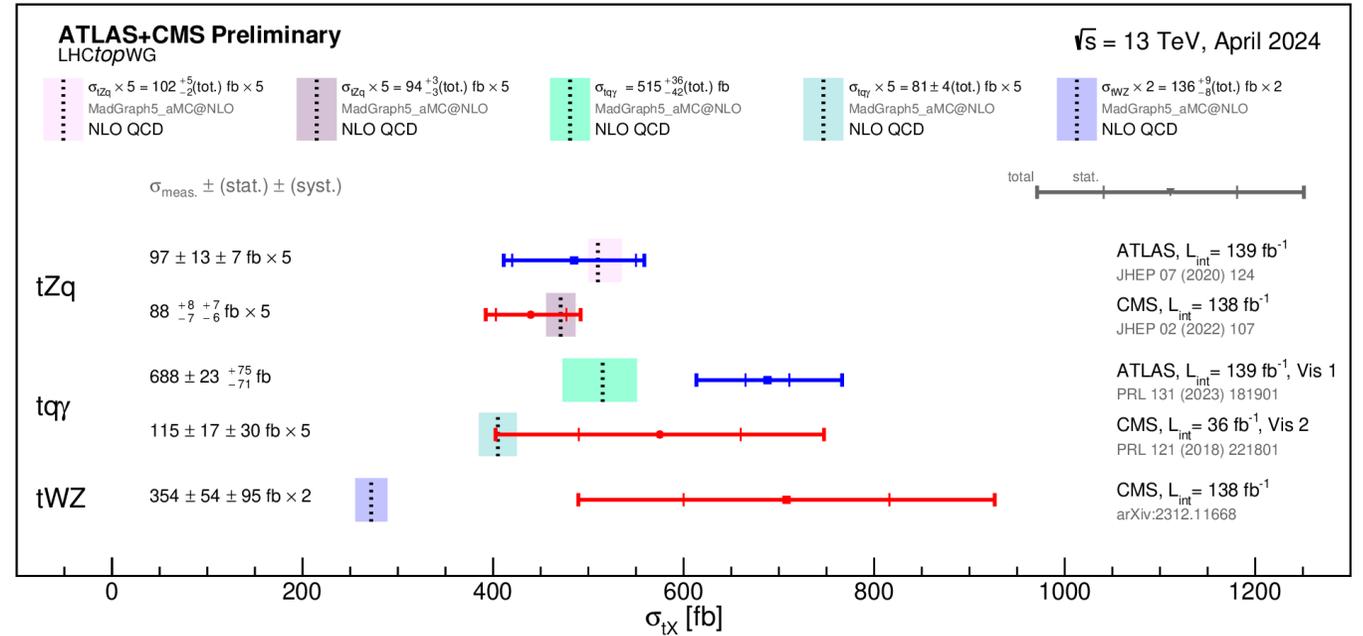
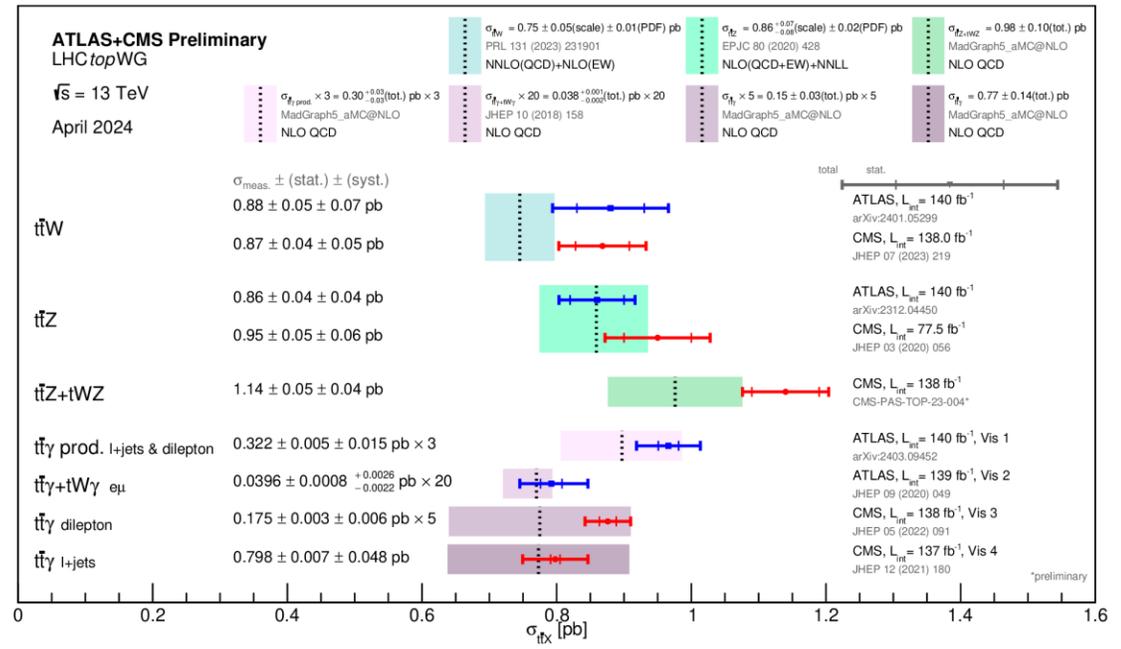
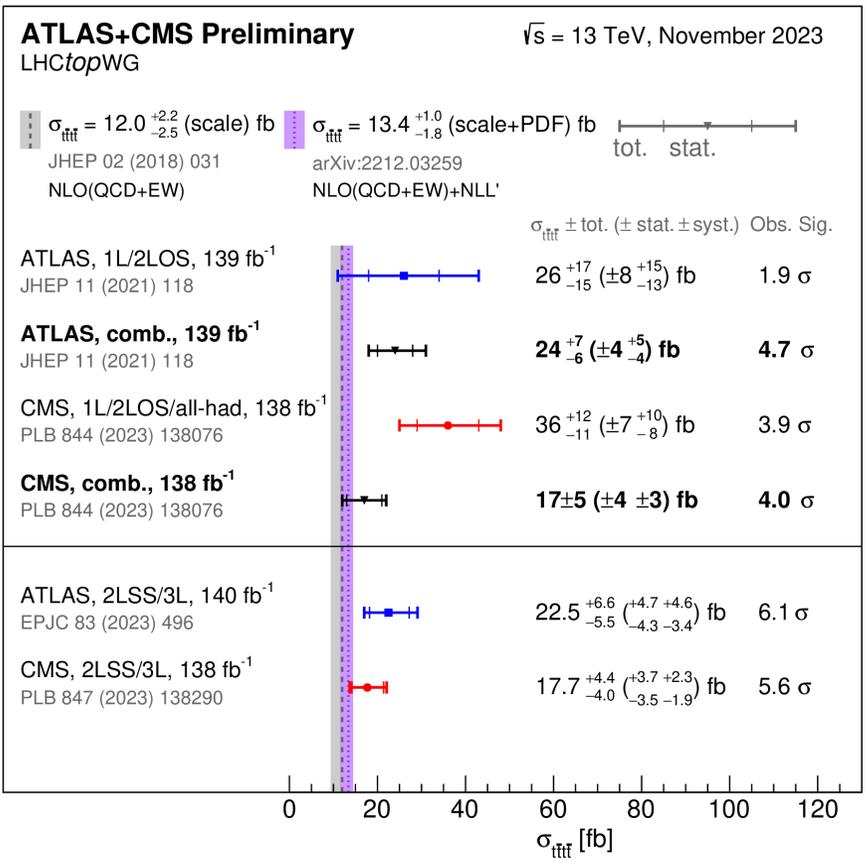


What's next?

Future Top+X EFT

Top+X ATL-PHYS-PUB-2024-005

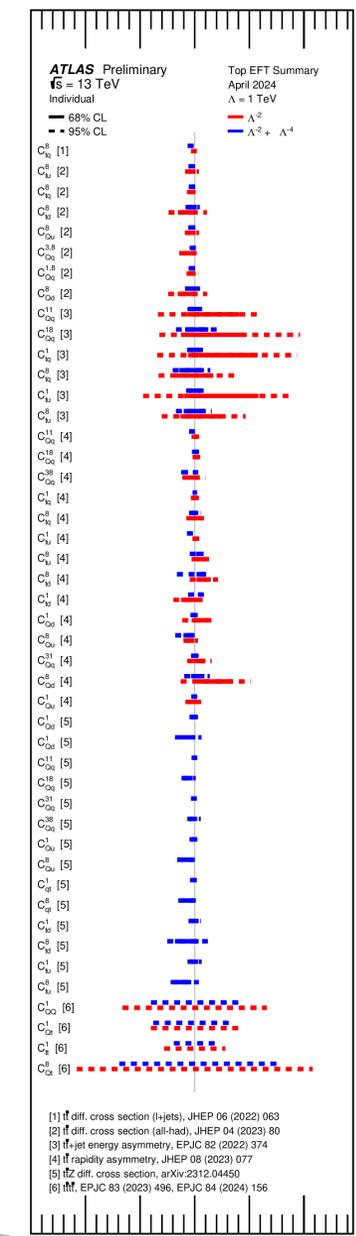
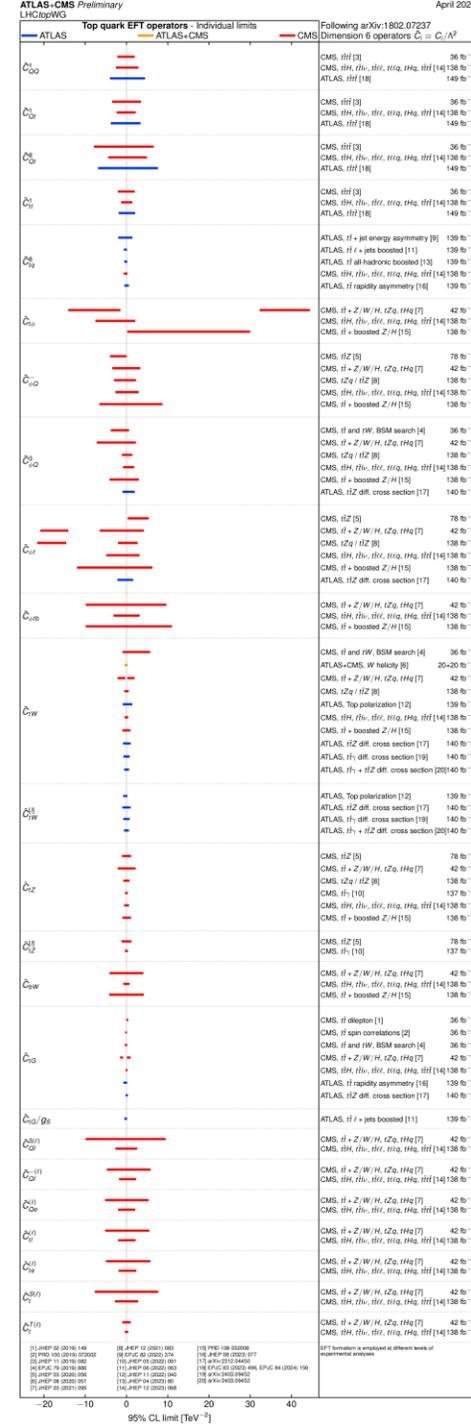
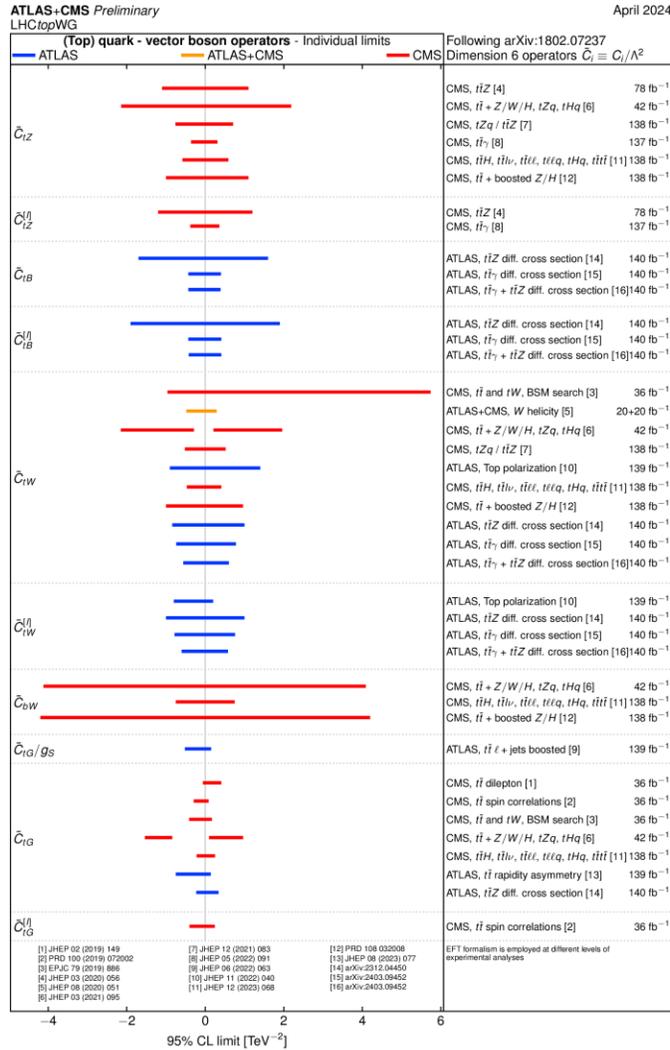
There are a lot of individual high-precision Top+X measurements!



