

Towards search for $100\ \mu\text{eV}$ axions and axion dark matter with high-frequency microwaves

Akira Miyazaki

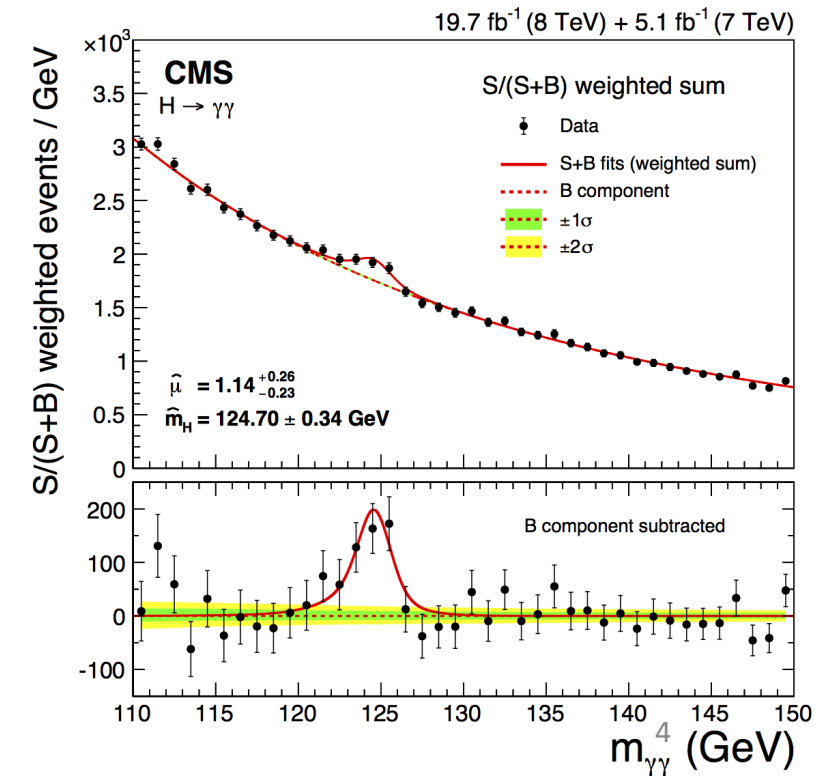
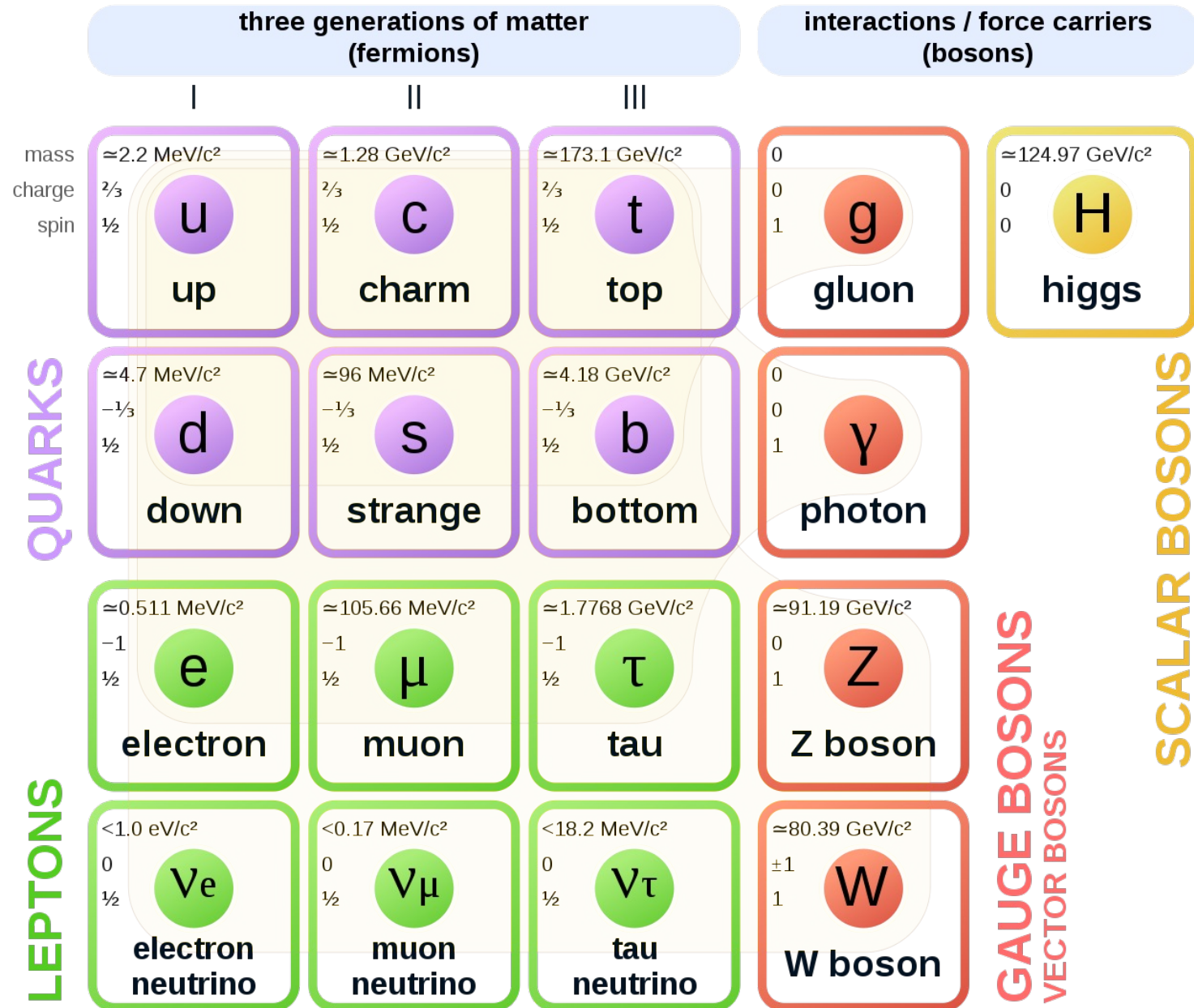
Outline

- Introduction
 - New physics with microwaves
 - Axion and axion dark matter
 - Particle vs wave
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 - ADMX experiment
 - Background noise and quantum limit
 - Squeezing (HAYSTAC) and photon counting
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 - MADMAX: signal boost with dielectric disks
 - ALPHA: plasma haloscope with wire metamaterial
- Conclusion

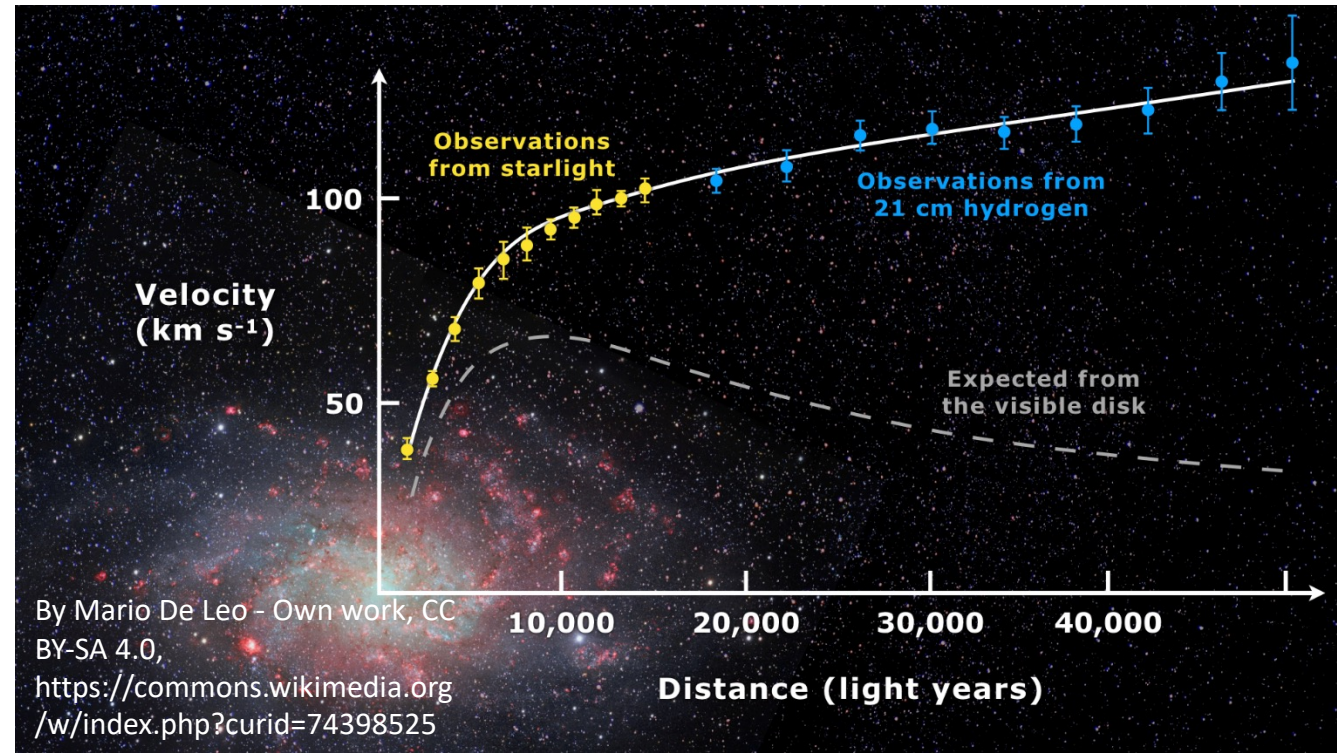
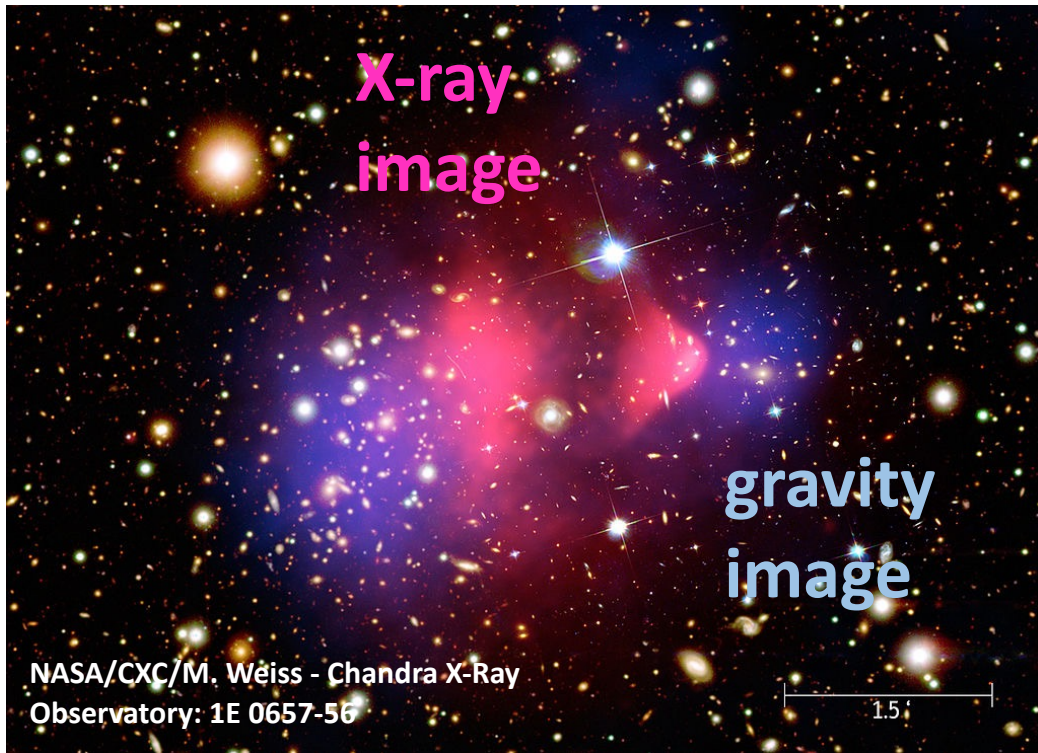
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Standard Model of Elementary Particles



Clear need for new physics: e.g. Dark Matter (DM)



~~Neutrino?~~

~~Dark astrophysical objects?~~

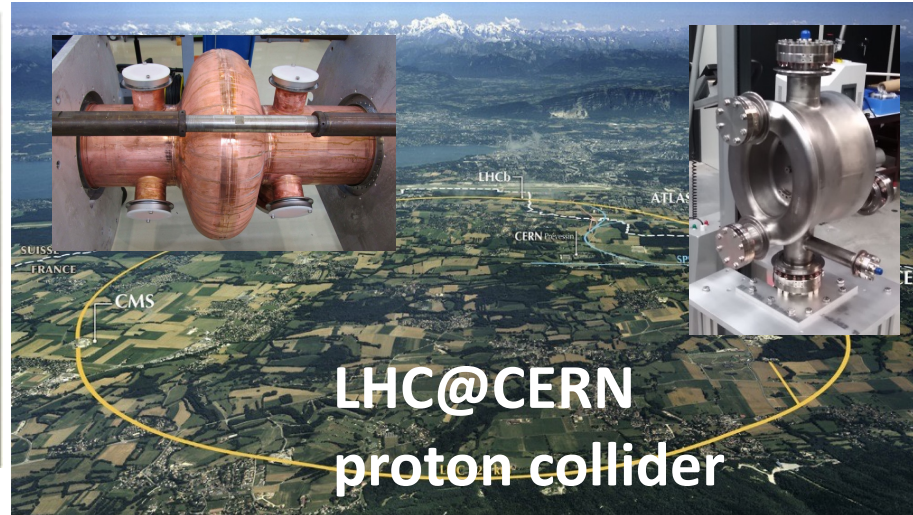
~~Modified gravity?~~ van Dokkum, et al. *Nature* **555**, 629–632 (2018)

Primordial black holes?

✓ Hypothetical new particles linked to intrinsic issues in the Standard Model?

My main business: Radio Frequency cavities for accelerators

HIE-ISOLDE@CERN
Heavy ion



ESS@Lund
Proton Linac for neutrons



PIP-II@FNL
proton driver for neutrino



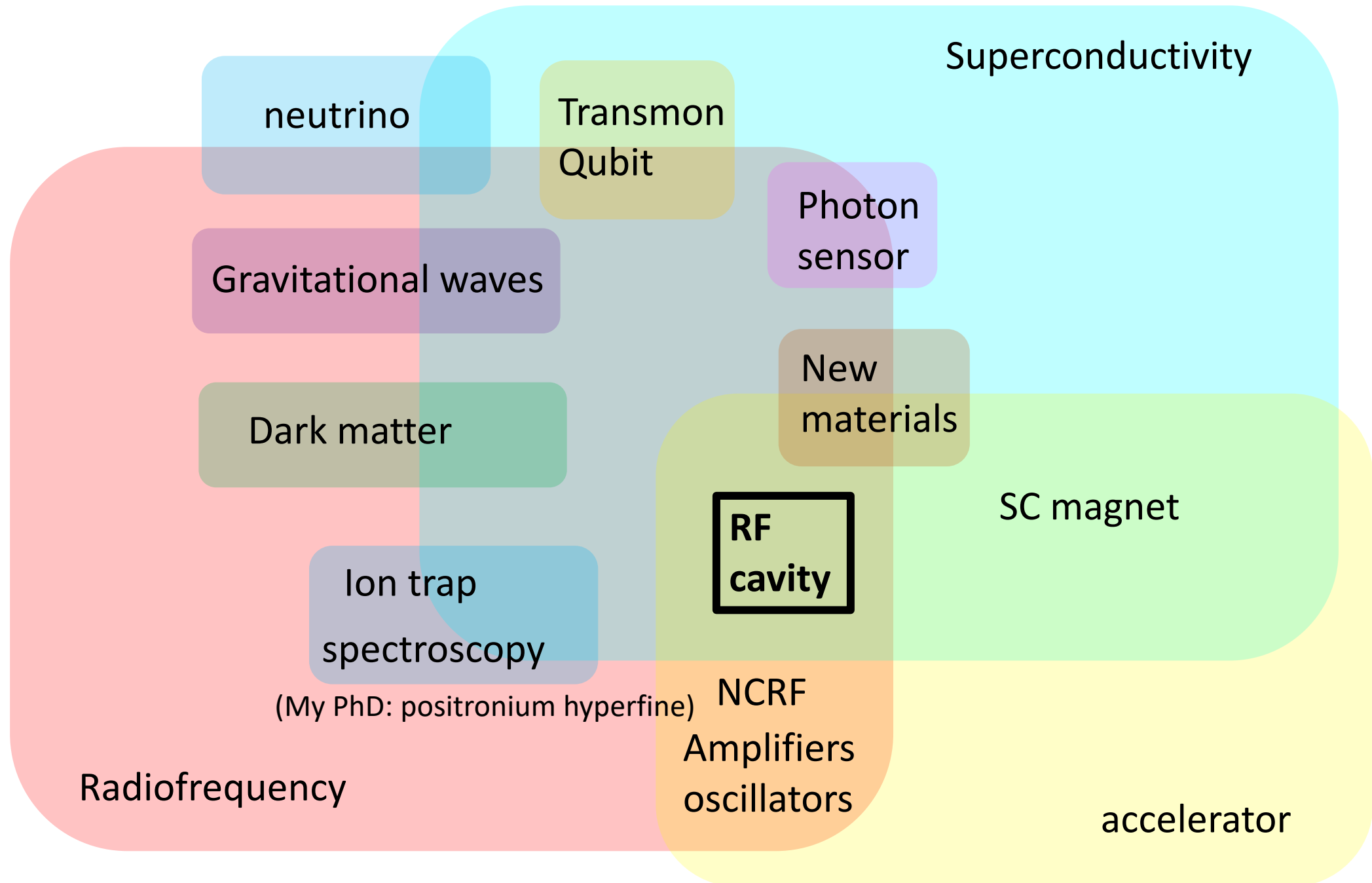
ILC Higgs Factory



Pros: any present and future accelerators would include superconducting RF cavities

Cons: Timeline (decades?) costs (>>BEUR?) still no promise for *new physics*

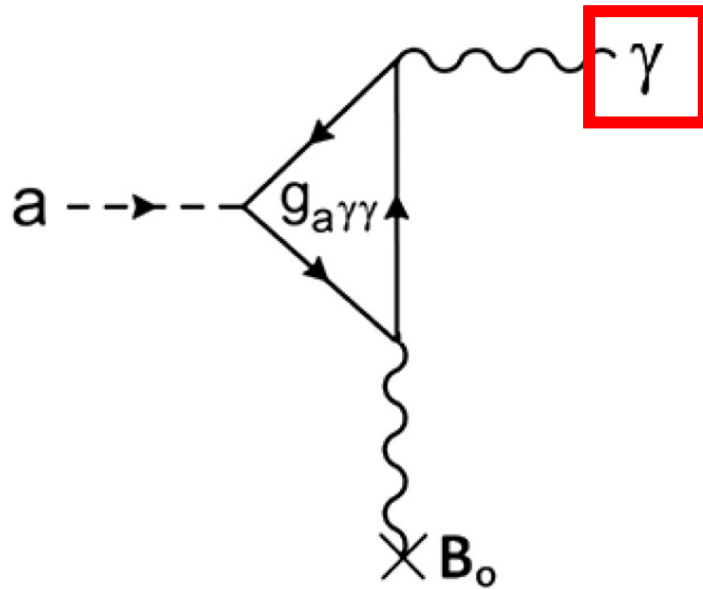
→ Can't we directly make use of RF for discovery?



Microwave photons may address fundamental physics

Today's
talk

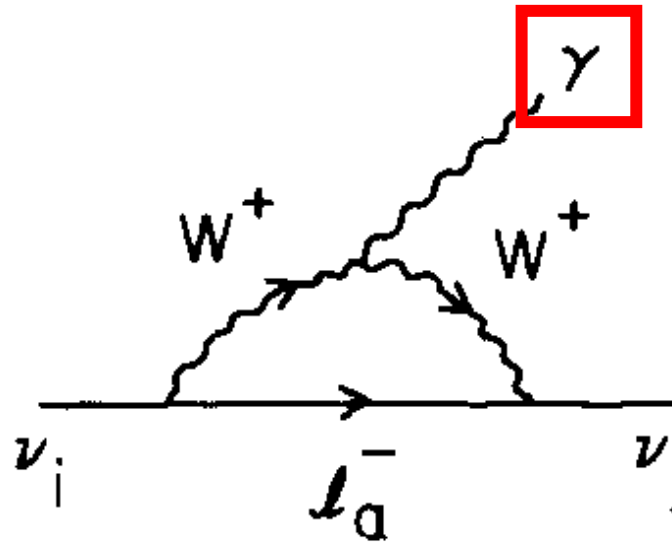
Axions



Inverse Primakoff effect

Minimal extension of SM

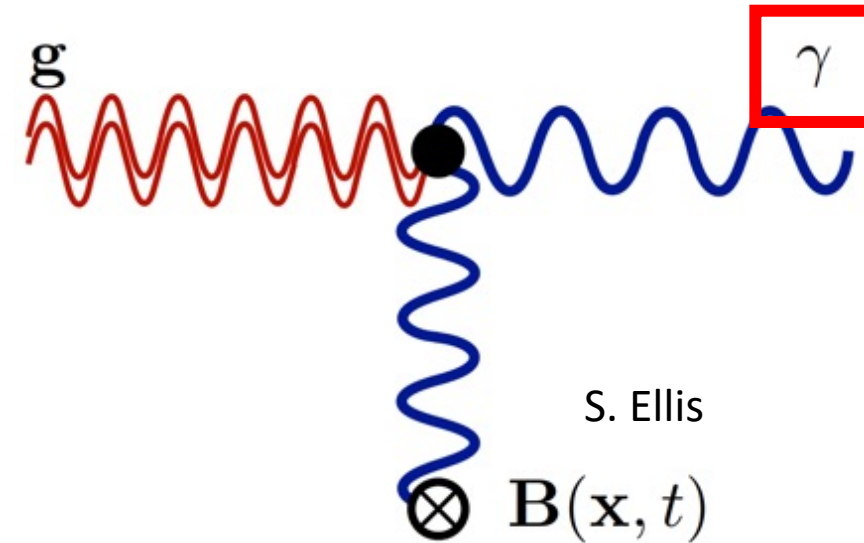
Neutrinos



Cosmic neutrino background

Extension of SM and/or SM

Gravitational waves



Inverse Gertsenshtein effect

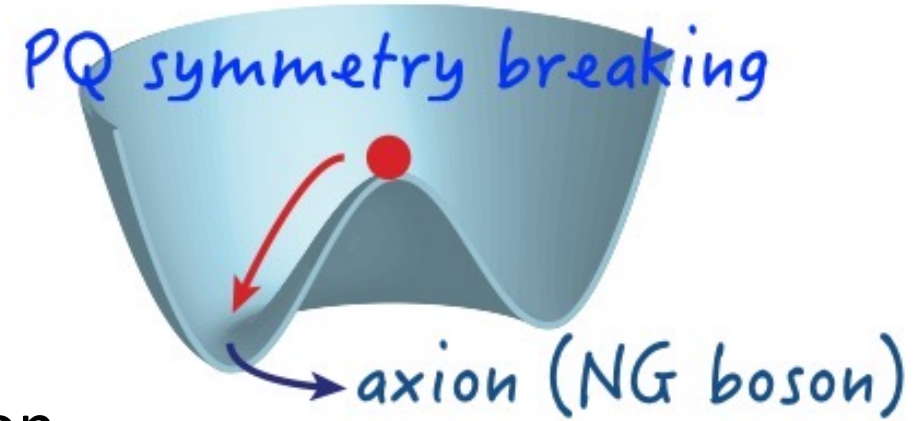
Solution of general relativity

Axions: a byproduct to cancel the strong CP

Quantum Chromodynamics (theory of strong force)

$$L_{QCD} \supset -\frac{1}{4} G_{\mu\nu}^a G^{\mu\nu a} + \frac{g_s^2}{32\pi^2} \theta G_{\mu\nu}^a \tilde{G}^{\mu\nu a}$$

gluons



This term generates electric dipole moment in neutron

- Theory: $d_n \sim 4.5 \times 10^{-15} \theta$ ecm
- Experiment: $|d_n| < 2.9 \times 10^{-29}$ ecm

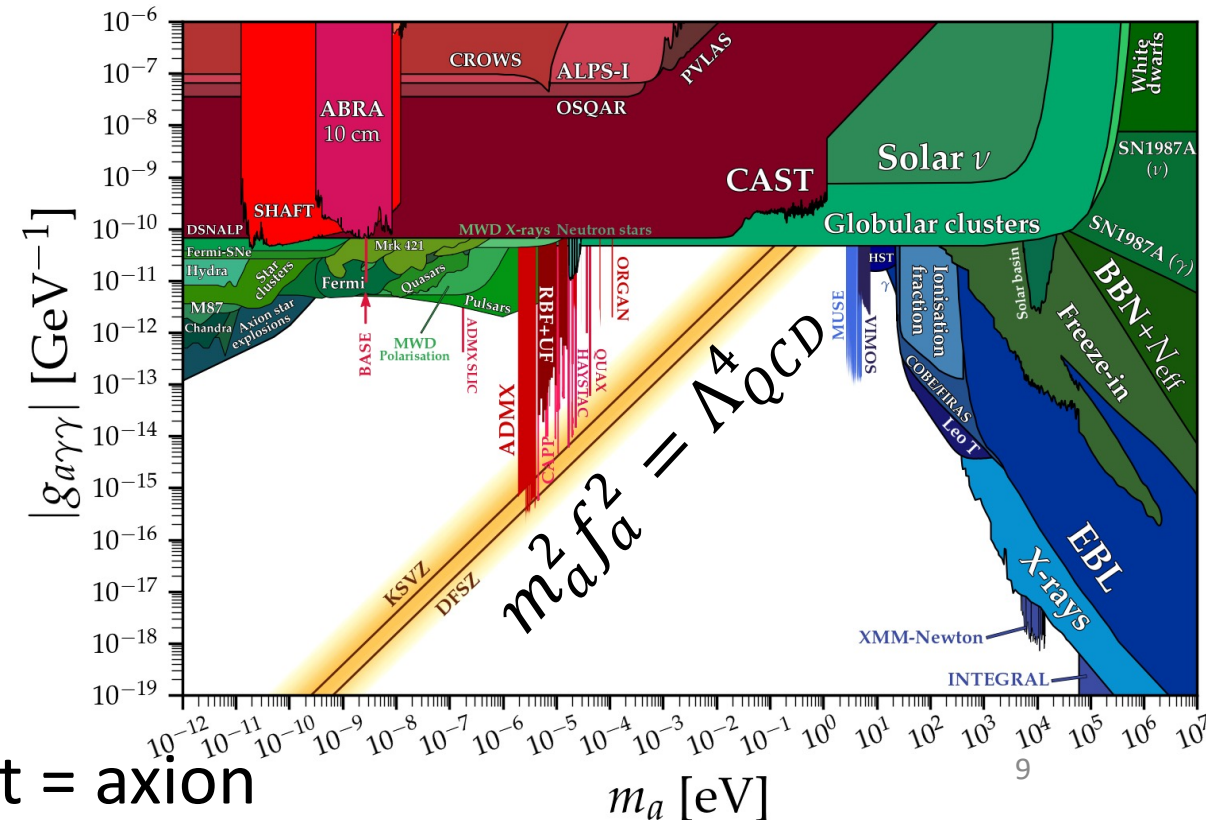
$$\Rightarrow |\theta| < 0.7 \times 10^{-11} \ll 1$$