Top EFT

ATL-PHYS-PUB-2024-004

There are a lot of individual high-precision Top EFT measurements!



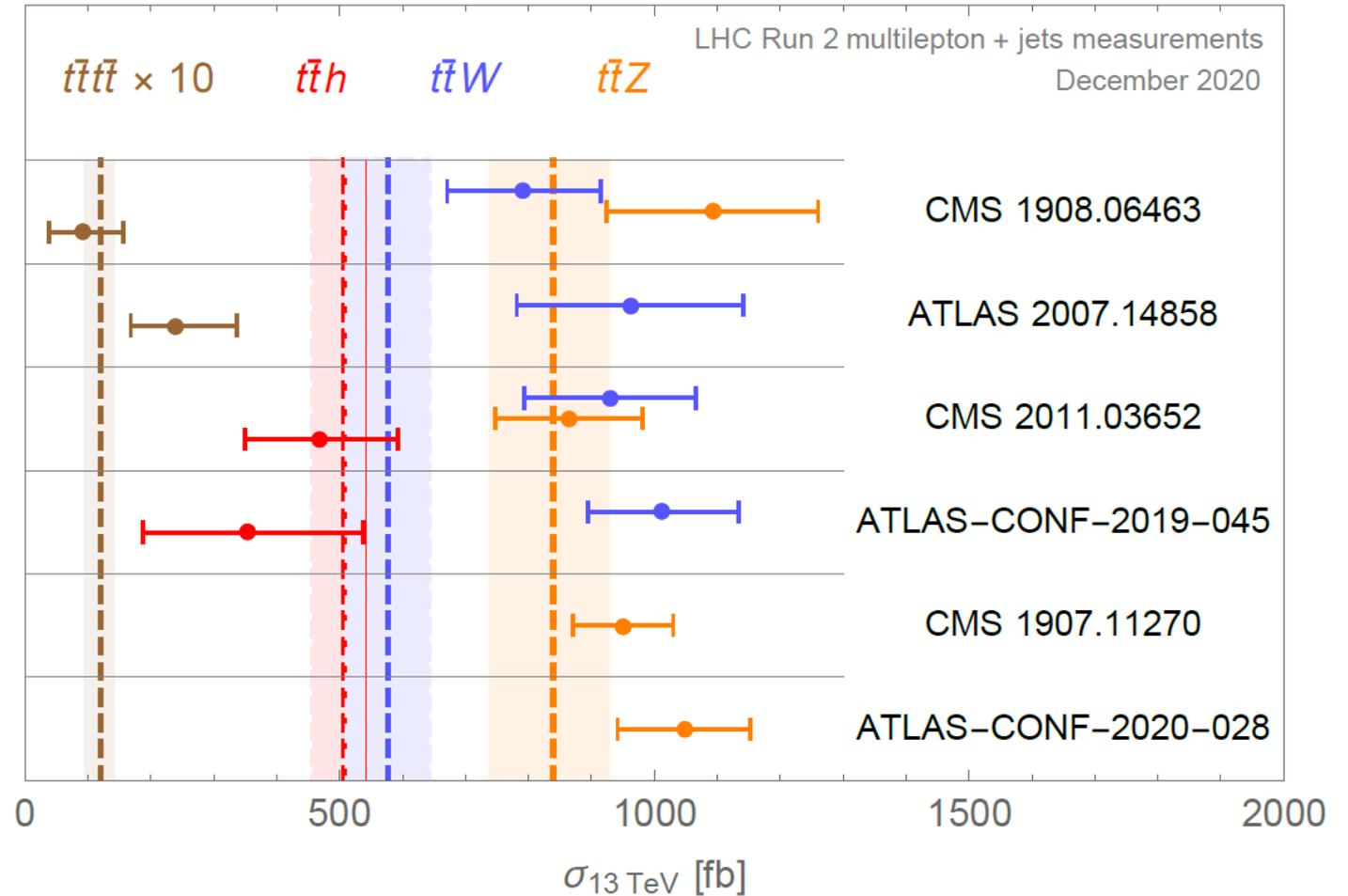
Top+X (EFT) Combinations

(Plot not up to date, just exemplar)

There are also some hints of disagreement with SM predictions - especially in $t\bar{t}W$ and potentially $t\bar{t}t\bar{t}$

How to understand these effects in the most robust way?

- In a Top+X measurement, every other Top+X process is the main background
- Many Top+X processes are sensitive to the same EFT couplings
- Impossible to disentangle them while measuring one at a time



[JHEP 02 \(2021\) 043](#)

Event category	Leptons	$m_{\ell\ell}$	b tags	Lepton charge sum	Jets	Kinematical variable
2l ss 2b	2	No requirement	2	>0, <0	4, 5, 6, ≥ 7	$p_T(\ell_j)_{\max}$
2l ss 3b	2	No requirement	≥ 3	>0, <0	4, 5, 6, ≥ 7	$p_T(\ell_j)_{\max}$
3l off-Z 1b	3	$ m_Z - m_{\ell\ell} > 10 \text{ GeV}$	1	>0, <0	2, 3, 4, ≥ 5	$p_T(\ell_j)_{\max}$
3l off-Z 2b	3	$ m_Z - m_{\ell\ell} > 10 \text{ GeV}$	≥ 2	>0, <0	2, 3, 4, ≥ 5	$p_T(\ell_j)_{\max}$
3l on-Z 1b	3	$ m_Z - m_{\ell\ell} < 10 \text{ GeV}$	1	No requirement	2, 3, 4, ≥ 5	$p_T(Z)$
3l on-Z 2b	3	$ m_Z - m_{\ell\ell} < 10 \text{ GeV}$	≥ 2	No requirement	2, 3, 4, ≥ 5	$p_T(Z)$ or $p_T(\ell_j)_{\max}$
4l	≥ 4	No requirement	≥ 2	No requirement	2, 3, ≥ 4	$p_T(\ell_j)_{\max}$

Grouping of WCs

WCs

Lead categories

2hq2l

$c_{Q\ell}^{3(\ell)}, c_{Q\ell}^{-3(\ell)}, c_{Qe}^{(\ell)}, c_{t\ell}^{(\ell)}, c_{te}^{(\ell)}, c_t^{S(\ell)}, c_t^{T(\ell)}$

3l off-Z

4hq

$c_{QQ}^1, c_{Qt}^1, c_{Qt}^8, c_{tt}^1$

2lss

2hq2lq "t \bar{t} lv-like"

$c_{Qq}^{11}, c_{Qq}^{18}, c_{tq}^1, c_{tq}^8$

2lss

2hq2lq "t \bar{t} lq-like"

c_{Qq}^{31}, c_{Qq}^{38}

3l on-Z

2hqV "t \bar{t} l \bar{t} -like"

$c_{tZ}, c_{\phi t}, c_{\phi Q}^-$

3l on-Z and 2lss

2hqV "tXq-like"