Naturalness without anthropic solution

Introduce a new global chiral U(1) field a

$$\frac{g_s^2}{32\pi^2} \left(\theta + \frac{a}{F_a} \right) G_{\mu\nu}^a \tilde{G}^{\mu\nu a} \rightarrow 0 \text{ (after SSB)}$$

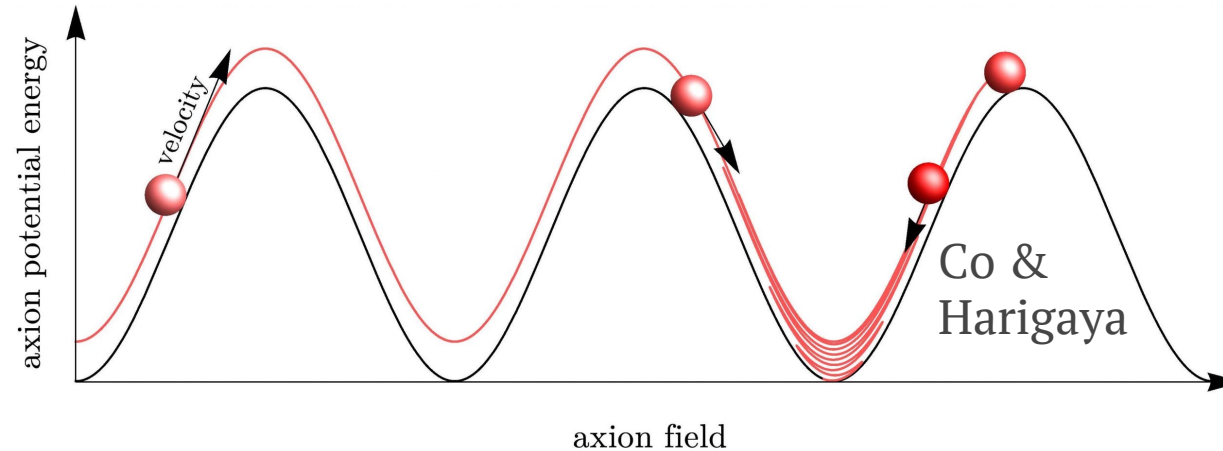
SSB \rightarrow A pNG boson appears as a byproduct = axion



Axion as dark matter

Axion loses kinetic energy ***non-thermally*** by coherent oscillation in the PQ potential

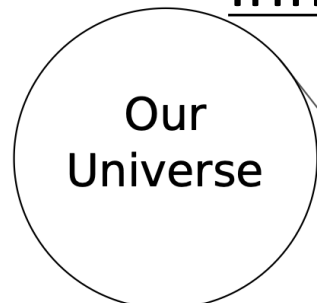
Misalignment
mechanism



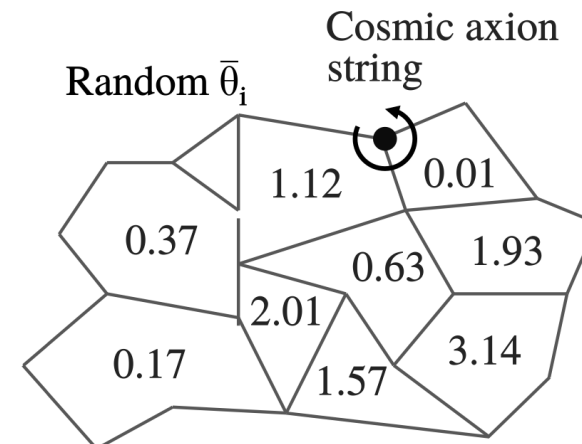
Two possible
scenarios
related to the
energy scale of
inflation

Inflation < PQ

Inflation > PQ



Our Universe:



Remaining coherent
oscillation = DM

Naturalness problem
in DM abundance
(initial value dependence)

Annihilating axion
string = DM

Natural solution to
DM abundance

Stefan Knirck PhD thesis

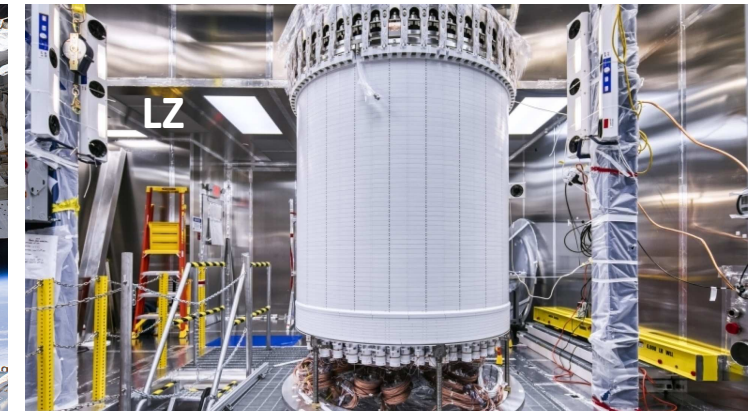
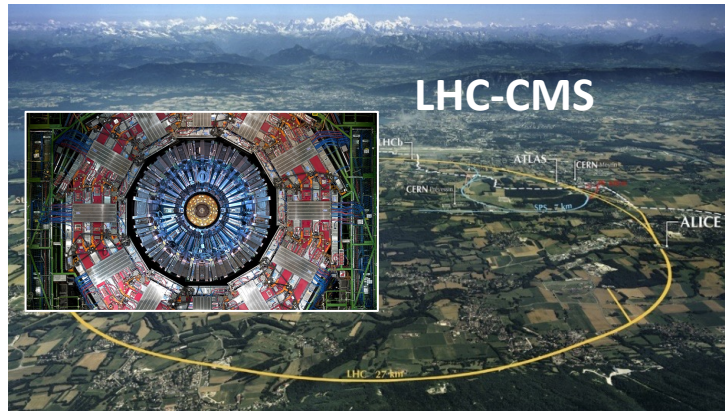
Three ways to study dark matter candidates

Production in lab

Signal from astrophysics

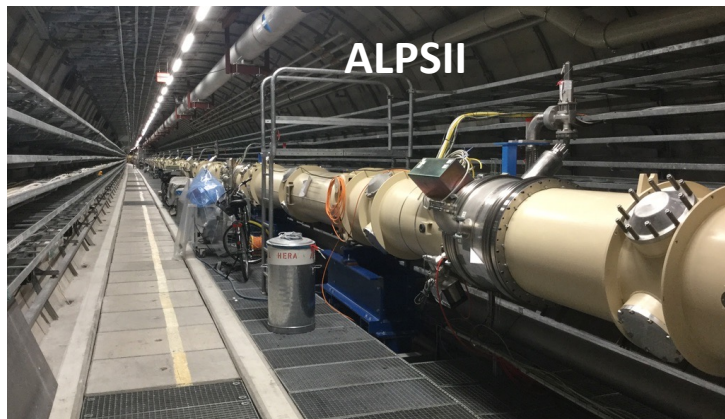
DM from galaxy halo

WIMP
SUSY



→ Common techniques: **particle** detection, reconstruction, PID, etc

WISP
axions



full knowledge in source

uncertainty in astrophysical models

Uncertainty in cosmological models

→ Common techniques: magnets & **photon science**

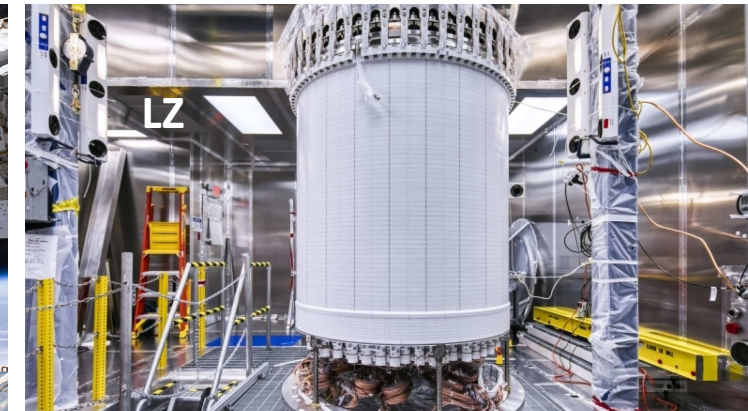
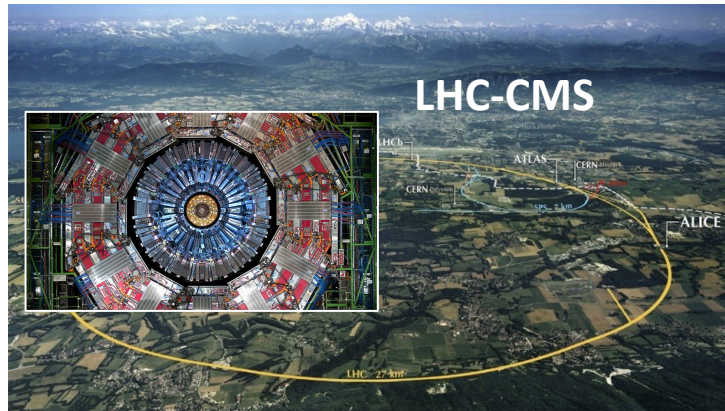
Three ways to study dark matter candidates

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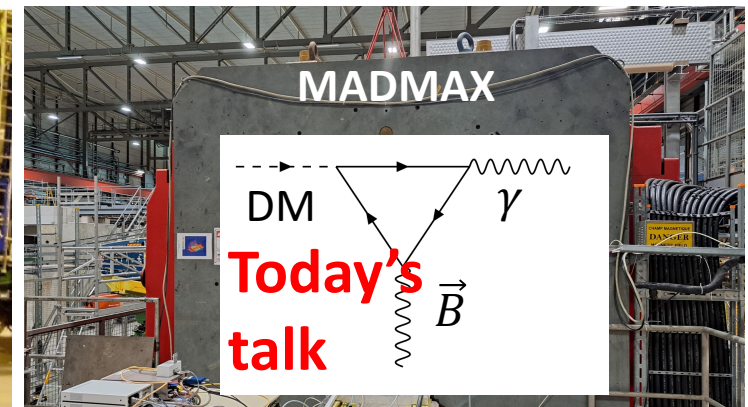
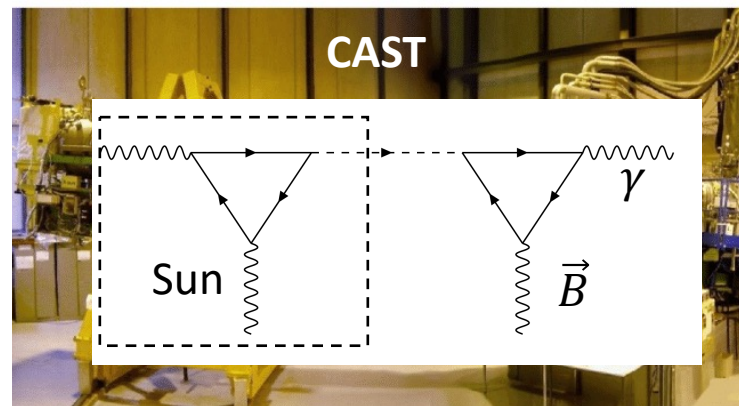
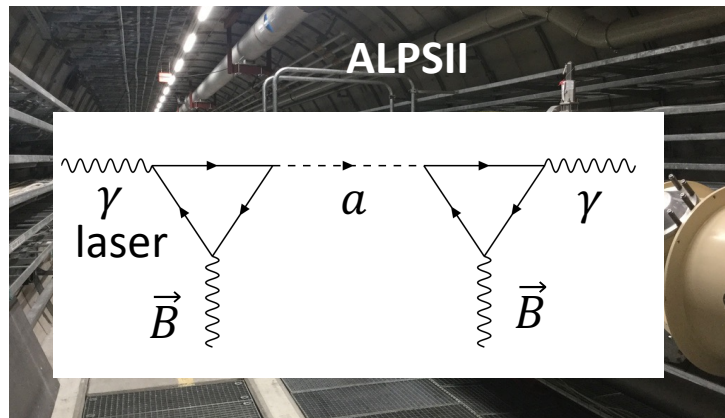
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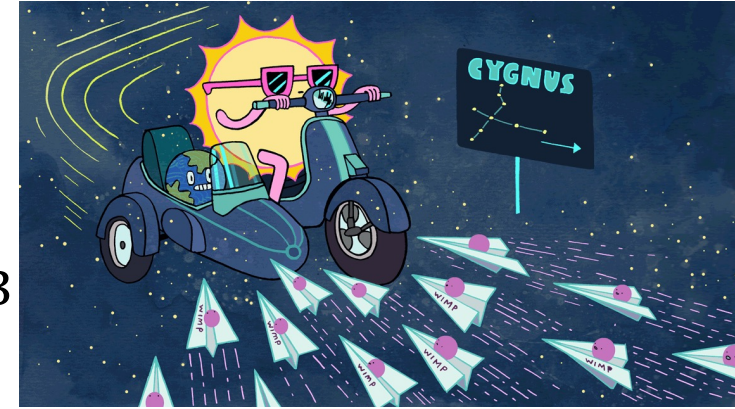
uncertainty in astrophysical models

Uncertainty in cosmological models

→ Common techniques: magnets & **photon science**

De Broglie wavelength λ_B vs density of DM \bar{n}

- We are moving in the **galaxy halo of dark matter** with speed of 220 km/s $\rightarrow \beta \sim 0.07\%$
- **Galaxy halo of dark matter density** $\rho \sim 0.45 \text{ GeV/cm}^3$



<https://www.symmetrymagazine.org/article/wimps-in-the-dark-matter-wind> Artwork by Sandbox Studio, Chicago with Corinne Mucha

WIMP: $m \sim 1 \text{ TeV}$ (?)

$$\lambda_B \sim \frac{196 \text{ MeVfm}}{0.7 \text{ GeV}} = 0.3 \text{ fm}$$

$$\bar{n} \sim \frac{0.45 \text{ GeV/cm}^3}{1 \text{ TeV}} \sim 10^{-3} \text{ cm}^{-3}$$

$$\rightarrow \bar{n} \ll \frac{1}{\lambda^3}$$

WIMP behaves
as a particle

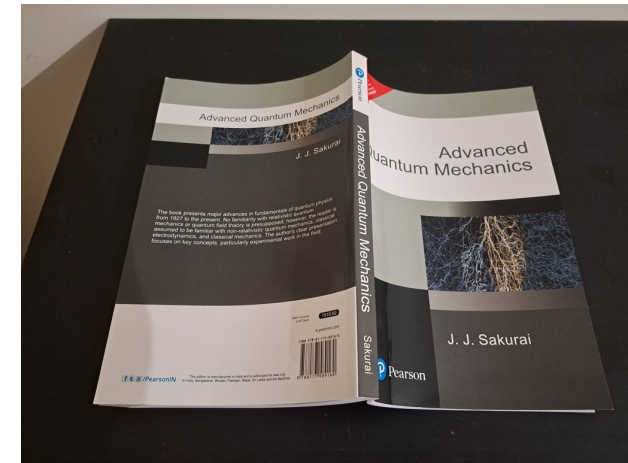
Axions: $m \sim 10 \mu\text{eV}$

$$\lambda_B \sim \frac{2 \times 10^{-7} \text{ eVm}}{7 \text{ neV}} = 28 \text{ cm}$$

$$\bar{n} \sim \frac{0.45 \text{ GeV/cm}^3}{10 \mu\text{eV}} \sim 10^{13} \text{ cm}^{-3}$$

$$\rightarrow \bar{n} \gg \frac{1}{\lambda^3}$$

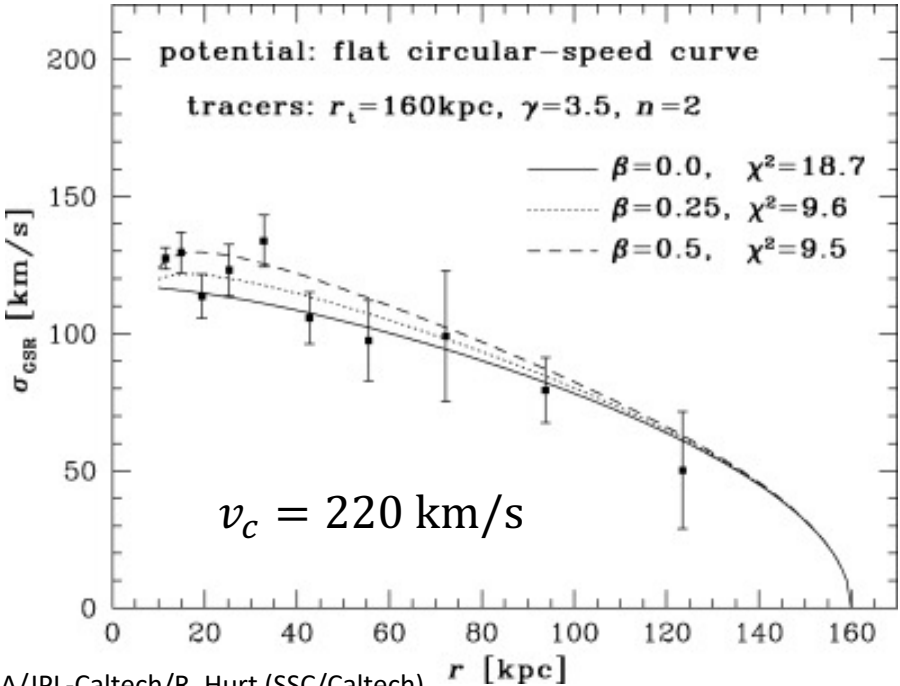
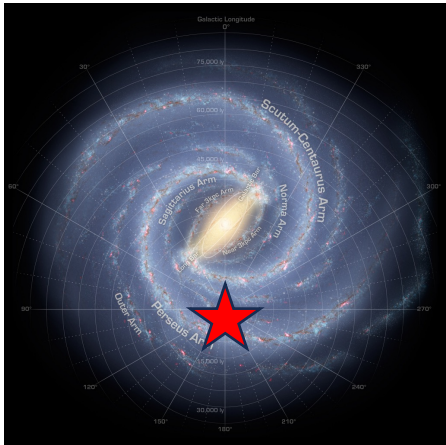
**DM Axions behave
as a wave**



$$E_{cl}^2 = \frac{\bar{n}}{\lambda} \gg \frac{1}{\lambda^4} \sim \langle 0 | \hat{E} \cdot \hat{E} | 0 \rangle$$

Standard model of dark matter axion distribution function

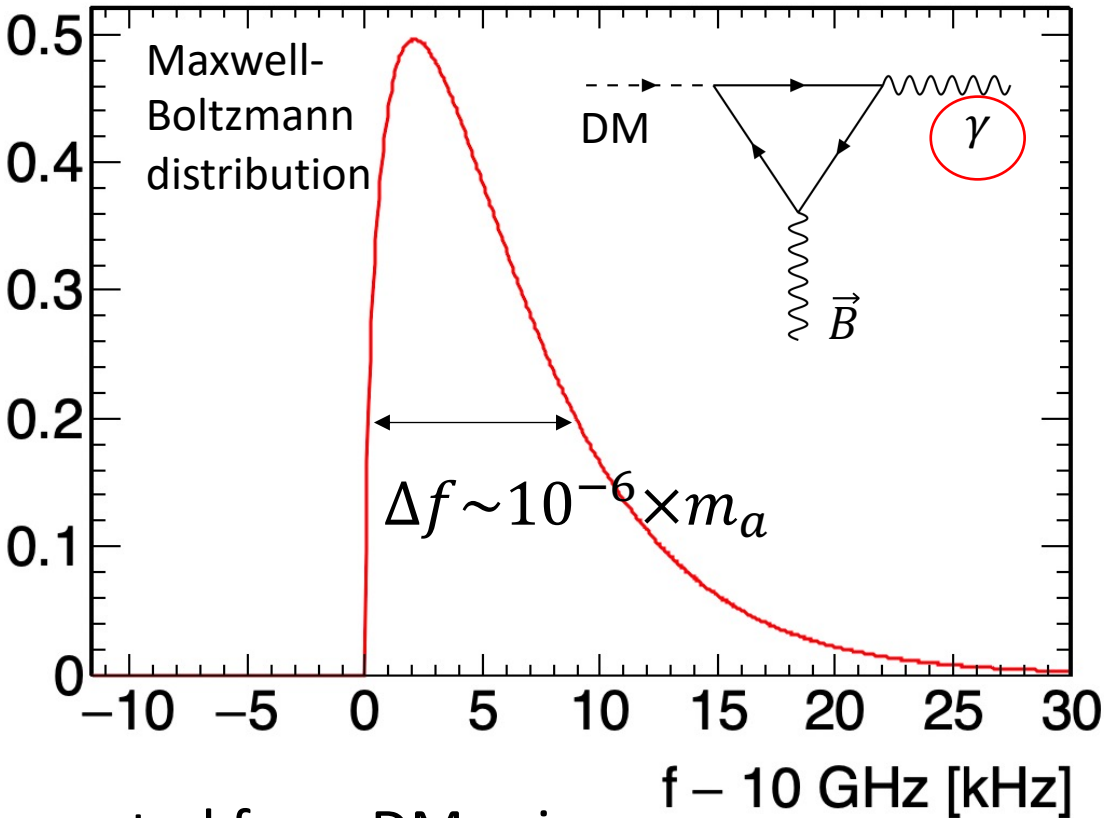
Velocity
dispersion of
Milky way
Galaxy around



NASA/JPL-Caltech/R. Hurt (SSC/Caltech)
Mon Not R Astron Soc, Volume 369, Issue 4, July 2006, Pages 1688–1692,

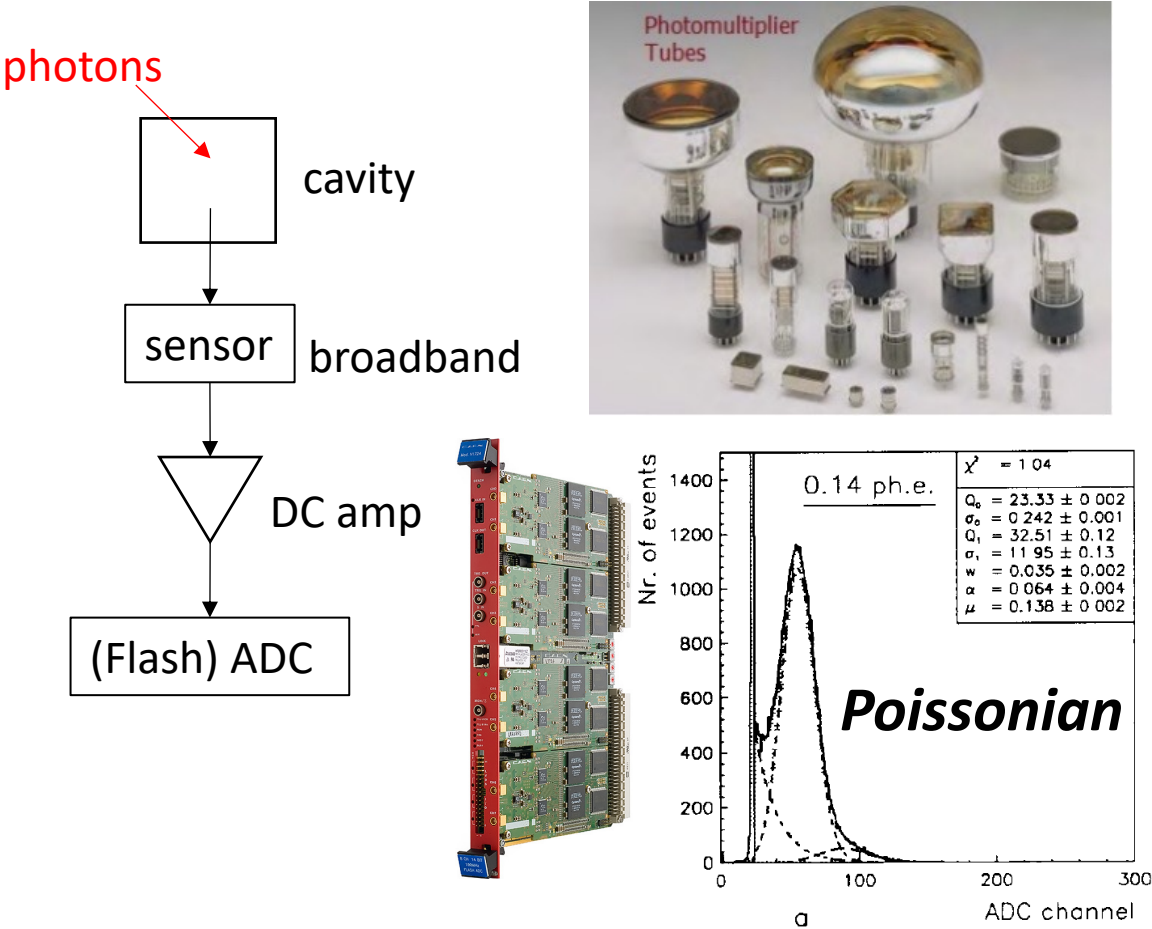
$$f(\omega) = P_0 \theta(\omega - m_a) 2\omega_0^{-\frac{3}{2}} \sqrt{\frac{\omega - m_a}{\pi}} \exp\left(-\frac{\omega - m_a}{\omega_0}\right)$$