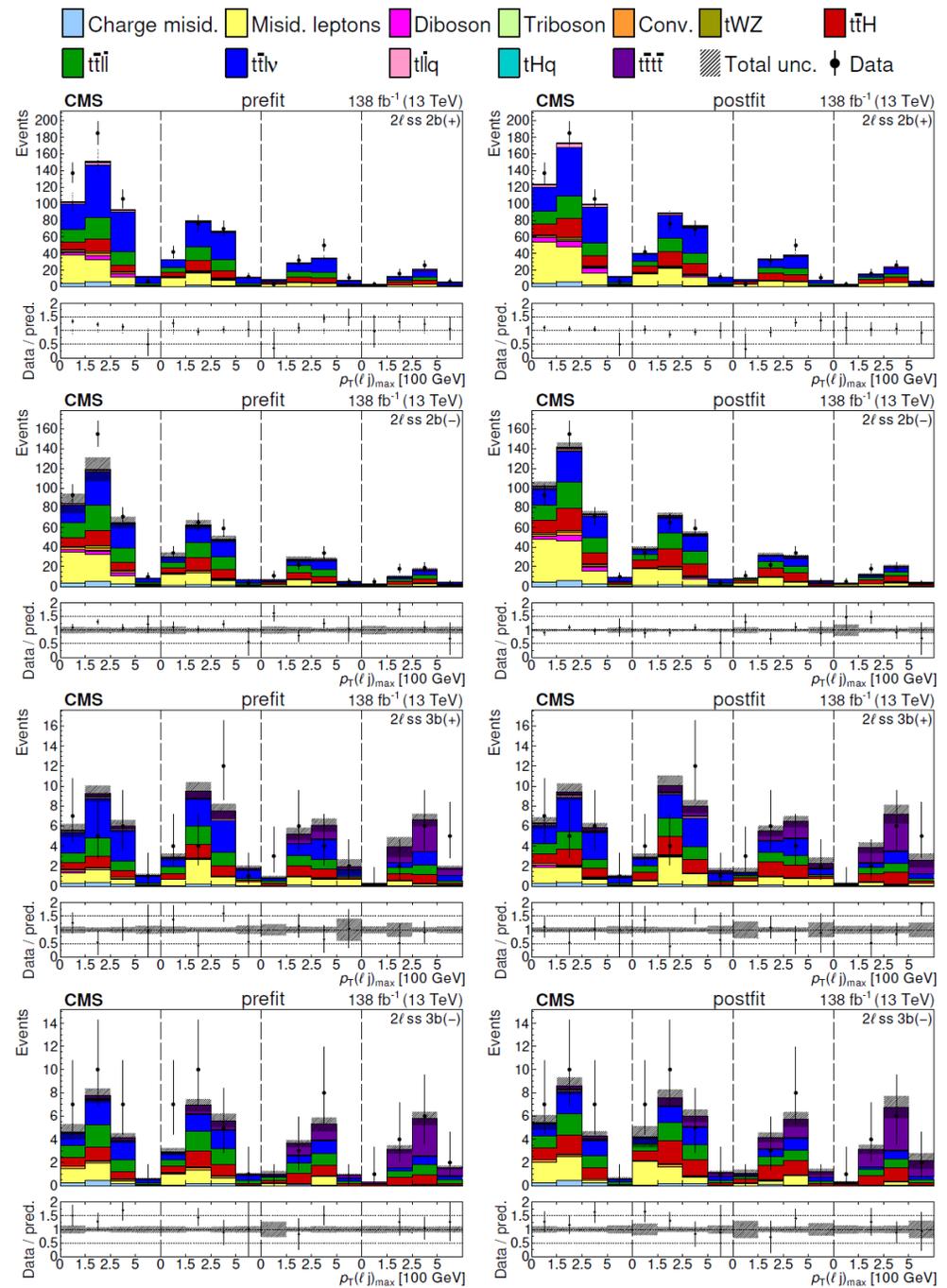
$c_{\phi Q}^3, c_{\phi tb}, c_{bW}$

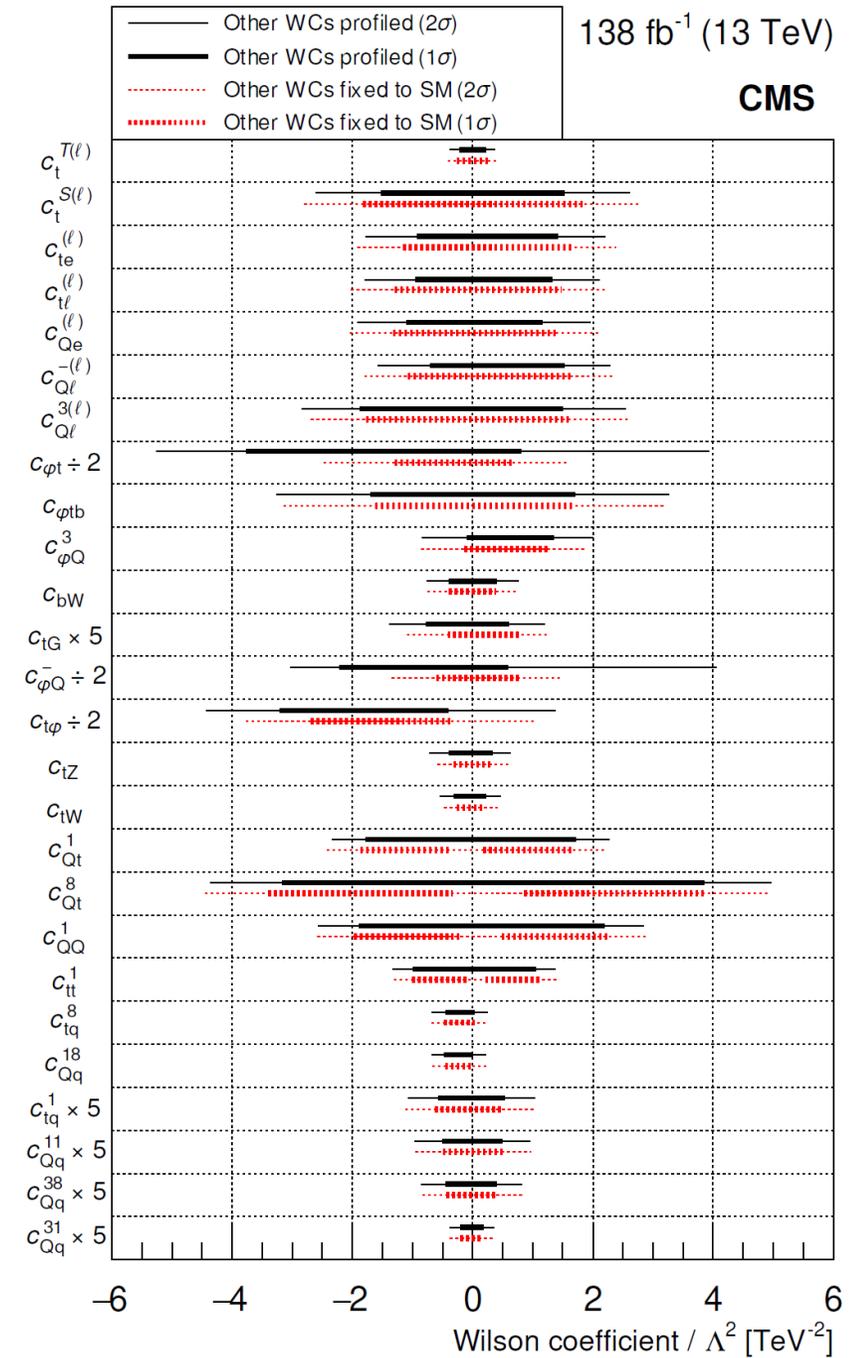
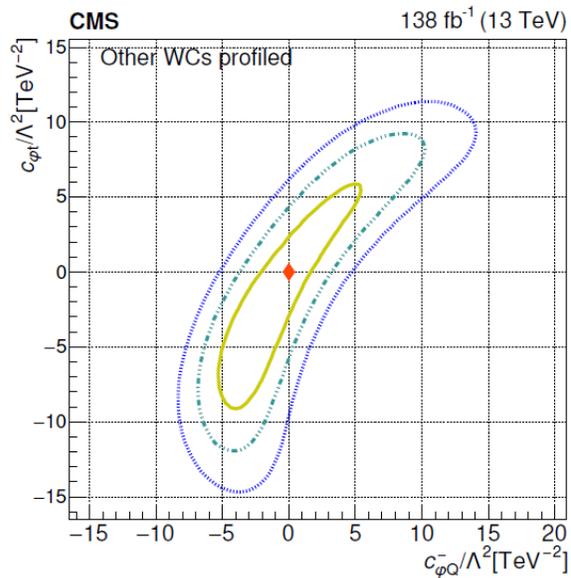
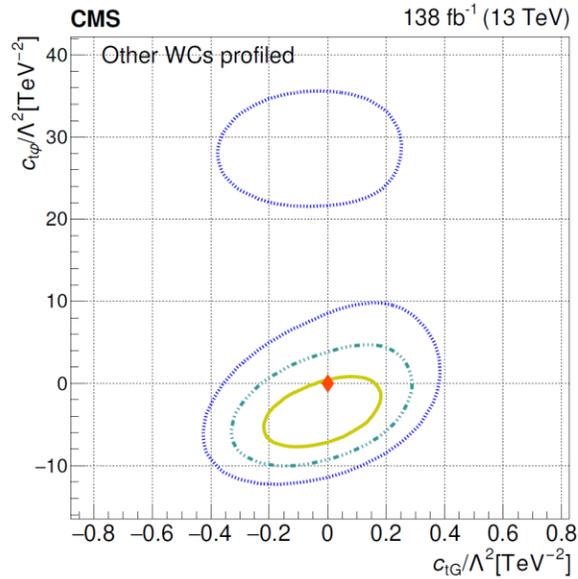
3l on-Z

2hqV (significant impacts on many processes)

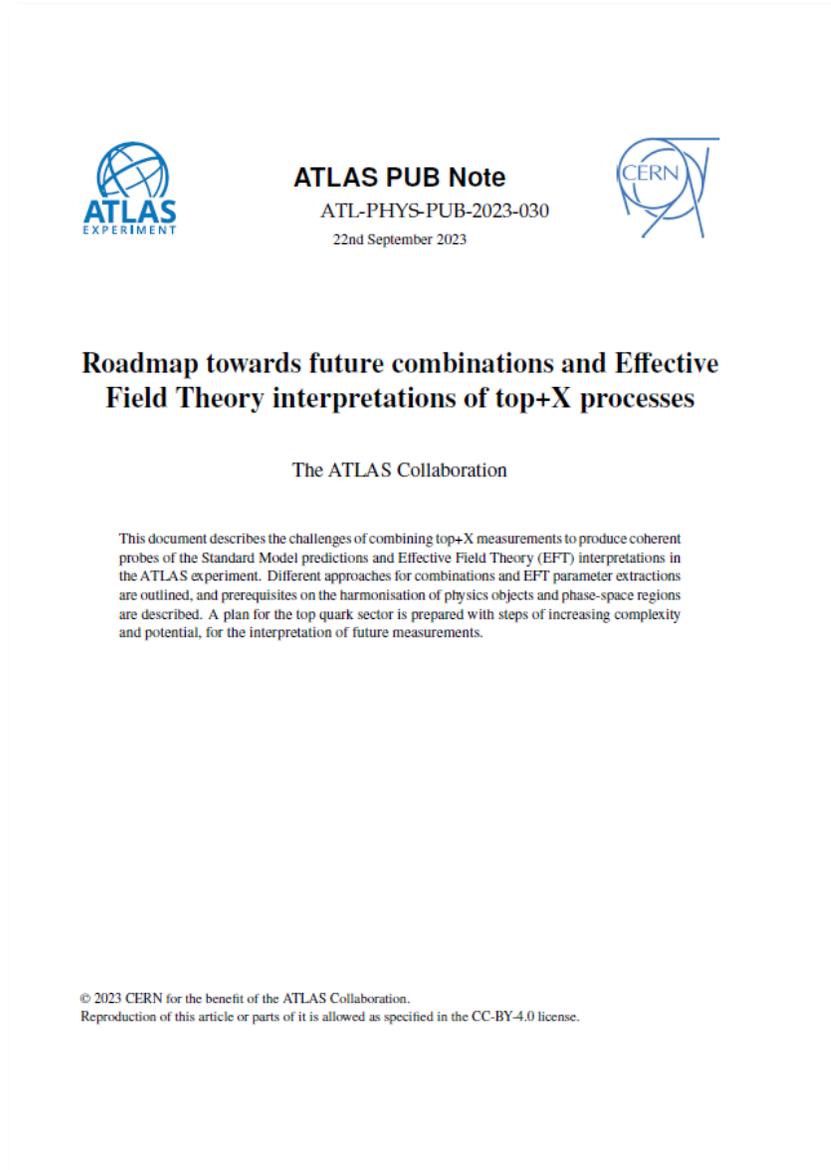
$c_{tG}, c_{t\phi}, c_{tW}$

3l and 2lss





ATLAS Top+X Roadmap



- **Describe:**
 - Challenges of combining Top+X measurements to coherently probe SM + EFTs
 - Available MC generators and UFOs
- **Discuss:**
 - Harmonisation of physics objects
 - Harmonisation of phase-space regions
- **Deliberate:**
 - Options for optimal observables
- **Develop:**
 - Incremental roadmap with increasing complexity, towards maximising the potential of Run-3 ATLAS data

[ATL-PHYS-PUB-2023-030](#)

ATLAS Top+X Roadmap

[ATL-PHYS-PUB-2023-030](#)

EFT for Monte Carlo

Generators:

- Madgraph
 - Predominant recommendation
 - Highly compatible with UFO models
 - 'Simple' user interface
 - Extension enabling computation of NLO in QCD and NLO EW corrections
 - (NLO generators often introduce more negative weights which can be difficult to deal with experimentally)
- Powheg:
 - Better modelling of SM $t\bar{t}$ process at NLO in QCD
 - Still requires reweighting according to MG5 EFT predictions
 - Resulting approximations would require extensive validation studies
- Pythia
 - Does not retain spin correlations
 - Problems associated to EFT operators which generate gluons and interaction with the parton shower

UFO models:

- SMEFTSim3.0
 - Current recommendation used widely in ATLAS
 - 'top' flavour assumption - treats operators with lepton-flavour indices as individual entities
 - LO accuracy only
 - Distinguishes between EFT insertions in vertices or in corrections to widths of propagators
- SMEFTatNLO
 - Both LO and NLO QCD precision
 - No implementation of CP violating operators, or operators with b-quarks in the initial state, or FCNC interactions
 - Extensive upgrades planned over the next ~5 years

Other topics discussed:

- Coupling orders
- Decomposition of EFT contributions
- Internal reweighting vs dedicated generation
- Higher-order corrections
- EFT effects in top decay

ATLAS Top+X Roadmap

[ATL-PHYS-PUB-2023-030](#)

Harmonisation

Object definitions proposals:

- Harmonise object definitions between all combinable analyses apriori
- Design lepton working points which support (pseudo)-continuous calibrations
- Adopt common-denominator systematic reduction schemes for different processes, according to the sensitivity of each

Phase-space regions proposals:

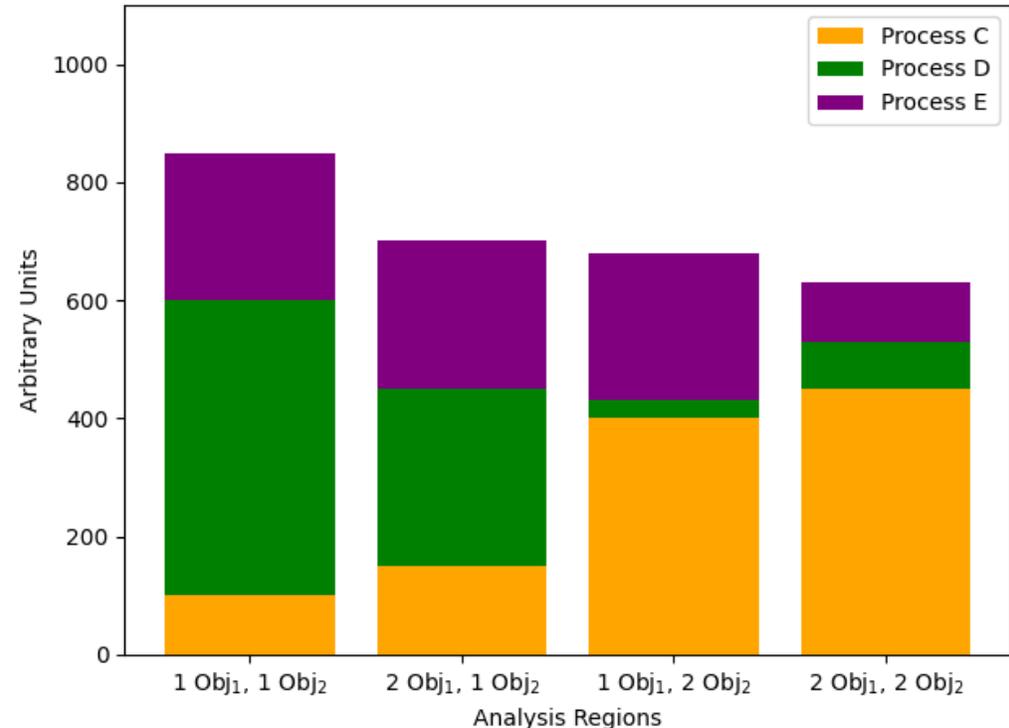
- Harmonise region definitions between all combinable analyses apriori
- Design common ML algorithms to separate heavily overlapping processes ($t\bar{t}H$, $t\bar{t}H$, $t\bar{t}t\bar{t}$)
- Adopt common fakes control regions between analyses

ATLAS Top+X Roadmap

ATL-PHYS-PUB-2023-030

Region definitions and fitting tactics:

- 1. Object-based (OB) fit:** The regions are broken down by lepton/jet/b-tag multiplicity, lepton charge etc. (à la CMS!)
 - Clean and simple to implement
 - Object + region harmonisation are automatic
 - Fakes treatment is coherent
- Some processes easy to distinguish - e.g. $t\bar{t}\gamma$
- Other processes difficult to separate this way - e.g. $t\bar{t}W, t\bar{t}H, t\bar{t}t\bar{t}$
- Principal Component Analysis will identify sensitive directions
- **Need to be clear what you are optimising for!**

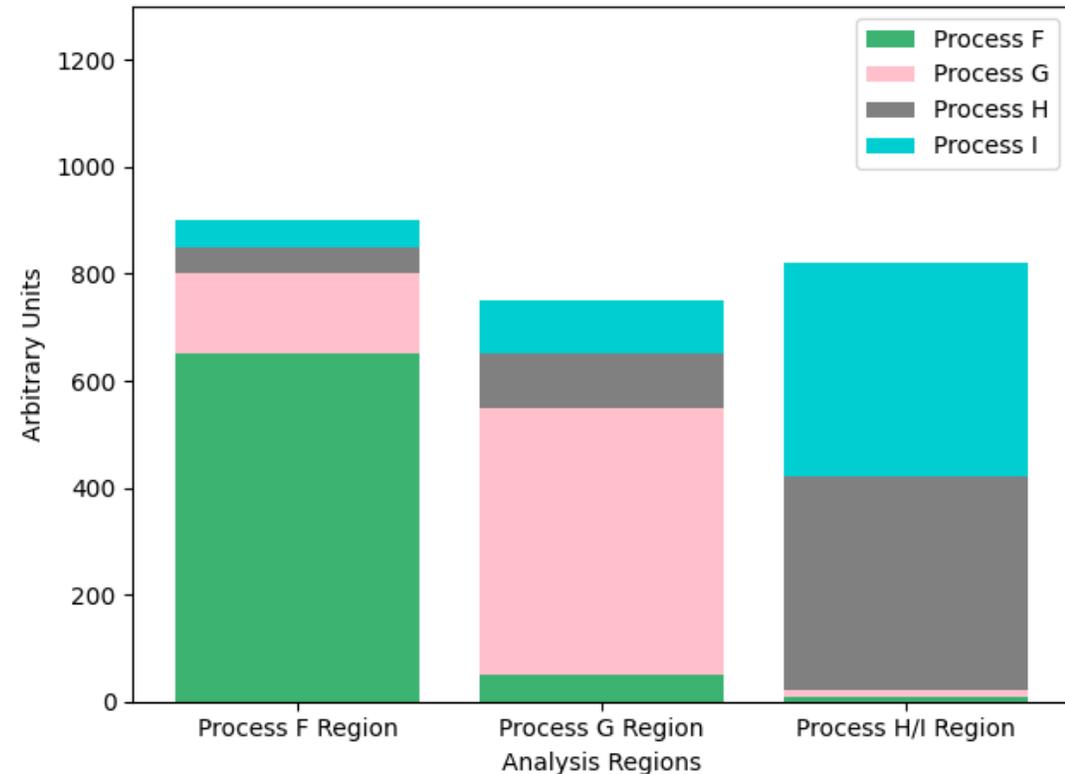


ATLAS Top+X Roadmap

ATL-PHYS-PUB-2023-030

2. Process-based (PB) fit: The regions are defined with specific Top+X processes individually targeted in each.

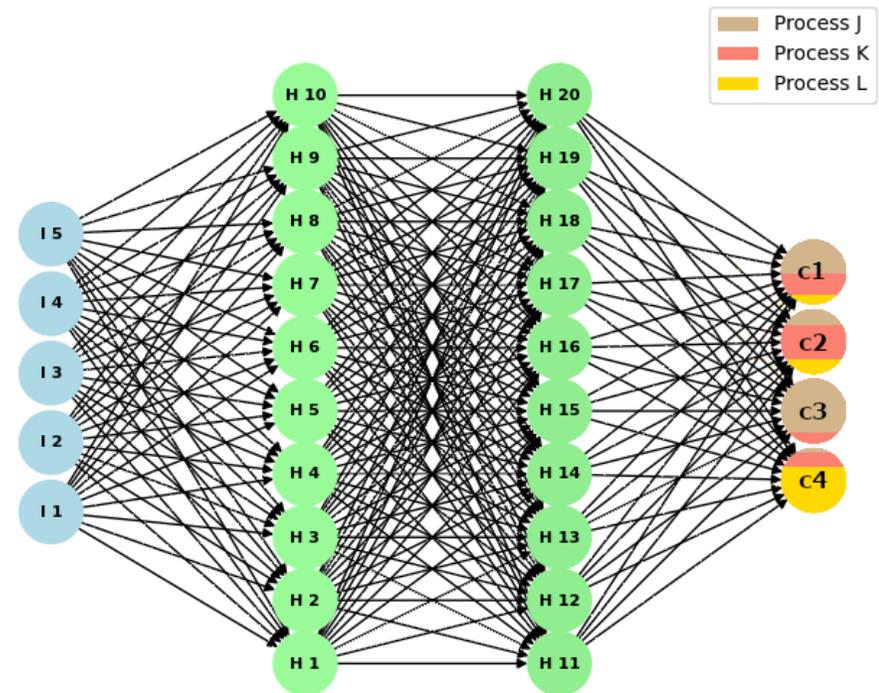
- Potential to re-use dedicated cross section analyses to minimise work duplication
- Object + Region harmonisation and fakes treatment all require careful consideration if starting from separate analyses
- Some processes 'easy' to distinguish - e.g. $t\bar{t}Z, tZq, t\bar{t}\gamma, t\bar{t}H$
- Other processes remain difficult to separate this way - e.g. $t\bar{t}W, t\bar{t}H, t\bar{t}t\bar{t}$
- Principal Component Analysis will identify sensitive directions
- **Need to be clear what you are optimising for!**



ATLAS Top+X Roadmap

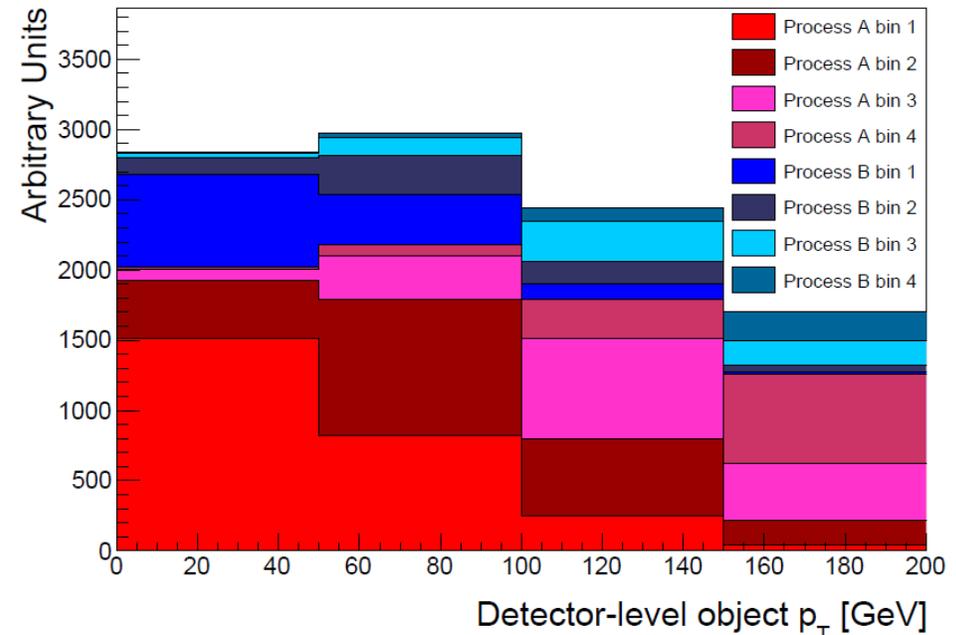
ATL-PHYS-PUB-2023-030

- 3. EFT-optimised (EO) fit:** The regions are defined by ML algorithms to select events with the highest sensitivity to particular EFT operators. [Lots of freedom here to define your targets, but lots of complications too].
- Object + region harmonisation are automatic
 - Fakes treatment is coherent
 - Higher dependency on EFT model
 - Is it easily reinterpretable? How about surrogate networks?
- This methodology may provide the opportunities to separate $t\bar{t}W$, $t\bar{t}H$, $t\bar{t}t\bar{t}$
 - (Or can determine whether it is even necessary)
 - Principal Component Analysis will identify sensitive directions
 - **Need to be clear what you are optimising for!**