If $m_a = 10 \text{ GHz}$



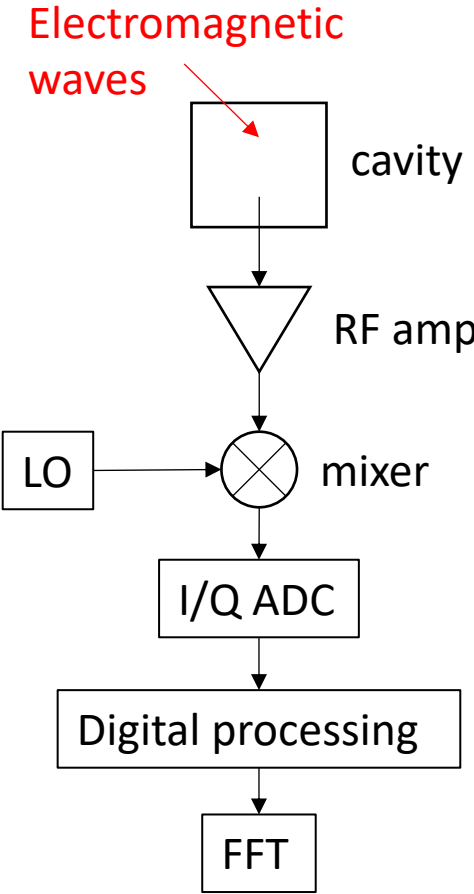
Microwaves converted from DM axion
is very narrow band classical waves

Photon (energy) detection vs wave detection



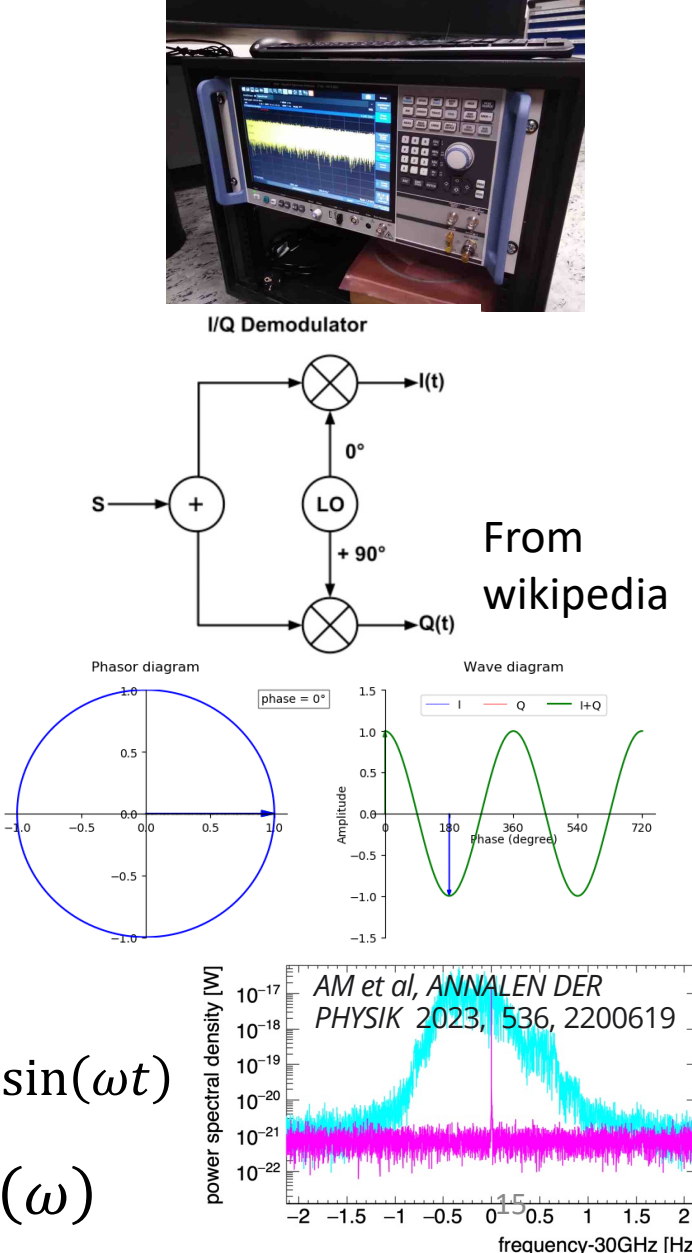
$$P(t) = n \times \hbar \omega \propto V_{ADC}(t)$$

$$\Delta \phi \Delta n > 0$$

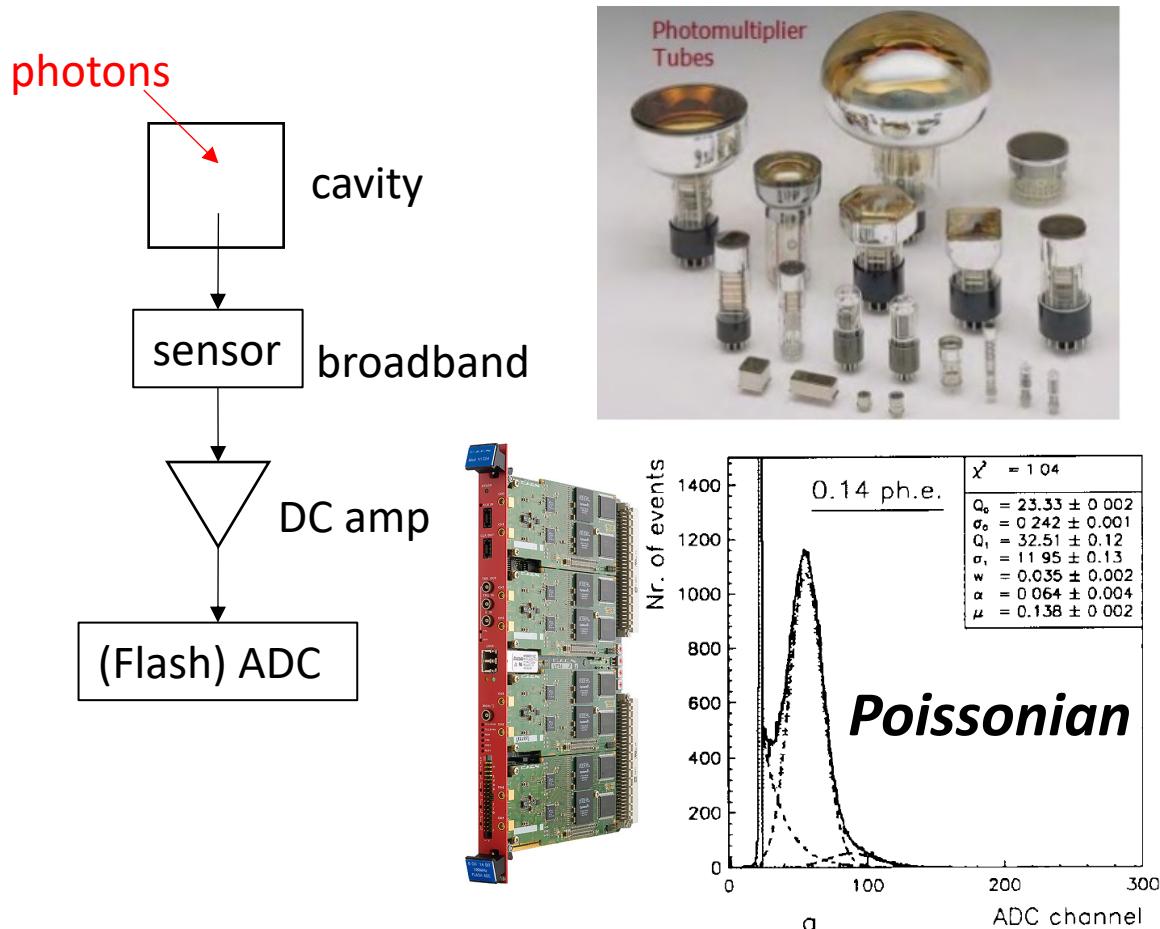


$$RF(t) = I(t) \cos(\omega t) + Q(t) \sin(\omega t)$$

$$\rightarrow P(\omega) = \tilde{I}^2(\omega) + \tilde{Q}^2(\omega)$$

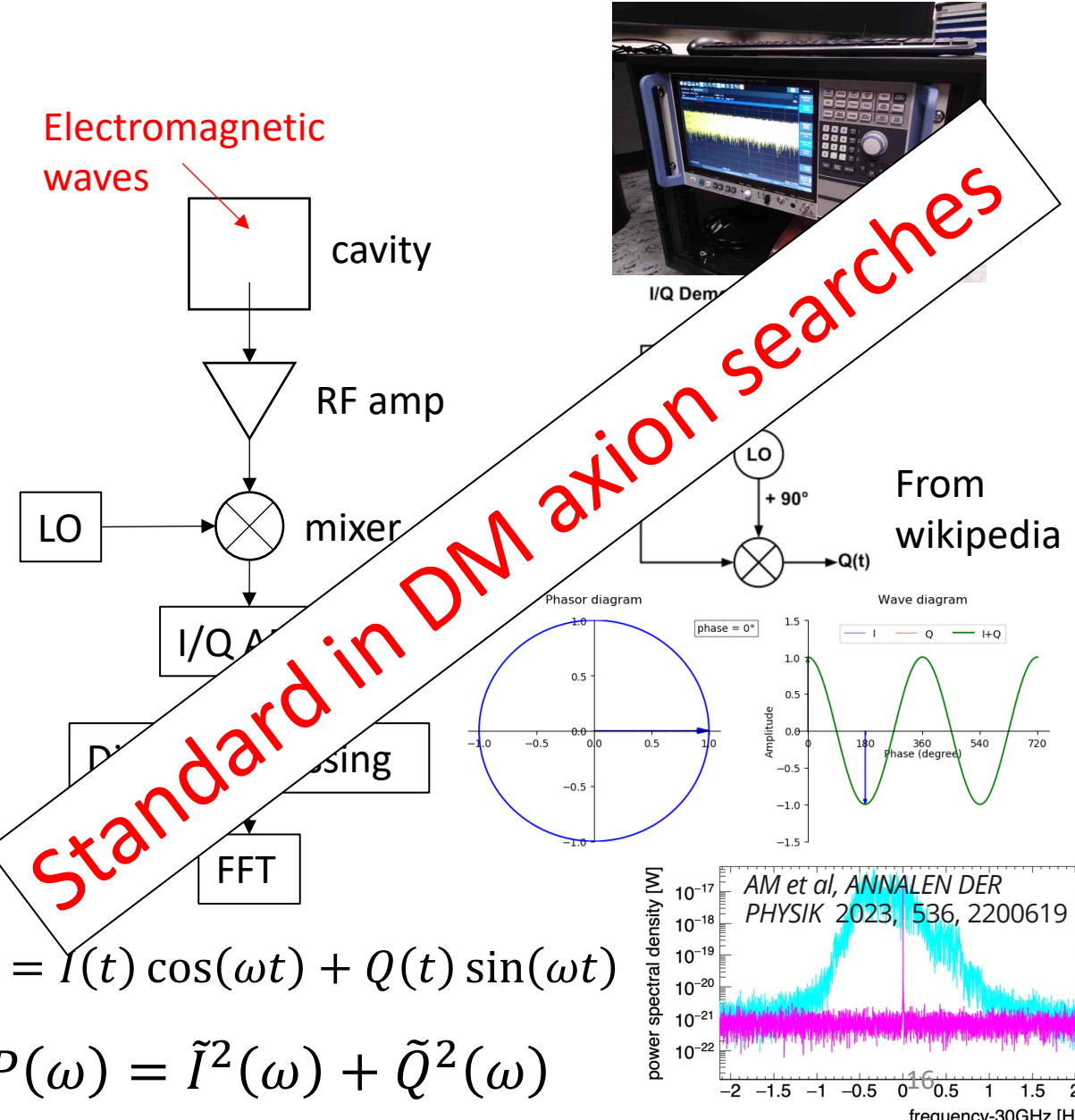


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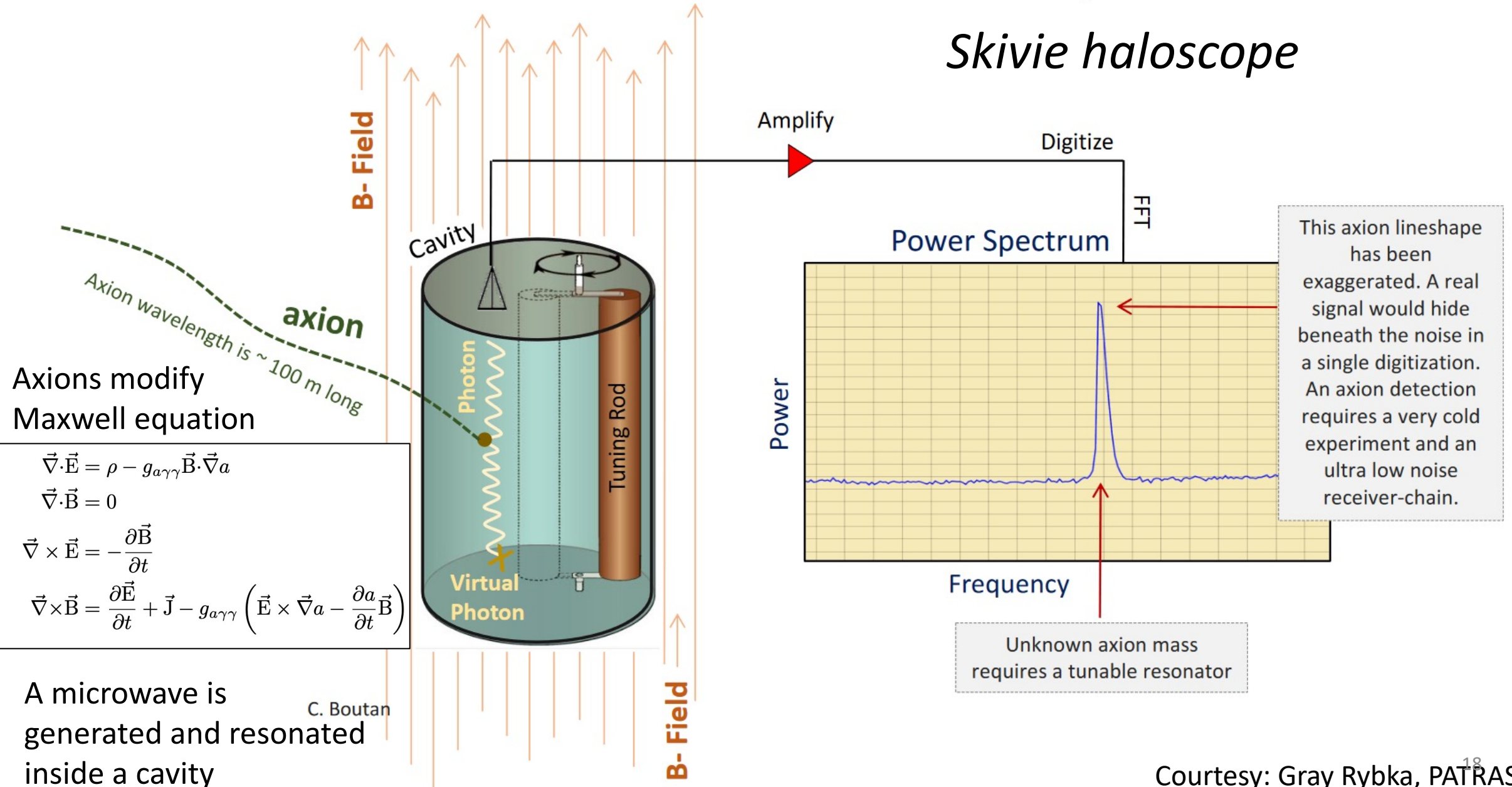
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Classical electrodynamics is the mean to hunt axions

Skivie haloscope



Axion Dark Matter eXperiment (ADMX)

arXiv:2010.00169

Signal to Noise Ratio is the key for discovery

- Signal is a narrow peak ($f/\Delta f \sim 10^6$) from axion

$$P_S = (1.0 \times 10^{-22} \text{ W}) \times \left(\frac{V}{136\text{L}}\right) \left(\frac{B}{6.8\text{T}}\right)^2 \left(\frac{C}{0.4}\right) \left(\frac{g}{0.97}\right)^2 \left(\frac{\rho}{0.45 \text{ GeV/cm}^3}\right) \left(\frac{f}{650 \text{ MHz}}\right) \left(\frac{Q}{50000}\right)$$

- Johnson Nyquist noise power

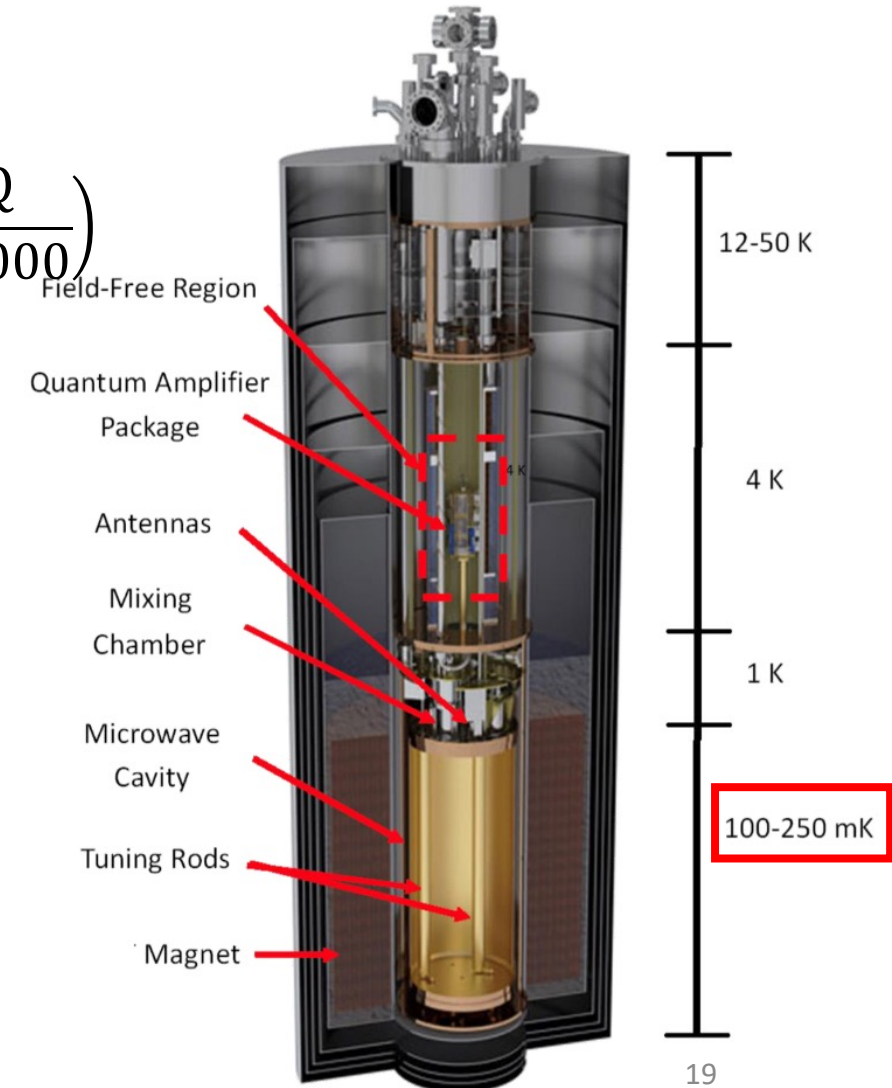
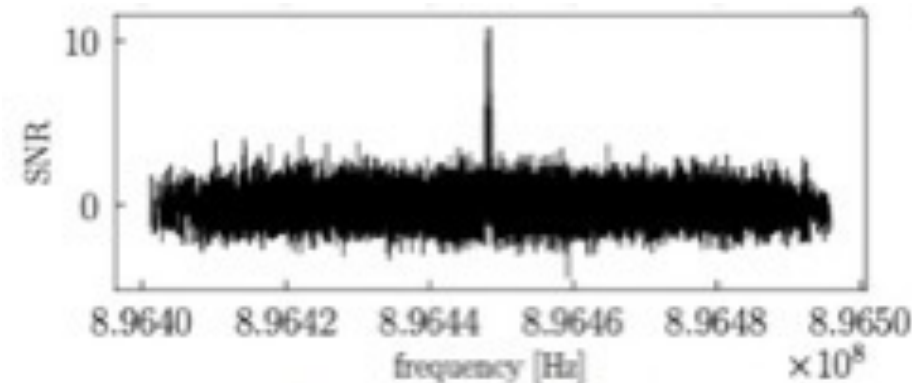
$$P_N = k_B T_s = 1.4 \times 10^{-23} \left(\frac{T_s}{1\text{K}}\right) \text{ W/Hz}$$

- Dicke's radiometer formula

$$S/N = \frac{P_s}{P_N} \sqrt{\frac{t}{b}}$$

t : integration time

b : measurement bandwidth



Rybka - August 2022

Jonsson Nyquist Noise

J. B. Johnson Phys Rev 32 97 (1928): Experimental discovery of the relation

H. Nyquist Phys Rev 32 110 (1928): Thermodynamics + statistical mechanics of **bosonic** modes

$$\langle V^2 \rangle \Delta\nu \sim 4R\Delta\nu \frac{h\nu}{e^{h\nu/k_B T} - 1} \xrightarrow[\text{Rayleigh Jeans}]{h\nu \ll k_B T} 4Rk_B T \Delta\nu$$

Noise power spectral density $P_N = \frac{\langle V^2 \rangle}{4R\Delta\nu} \sim k_B T$

→ “Blackbody radiation” of electromagnetic waves inside a 1D conductor

Quantum mechanical derivation H. B. Callen and T. A. Welton Phys Rev 1 34 (1951)

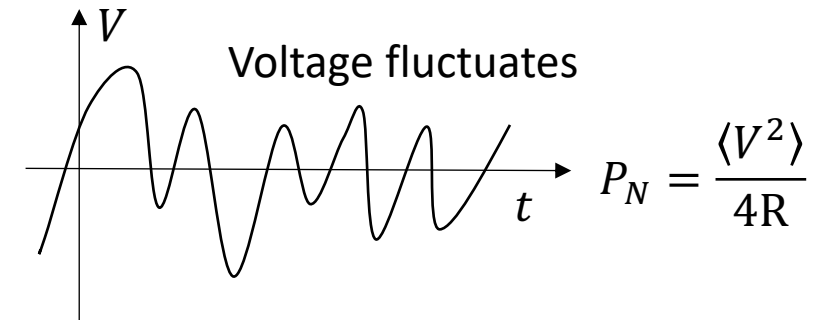
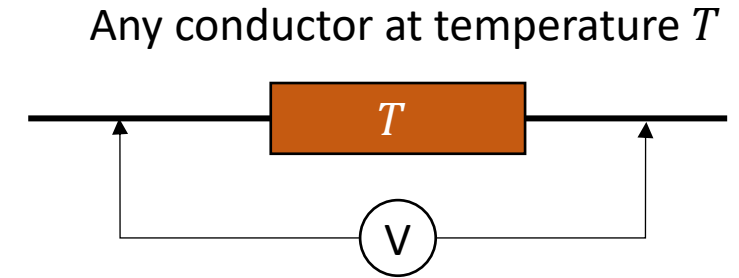
$$P_N = \left(\frac{h\nu}{2} + \frac{h\nu}{e^{h\nu/k_B T} - 1} \right) \quad [\text{W/Hz}]$$

Zero-point energy

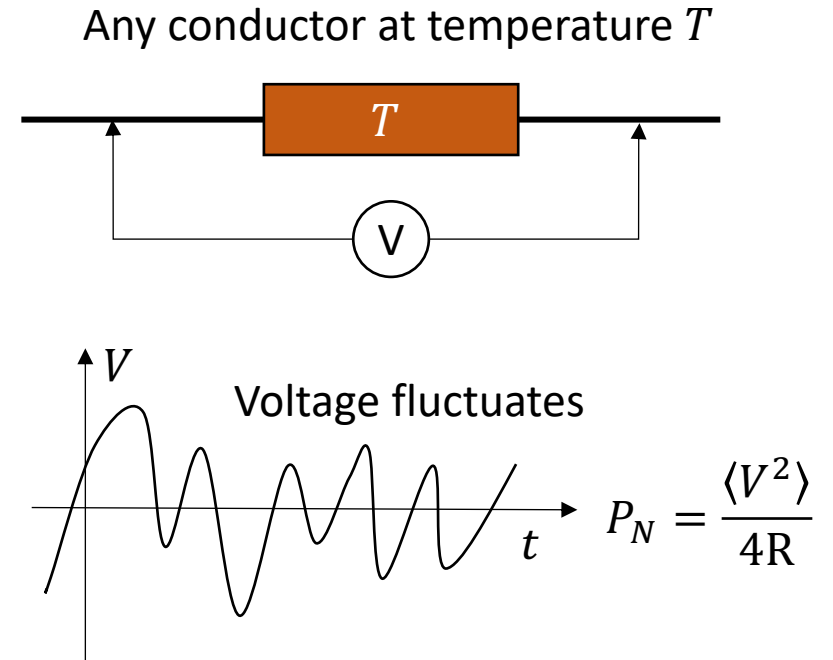
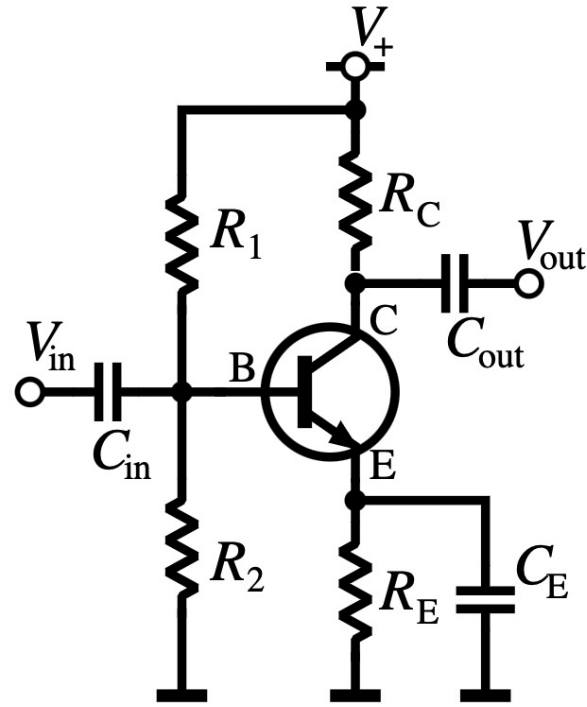
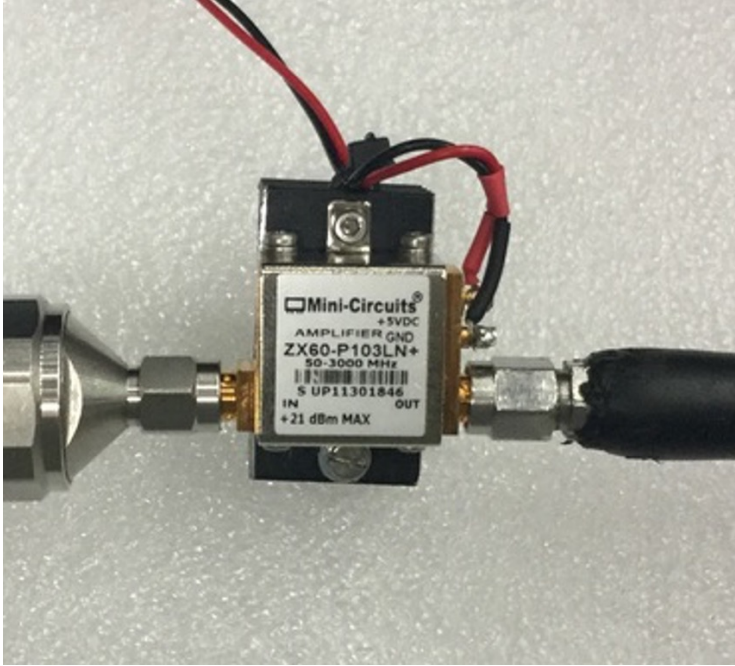
→ Cooling down reveals
fundamental noise floor