4. Fully differential multi-process unfolding:

- An extension of **(1)** or **(2)** (or technically **(3)**, with adjustments)
 - Best reinterpretations and reusability
 - Unbiased unfolding retains reliable results even under updated SM or EFT predictions
 - Simple to compare to new theories
 - Profile-likelihood unfolding with multiple signals reduces assumptions about EFT contributions compared to methods subtracting fixed SM backgrounds
-
- Truth-level binning optimisation required for EFT sensitivity
 - Multi-signal unfolding is useful when dealing with largely inseparable processes



Summary

- Lepton and Flavour physics anomalies are persistent
- Top quarks are a fantastic tool to search for new physics
- Effective Field Theory is a highly active area of research for model-independent BSM searches
- Put it all together - maybe we'll get magic

Backup

LHC EFT WG <https://lpsc.web.cern.ch/lhc-eft-wg>

The [LHC EFT WG](https://lpsc.web.cern.ch/lhc-eft-wg)'s mandate is to provide a framework for the interpretation of LHC data in the context of effective field theories

- Study physics requirements needed to facilitate an interpretation commensurate with the available measurements, including Higgs bosons, top quarks, and electroweak bosons.
- Provide recommendations for the use of EFTs by the experiments to interpret their data
- Provide recommendations on theory setups and Monte Carlo simulations, as well as other tools.
- Provide a forum for theoretical discussions of EFT issues, such as constraints, higher-order corrections, and BSM interpretations.
- Discuss common uncertainties and combination procedures.
- Coordinate between the existing experimental WGs, to allow global EFT analyses inside and outside of experimental collaborations.

Conveners:

ATLAS:

- Sarah Heim (Higgs WG contact)
- Jacob Kempster (Top WG contact)
- Karolos Potamianos (EW WG contact)
- Sandra Kortner

CMS:

- Matteo Presilla (EW WG contact)
- Nadjieh Jafari
- Robert Schoefbeck (Top WG contact)
- Nicholas Wardle (Higgs WG contact)

LHCb:

- Greg Ciezarek and Christoph Langenbruch

Theory:

- Ilaria Brivio
- Anke Biekötter (Higgs WG contact)
- Shankha Banerjee (EW WG contact)
- Gauthier Durieux
- Ken Mimasu (Top WG contact)
- Peter Stangl

LHC EFT WG

TWiki:

<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/LHCEFT>

Indico: <https://indico.cern.ch/category/12374/>

Documents: [CDS](#)

7th General Meeting of the LHC EFT
Working Group

<https://indico.cern.ch/event/1384135>

(Recordings available)

Area 1: [EFT Formalism](#) - Higher-order corrections in SMEFT, Positivity Constraints, SMEFT vs HEFT

Area 2: [Predictions and Tools](#) - Common toolchain for SMEFT parameterisations, Common methodology for EFT MC production (reweighting vs direct) - PUB note under [development](#)

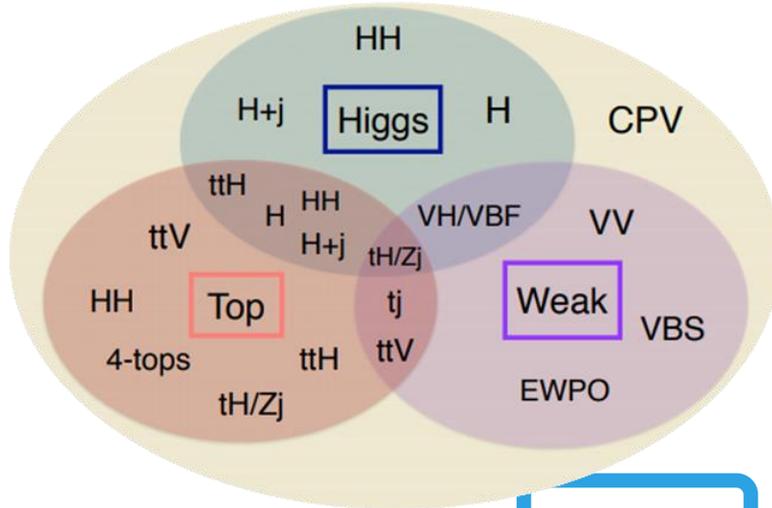
Area 3: [Measurements and Observables](#) - Optimal observables, complementarities, Machine learning opportunities (and challenges) for EFTs - [dedicated discussion](#), Reinterpretability

Area 4: [Fits and Related Systematics](#) - "Fitting exercise" (for study only!)

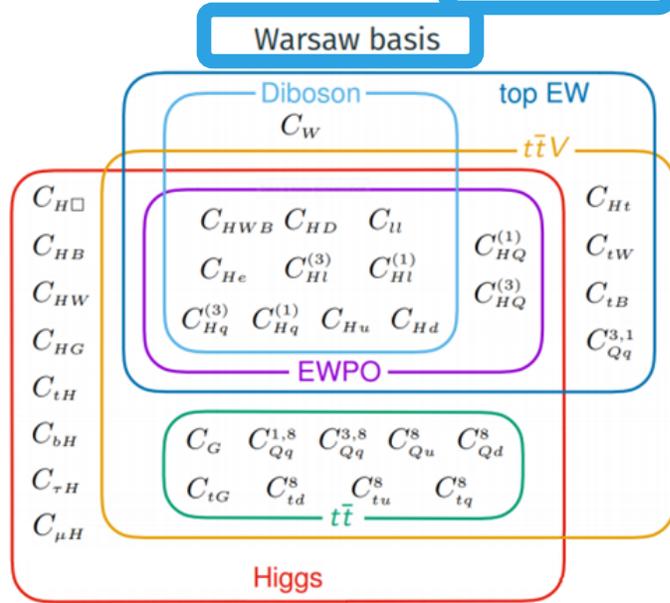
Area 5: [Benchmark Scenarios from UV Models](#) - Mapping BSM to SMEFT (database, framework)

Area 6: [Flavour](#) - Connecting flavour physics (and anomalies) to global EFT fits

Top EFT



Adapted from K. Mimasu



J. Ellis et al, JHEP 04 (2021) 279

Grzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

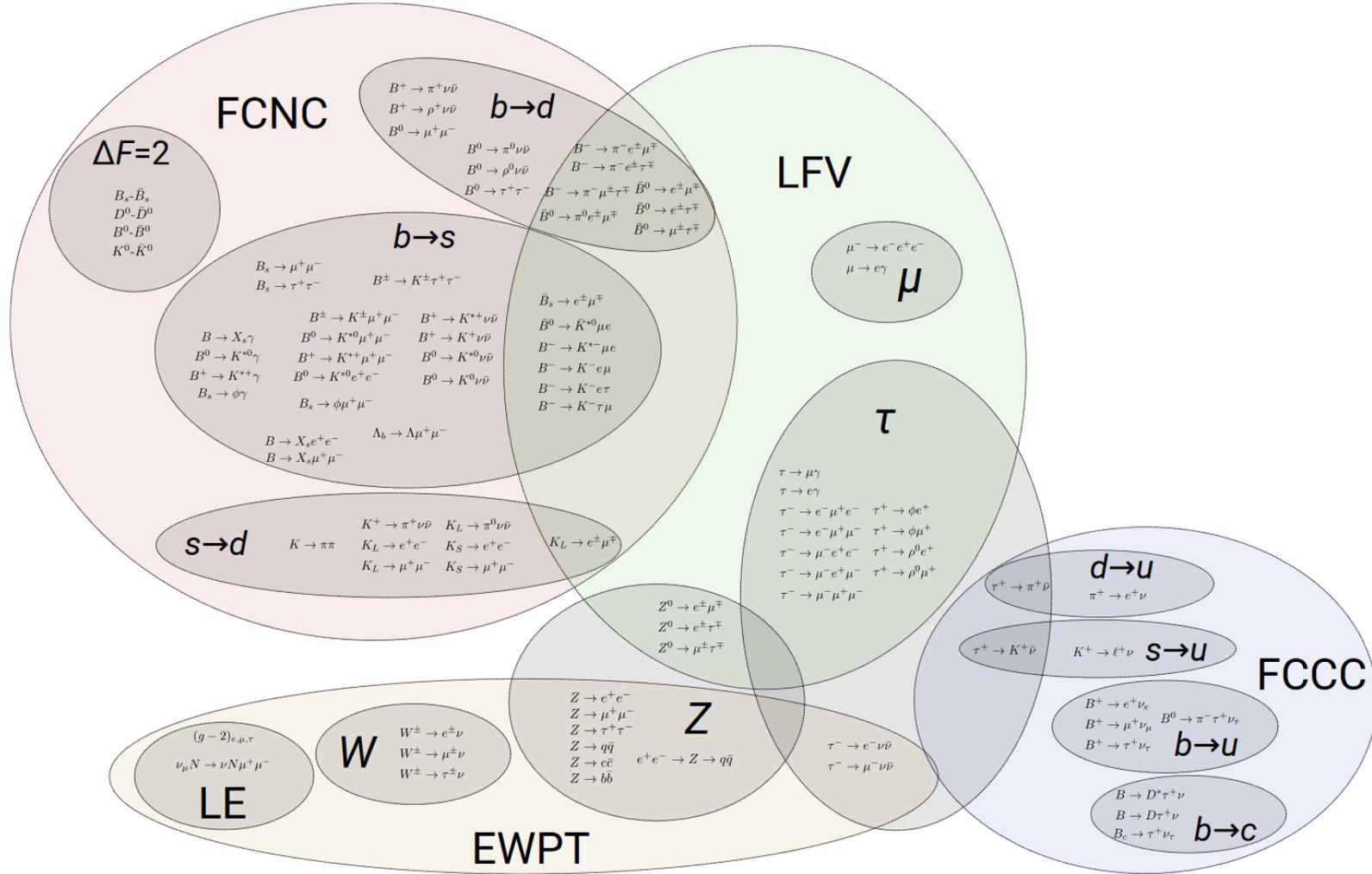
	X^3	φ^6 and $\varphi^4 D^2$	$\psi^2 \varphi^3$		
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \varphi)$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				

	$X^2 \varphi^2$	$\psi^2 X \varphi$	$\psi^2 \varphi^2 D$		
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{WB}}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

Grzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

	$(\bar{L}L)(\bar{L}L)$	$(\bar{R}R)(\bar{R}R)$	$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$

	$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$	B-violating	
Q_{ledq}	$(\bar{l}_p e_r)(\bar{d}_s q_t^c)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{quu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^\alpha)^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	Q_{quq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mnn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$
$Q_{lequ}^{(1)}$	$(\bar{l}_p e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$
$Q_{lequ}^{(3)}$	$(\bar{l}_p \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$		

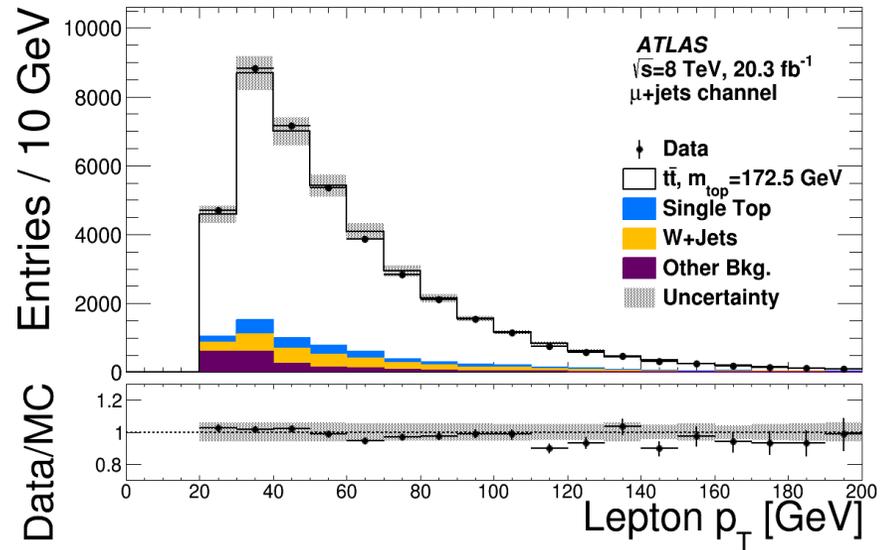


D. Straub

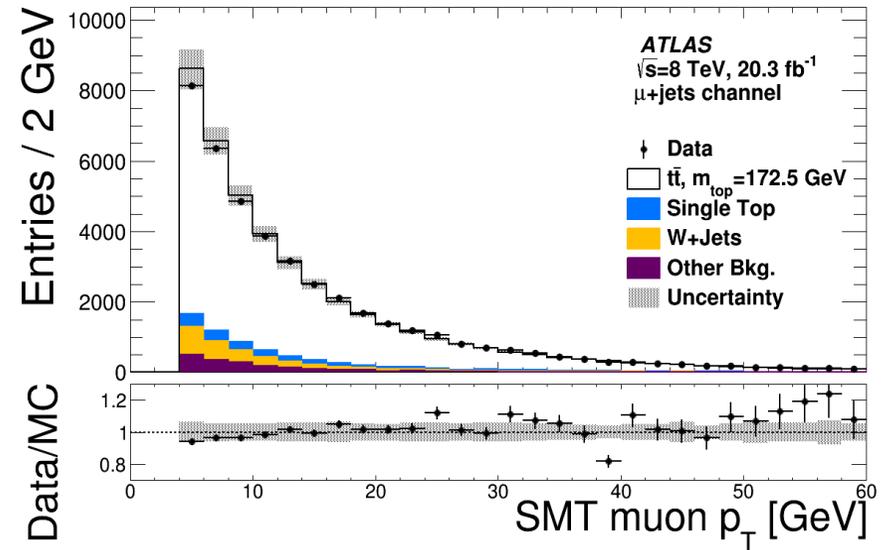
EPJC 79 (2019) 505



“Soft” muon



↓
“Hard-lepton”
“W-lepton”



↓
“Soft Muon”

- **Opposite Sign (OS)**
 - $t \rightarrow l^+ \nu b \rightarrow l^+ l^- X \sim 55\%$
 - $t \rightarrow l^+ \nu (b \rightarrow \bar{b} \rightarrow \bar{c}) \rightarrow l^+ l^- X \sim 4\%$
 - $t \rightarrow l^+ \nu (b \rightarrow c \bar{c}) \rightarrow l^+ l^- X \sim 3\%$
- **Same Sign (SS)**
 - $t \rightarrow l^+ \nu (b \rightarrow \bar{b}) \rightarrow l^+ l^+ X \sim 7\%$
 - $t \rightarrow l^+ \nu (b \rightarrow c) \rightarrow l^+ l^+ X \sim 28\%$
 - $t \rightarrow l^+ \nu (b \rightarrow \bar{b} \rightarrow c \bar{c}) \rightarrow l^+ l^+ X \sim 3\%$

Comparing these processes with their charge conjugates allows for building of inclusive asymmetries sensitive to CP violation:

- Consider number of SMT muons, $N^{\alpha\beta}$, where:

$$P(b \rightarrow l^-) = \frac{N(b \rightarrow l^-)}{N(b \rightarrow l^-) + N(b \rightarrow l^+)} = \frac{N^{+-}}{N^{+-} + N^{++}} = \frac{N^{+-}}{N^+}$$

$$P(\bar{b} \rightarrow l^+) = \frac{N(\bar{b} \rightarrow l^+)}{N(\bar{b} \rightarrow l^-) + N(\bar{b} \rightarrow l^+)} = \frac{N^{-+}}{N^{--} + N^{-+}} = \frac{N^{-+}}{N^-}$$

$$P(b \rightarrow l^+) = \frac{N(b \rightarrow l^+)}{N(b \rightarrow l^-) + N(b \rightarrow l^+)} = \frac{N^{++}}{N^{+-} + N^{++}} = \frac{N^{++}}{N^+}$$

$$P(\bar{b} \rightarrow l^-) = \frac{N(\bar{b} \rightarrow l^-)}{N(\bar{b} \rightarrow l^-) + N(\bar{b} \rightarrow l^+)} = \frac{N^{--}}{N^{--} + N^{-+}} = \frac{N^{--}}{N^-}$$

Decay chain fractions (Obtained from simulation)

Same Sign

$$N_{r_b} = N [t \rightarrow \ell^+ \nu (b \rightarrow \bar{b}) \rightarrow \ell^+ \ell^+ X],$$

$$N_{r_c} = N [t \rightarrow \ell^+ \nu (b \rightarrow c) \rightarrow \ell^+ \ell^+ X],$$

$$N_{r_{c\bar{c}}} = N [t \rightarrow \ell^+ \nu (b \rightarrow \bar{b} \rightarrow c\bar{c}) \rightarrow \ell^+ \ell^+ X],$$

$$r_b = \frac{N_{r_b}}{N_{r_b} + N_{r_c} + N_{r_{c\bar{c}}}},$$

$$r_c = \frac{N_{r_c}}{N_{r_b} + N_{r_c} + N_{r_{c\bar{c}}}},$$

$$r_{c\bar{c}} = \frac{N_{r_{c\bar{c}}}}{N_{r_b} + N_{r_c} + N_{r_{c\bar{c}}}},$$

Opposite Sign

$$N_{\tilde{r}_b} = N [t \rightarrow \ell^+ \nu b \rightarrow \ell^+ \ell^- X],$$

$$N_{\tilde{r}_c} = N [t \rightarrow \ell^+ \nu (b \rightarrow \bar{b} \rightarrow \bar{c}) \rightarrow \ell^+ \ell^- X],$$

$$N_{\tilde{r}_{c\bar{c}}} = N [t \rightarrow \ell^+ \nu (b \rightarrow c\bar{c}) \rightarrow \ell^+ \ell^- X].$$

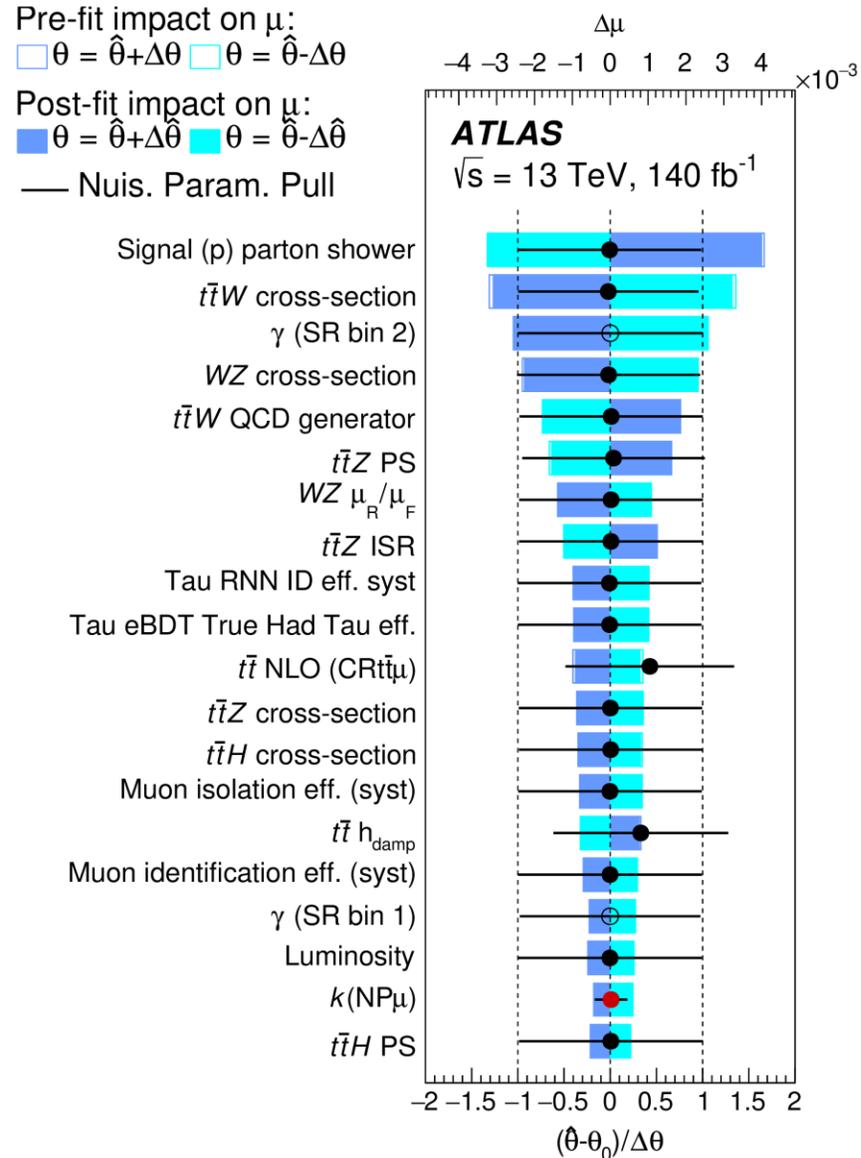
$$\tilde{r}_b = \frac{\tilde{N}_{r_b}}{\tilde{N}_{r_b} + \tilde{N}_{r_c} + \tilde{N}_{r_{c\bar{c}}}},$$

$$\tilde{r}_c = \frac{\tilde{N}_{r_c}}{\tilde{N}_{r_b} + \tilde{N}_{r_c} + \tilde{N}_{r_{c\bar{c}}}},$$