$P_{SQL} = h\nu$: standard quantum limit

Ex) $h \times 1 \text{ GHz} = 6.6 \times 10^{-25} \text{ W/Hz}$



Classical: amplifier based on transistors



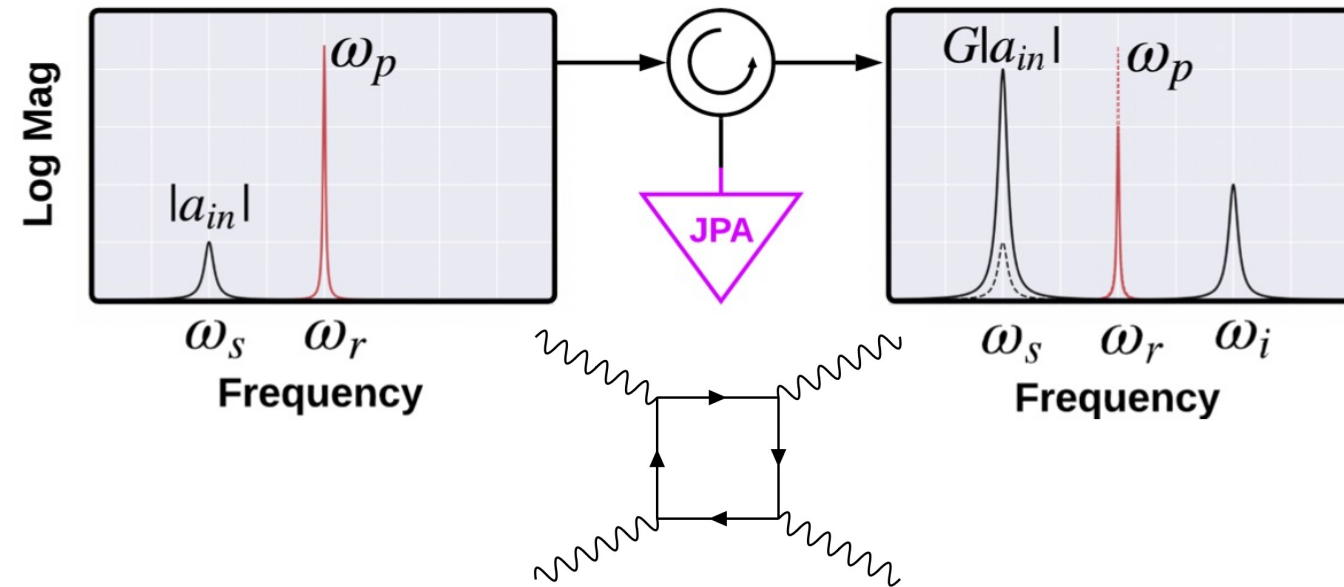
- Amplification of microwaves (typically $> \times 100$) via electron or hole current in the transistors
- Noise sources

- Resistance' thermal noise
- Shot noise of currents (dominating)

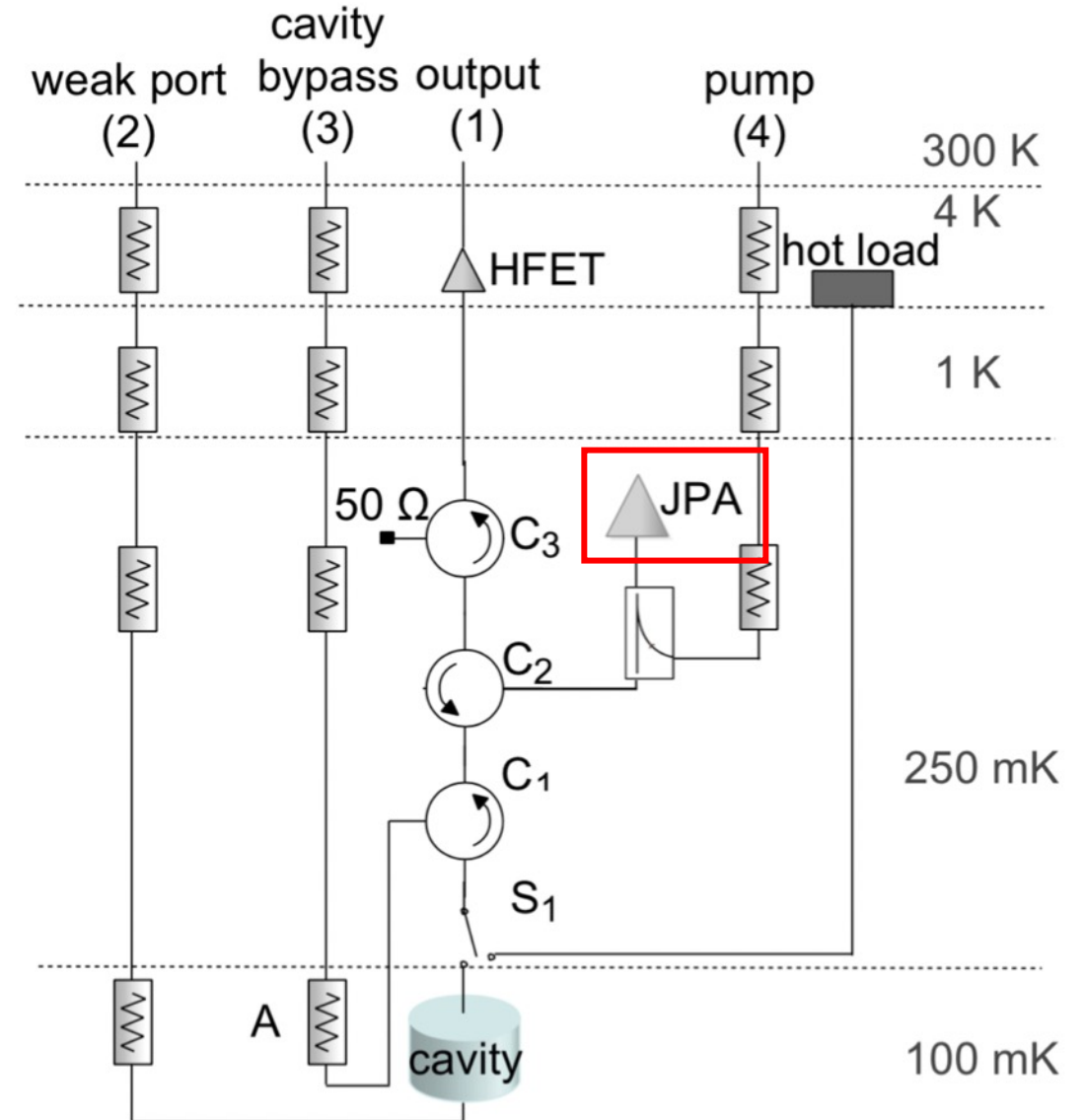
→ The effective noise temperature is always limited by a certain value

→ One cannot reach standard quantum limit by cooling down $k_B T_{SQL} = h\nu < k_B T_S$ ☹

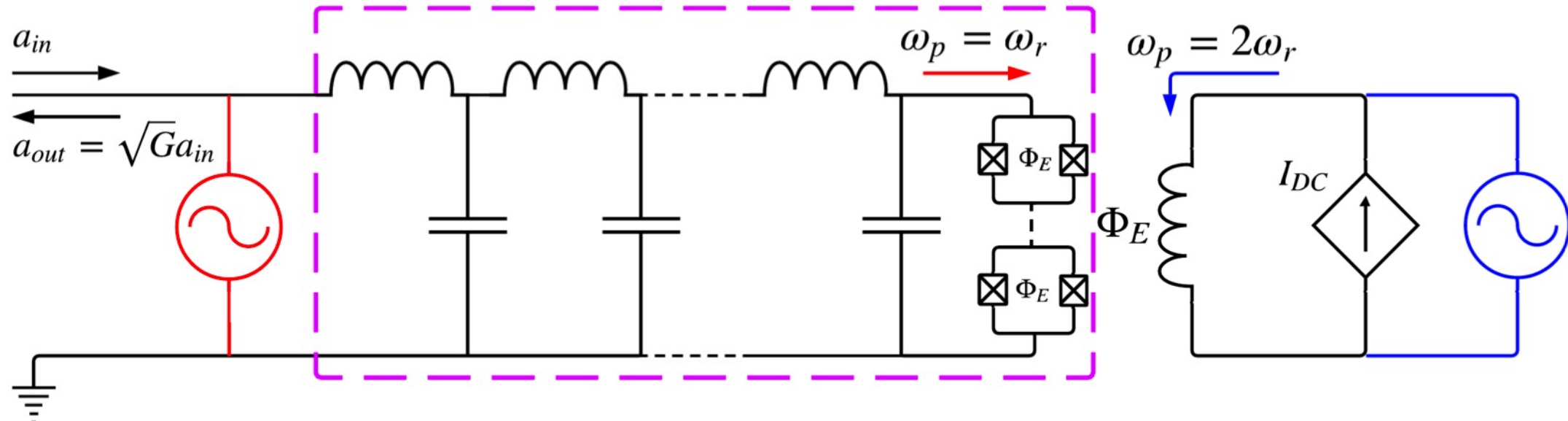
Semi-classical: Parametric Amplifier (in ADMX)



- Amplification of microwave signal at ω_s via pump microwaves at ω_p
- Nonlinear optics (Kerr effect) for frequency mixing
- No real electron/hole current
 - Free from the noise source of transistors
 - One can reach $k_B T_{SQL} = h\nu$ by cooling down