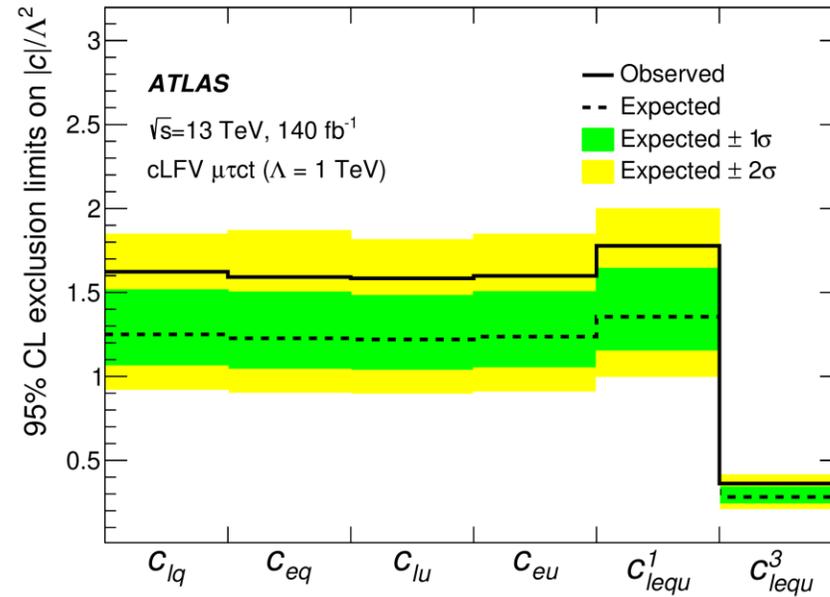
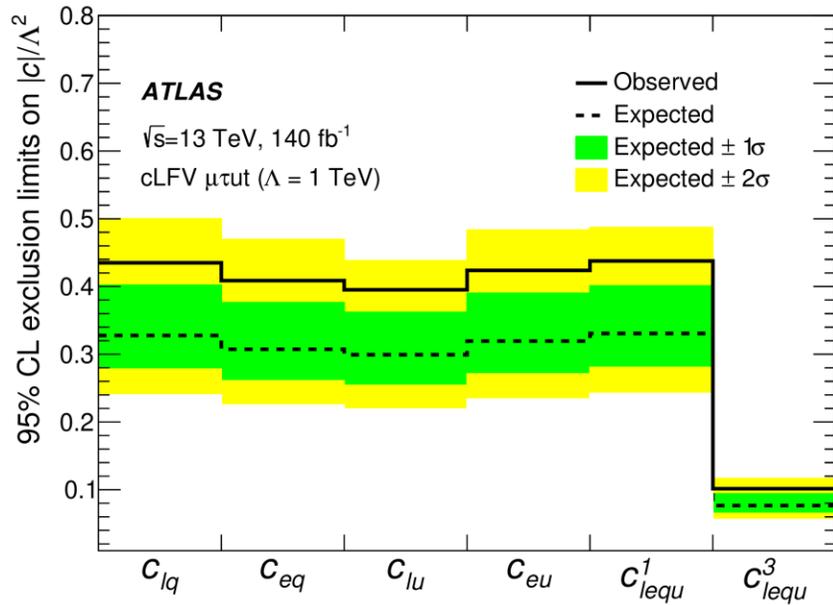
$$\tilde{r}_{c\bar{c}} = \frac{\tilde{N}_{r_{c\bar{c}}}}{\tilde{N}_{r_b} + \tilde{N}_{r_c} + \tilde{N}_{r_{c\bar{c}}}}.$$

(Best measured in a well-defined fiducial volume)

CLFV EFT Result breakdown

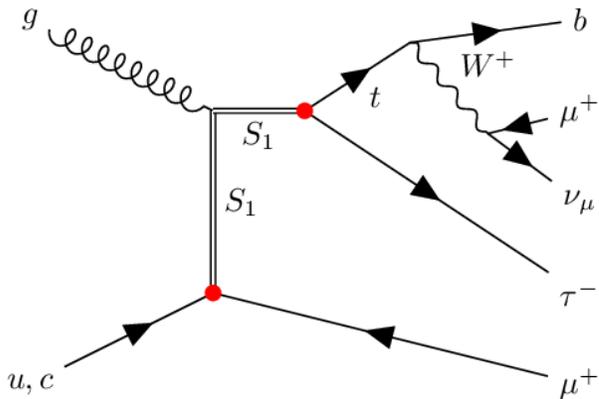
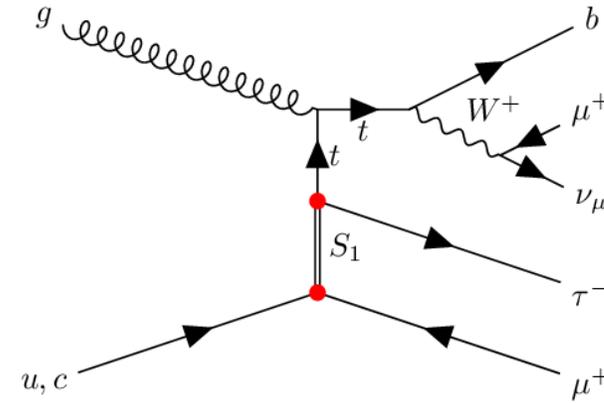
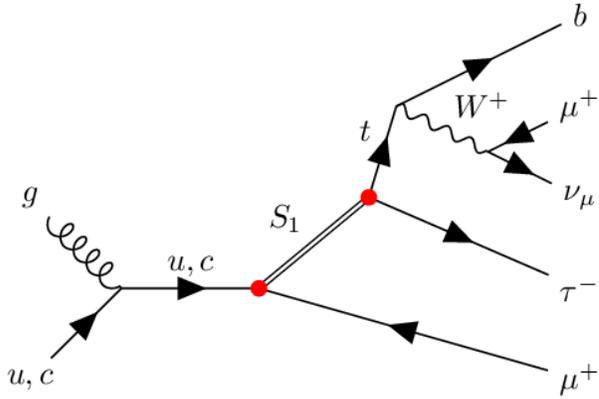


CLFV EFT Result breakdown



CLFV - Leptoquark interpretation

Scalar leptoquark with cross-generational couplings could produce CLFV processes.



$$\lambda_{ki} \in \begin{pmatrix} \lambda_{t\tau} & \lambda_{c\tau} & \lambda_{u\tau} \\ \lambda_{t\mu} & \lambda_{c\mu} & \lambda_{u\mu} \\ \lambda_{te} & \lambda_{ce} & \lambda_{ue} \end{pmatrix} \equiv \lambda^{\text{LQ}} \begin{pmatrix} 10 & 1 & 0.1 \\ 1 & 0.1 & 0.01 \\ 0.1 & 0.01 & 0.001 \end{pmatrix}$$



CLFV - Leptoquark interpretation

Cross-generational couplings introduce many degrees of freedom, which may be simplified with a hierarchical model:

$$\lambda_{ki} \in \begin{pmatrix} \lambda_{t\tau} & \lambda_{c\tau} & \lambda_{u\tau} \\ \lambda_{t\mu} & \lambda_{c\mu} & \lambda_{u\mu} \\ \lambda_{te} & \lambda_{ce} & \lambda_{ue} \end{pmatrix} \equiv \lambda^{\text{LQ}} \begin{pmatrix} 10 & 1 & 0.1 \\ 1 & 0.1 & 0.01 \\ 0.1 & 0.01 & 0.001 \end{pmatrix}$$

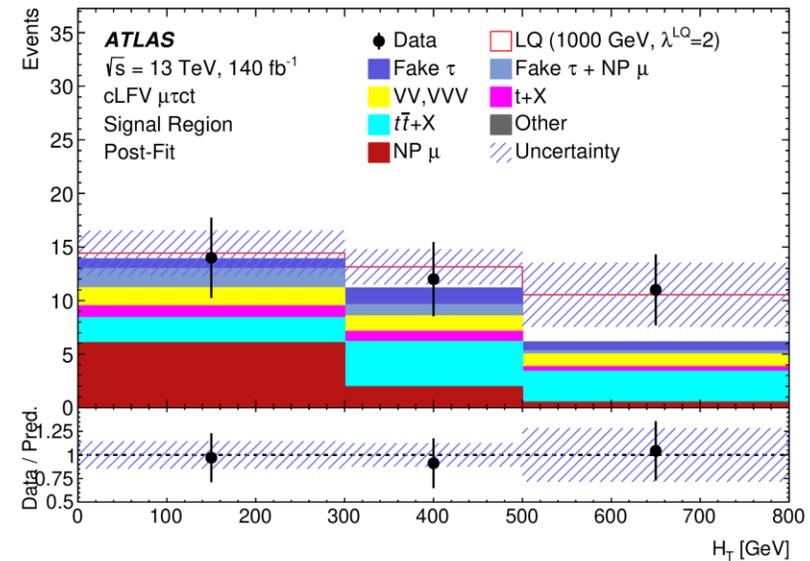
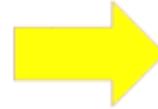
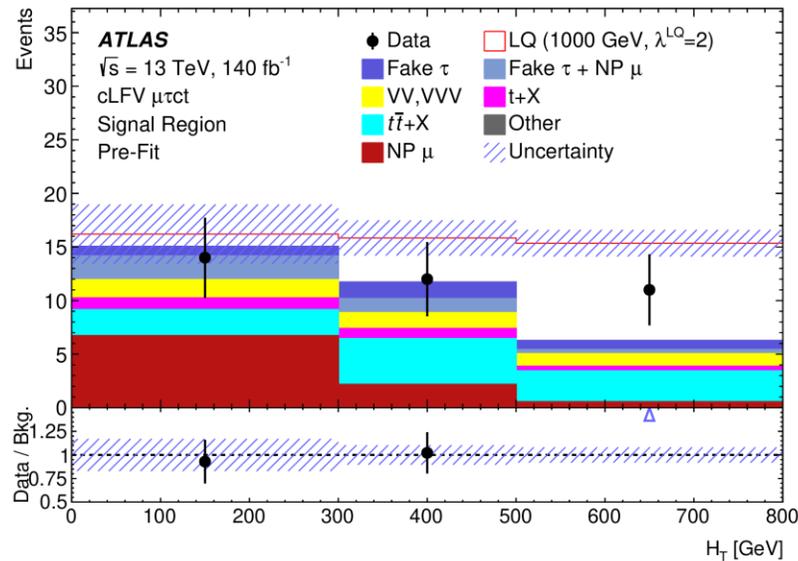
This reduces 10 degrees of freedom (9 coupling, 1 mass) into 2 (1 coupling, 1 mass).

Various theory papers apply hierarchical coupling models, with different magnitudes spanning steps of $\sqrt{2}$ to $\frac{1}{16}$ [1,2,3,4,5]

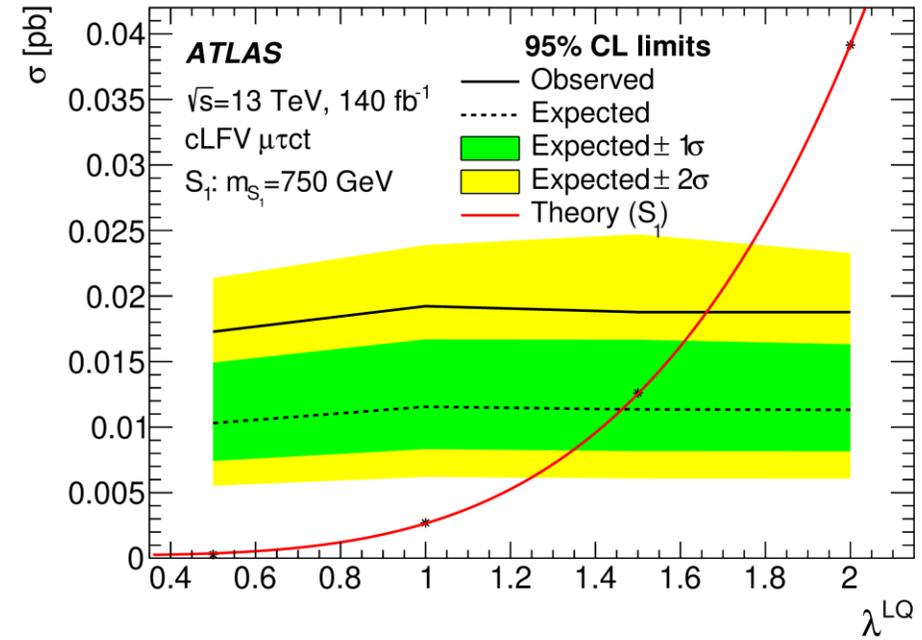
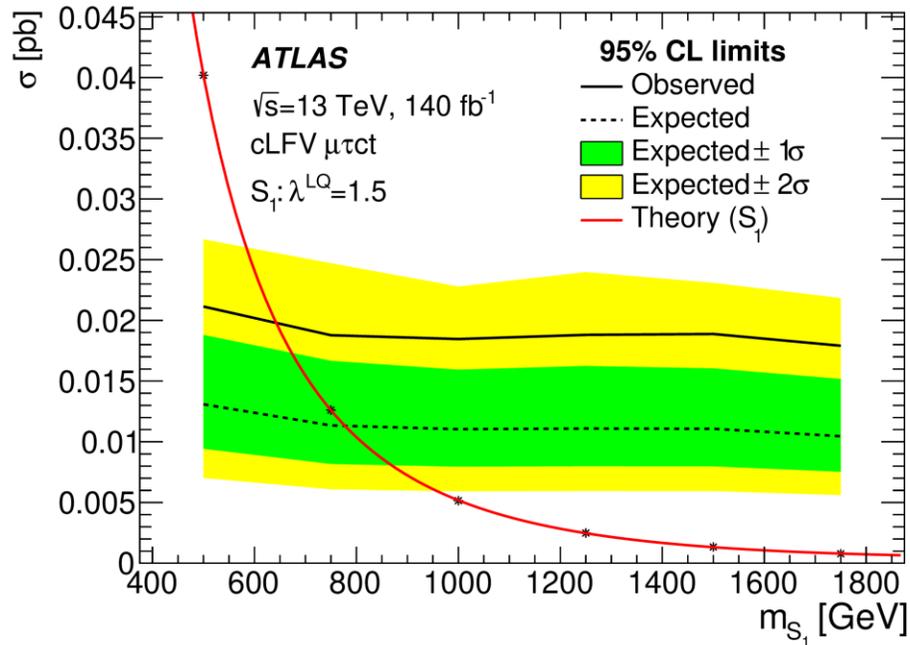


CLFV - Leptoquark interpretation

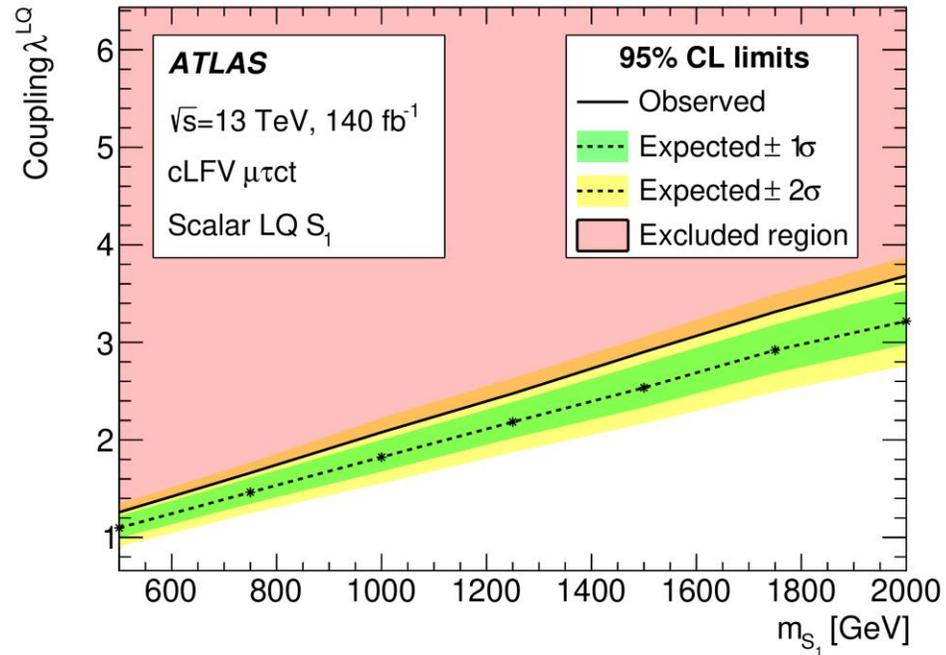
Analysis is not re-optimised for LQ signal, but HT is already a very good discriminating variable. Signals $0.5 < m_{LQ} < 2.5$ TeV, and $0.5 < \lambda^{LQ} < 3.5$ are fit independently:



CLFV - Leptoquark interpretation



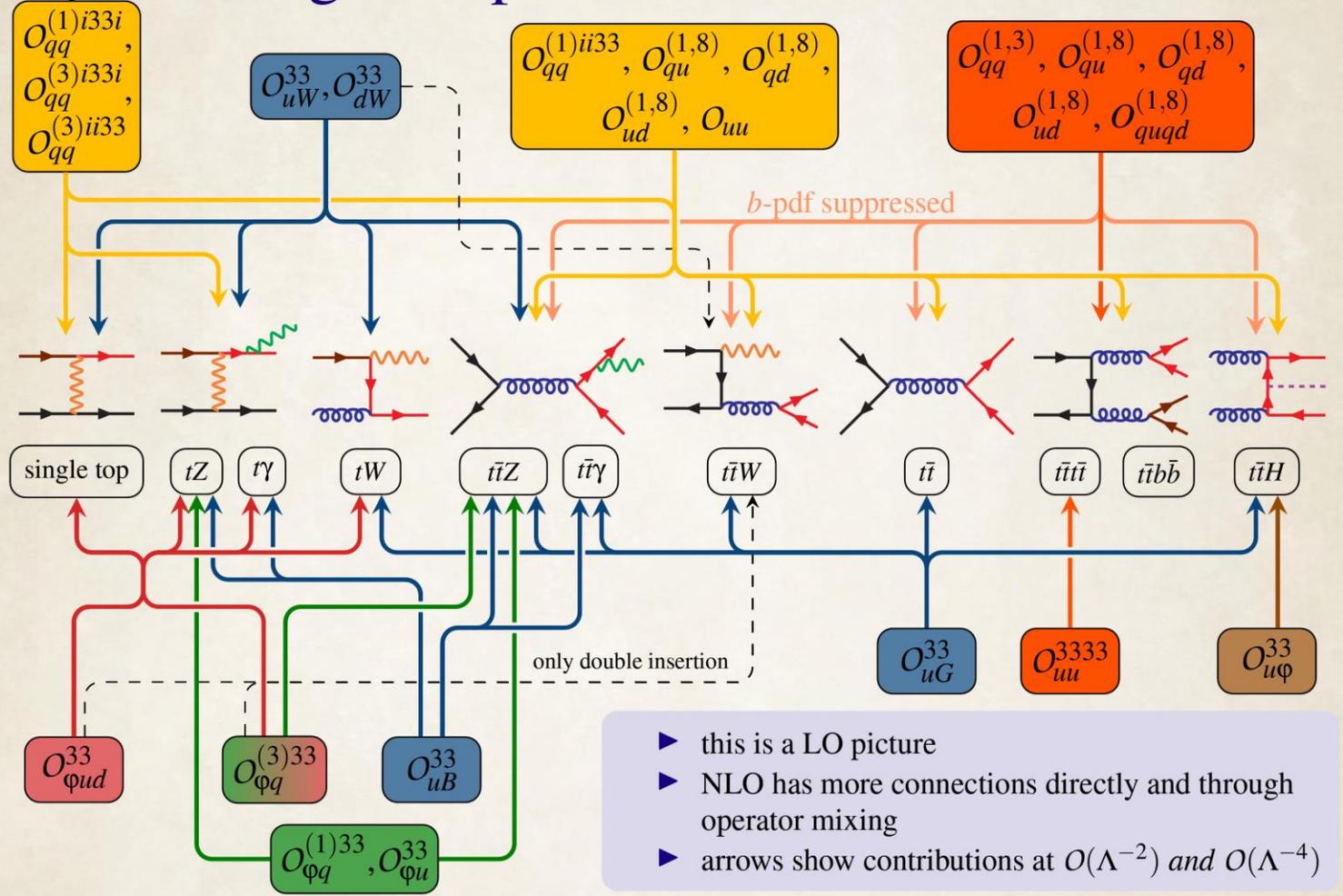
CLFV - Leptoquark interpretation



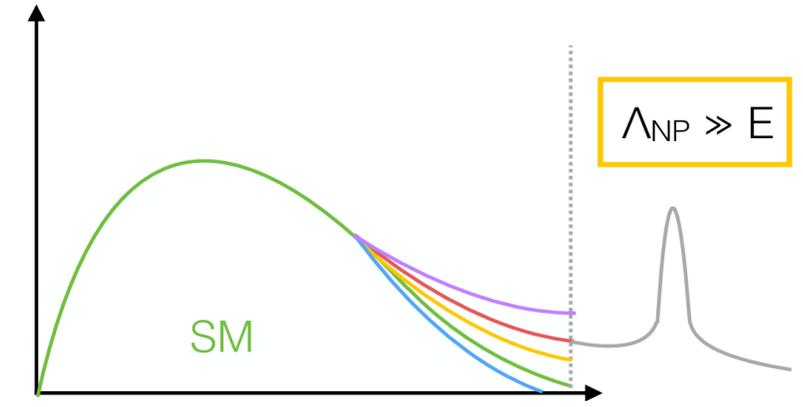
m_{S_1} [GeV]	Limit on λ^{LQ} (95% CL)	
	Observed	Expected
500	1.3	1.1
750	1.7	1.5
1000	2.1	1.8
1250	2.5	2.2
1500	2.9	2.5
1750	3.3	2.9
2000	3.7	3.2



Top EFT: a global picture



- ▶ this is a LO picture
- ▶ NLO has more connections directly and through operator mixing
- ▶ arrows show contributions at $O(\Lambda^{-2})$ and $O(\Lambda^{-4})$



parameter	$t\bar{t}$	single t	tW	tZ	t decay	$t\bar{t}Z$	$t\bar{t}W$
$C_{Qq}^{1,8}$	Λ^{-2}	-	-	-	-	Λ^{-2}	Λ^{-2}
$C_{Qq}^{3,8}$	Λ^{-2}	$\Lambda^{-4} [\Lambda^{-2}]$	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$	Λ^{-2}	Λ^{-2}
C_{tu}^8, C_{td}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	-
$C_{Qq}^{1,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{Qq}^{3,1}$	$\Lambda^{-4} [\Lambda^{-2}]$	Λ^{-2}	-	Λ^{-2}	Λ^{-2}	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
C_{tu}^1, C_{td}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	-
C_{Qu}^8, C_{Qd}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	-
C_{tq}^8	Λ^{-2}	-	-	-	-	Λ^{-2}	Λ^{-2}
C_{Qu}^1, C_{Qd}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	-
C_{tq}^1	$\Lambda^{-4} [\Lambda^{-2}]$	-	-	-	-	$\Lambda^{-4} [\Lambda^{-2}]$	$\Lambda^{-4} [\Lambda^{-2}]$
$C_{\phi Q}^-$	-	-	-	Λ^{-2}	-	Λ^{-2}	-
$C_{\phi Q}^3$	-	Λ^{-2}	Λ^{-2}	Λ^{-2}	Λ^{-2}	-	-
$C_{\phi t}$	-	-	-	Λ^{-2}	-	Λ^{-2}	-
$C_{\phi tb}$	-	Λ^{-4}	Λ^{-4}	Λ^{-4}	Λ^{-4}	-	-
C_{tZ}	-	-	-	Λ^{-2}	-	Λ^{-2}	-
C_{tW}	-	Λ^{-2}	Λ^{-2}	Λ^{-2}	Λ^{-2}	-	-
C_{bW}	-	Λ^{-4}	Λ^{-4}	Λ^{-4}	Λ^{-4}	-	-
C_{tG}	Λ^{-2}	$[\Lambda^{-2}]$	Λ^{-2}	-	$[\Lambda^{-2}]$	Λ^{-2}	Λ^{-2}