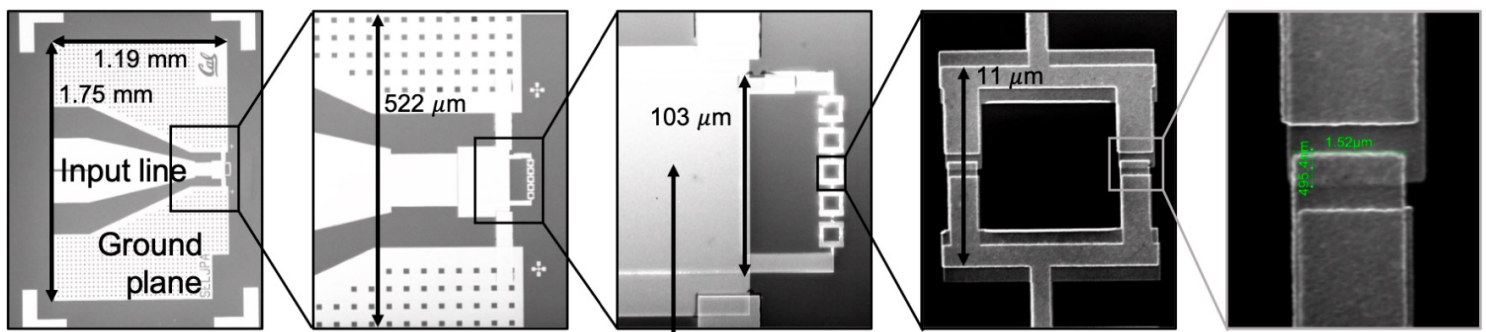


Implementation: Josephson Parametric Amplifier



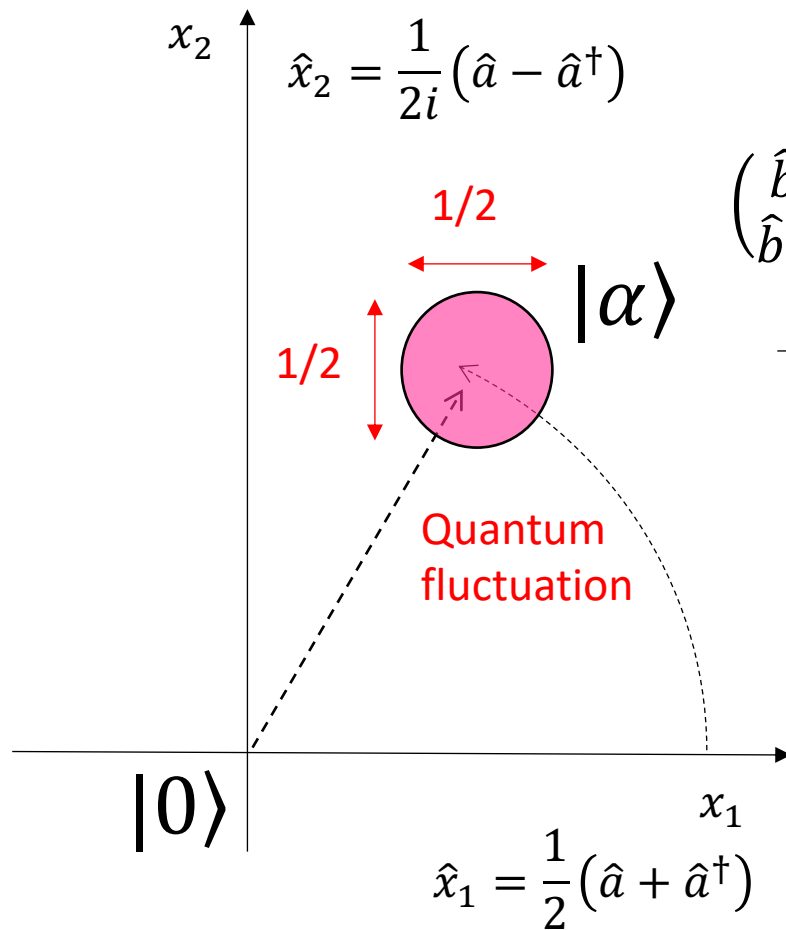
$$L_J = \frac{L_{J0}}{\sqrt{1 - (I/I_0)^2}} = L_{J0} \left(1 + \frac{1}{2} (I/I_0)^2 + \dots \right)$$

- The nonlinearity is induced from Josephson junctions inside SQUID
- Although SQUID is a superconducting quantum device, **microwave's behavior is classical** (→ semi-classical)



Another use of JPA: Squeezed state (not in ADMX)

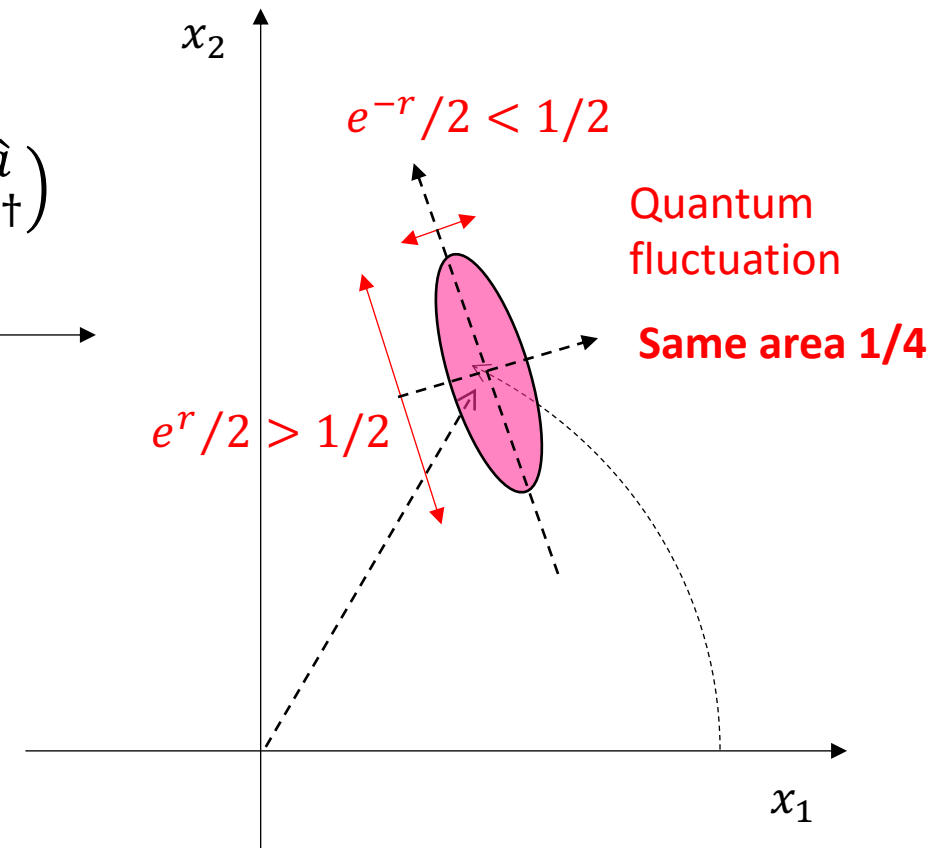
$$\hat{H} = \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right) \hbar \omega + \hbar \left(\frac{E^*}{2} \hat{a}^2 + \frac{E}{2} \hat{a}^{\dagger 2} \right) \quad \text{Nonlinear term added by parametric oscillation}$$



$$\begin{pmatrix} \hat{b} \\ \hat{b}^\dagger \end{pmatrix} = \begin{pmatrix} \cosh r & e^{2i\phi} \sinh r \\ e^{-2i\phi} \sinh r & \cosh r \end{pmatrix} \begin{pmatrix} \hat{a} \\ \hat{a}^\dagger \end{pmatrix}$$

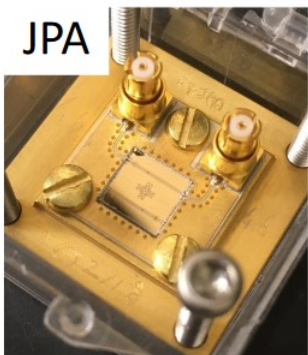
$$\hat{H} = \hbar \lambda \hat{b}^\dagger \hat{b} + \frac{\lambda - \omega}{2}$$

$$\begin{cases} \lambda = \sqrt{\omega^2 - |E|^2} \\ r = \frac{1}{2} \tanh^{-1}(|E|/\omega) \\ e^{2i\phi} = E/|E| \end{cases}$$

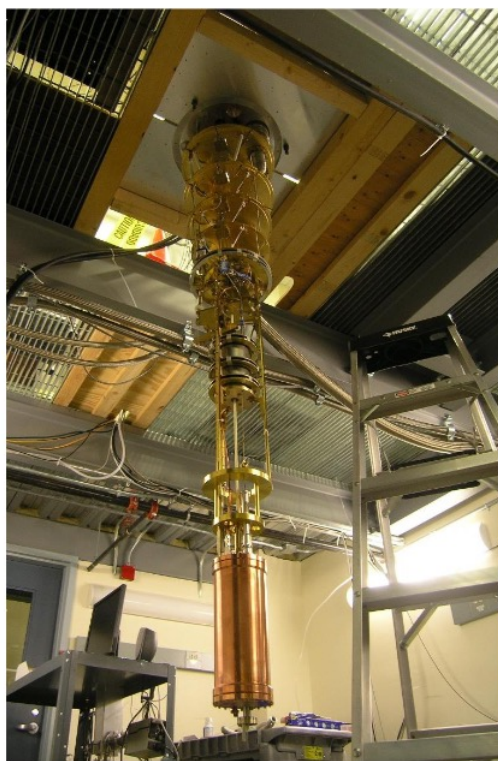


Axions search is entering a quantum regime

HAYSTAC reduces one of the noises via squeezing

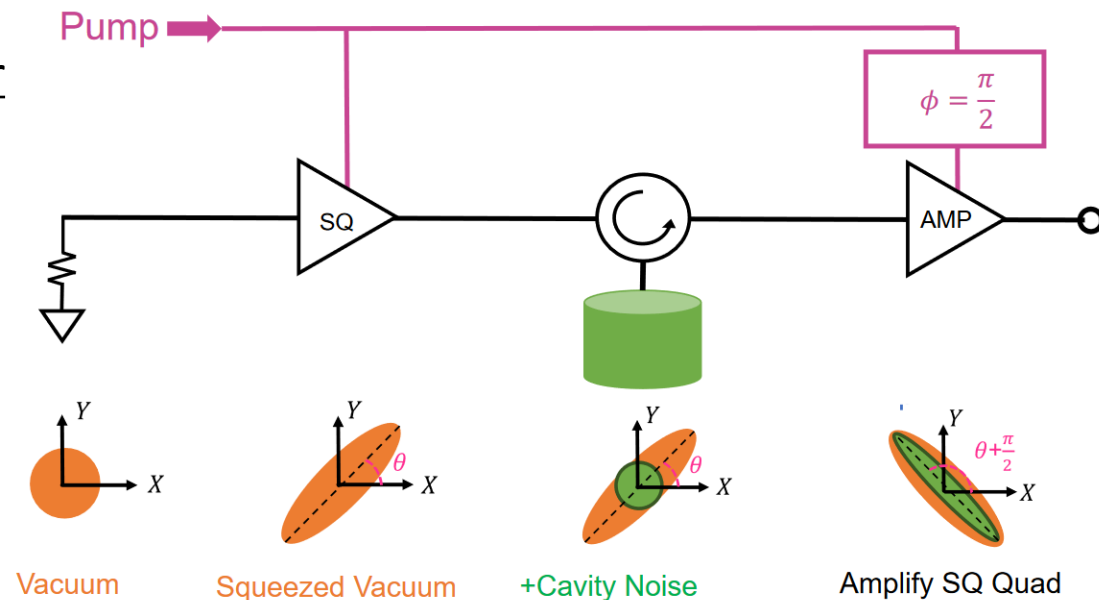
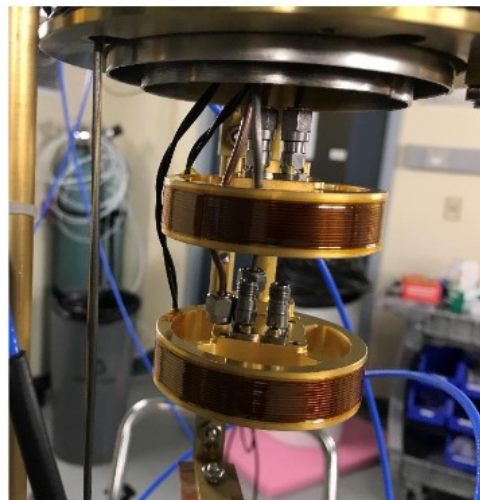


JPA

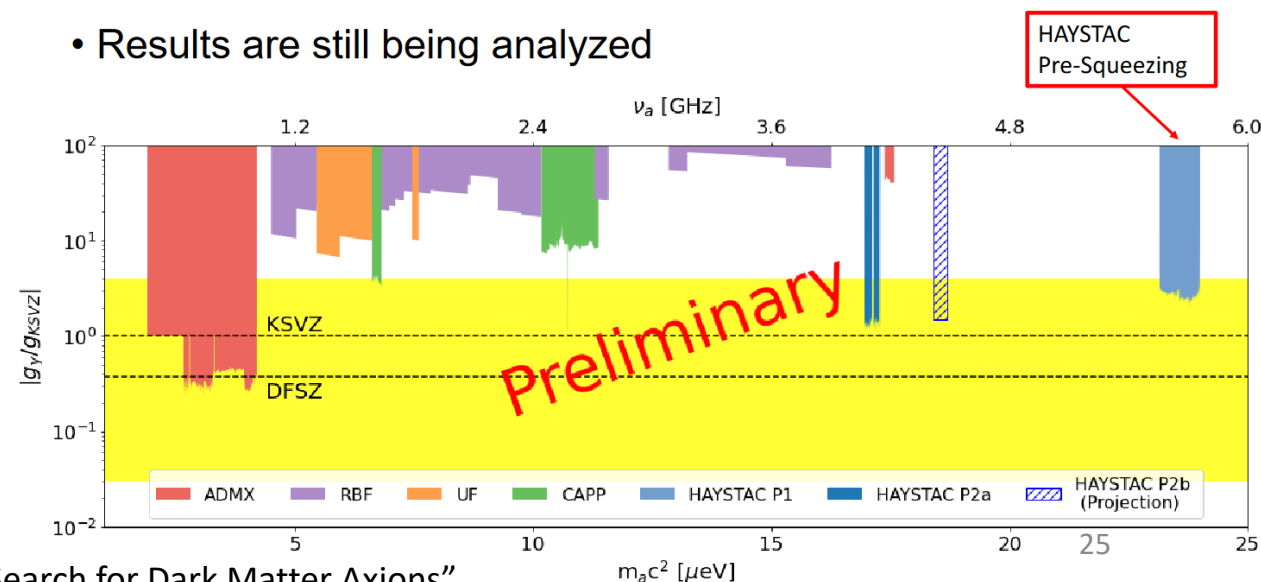


Cavity

Squeezed State Receiver



- Results are still being analyzed



Single quadrature read-out & reduced external noise from squeezed read-out line

→ Currently $\times 2$ (finite loss in circuit)

→ potentially $> \times 20$

Single photon sensors (?)

Noise power of wave detection

$$P_l = h\nu(\bar{n} + 1) \sqrt{\frac{\Delta\nu}{t}} \propto \nu$$

Noise power of photon detection

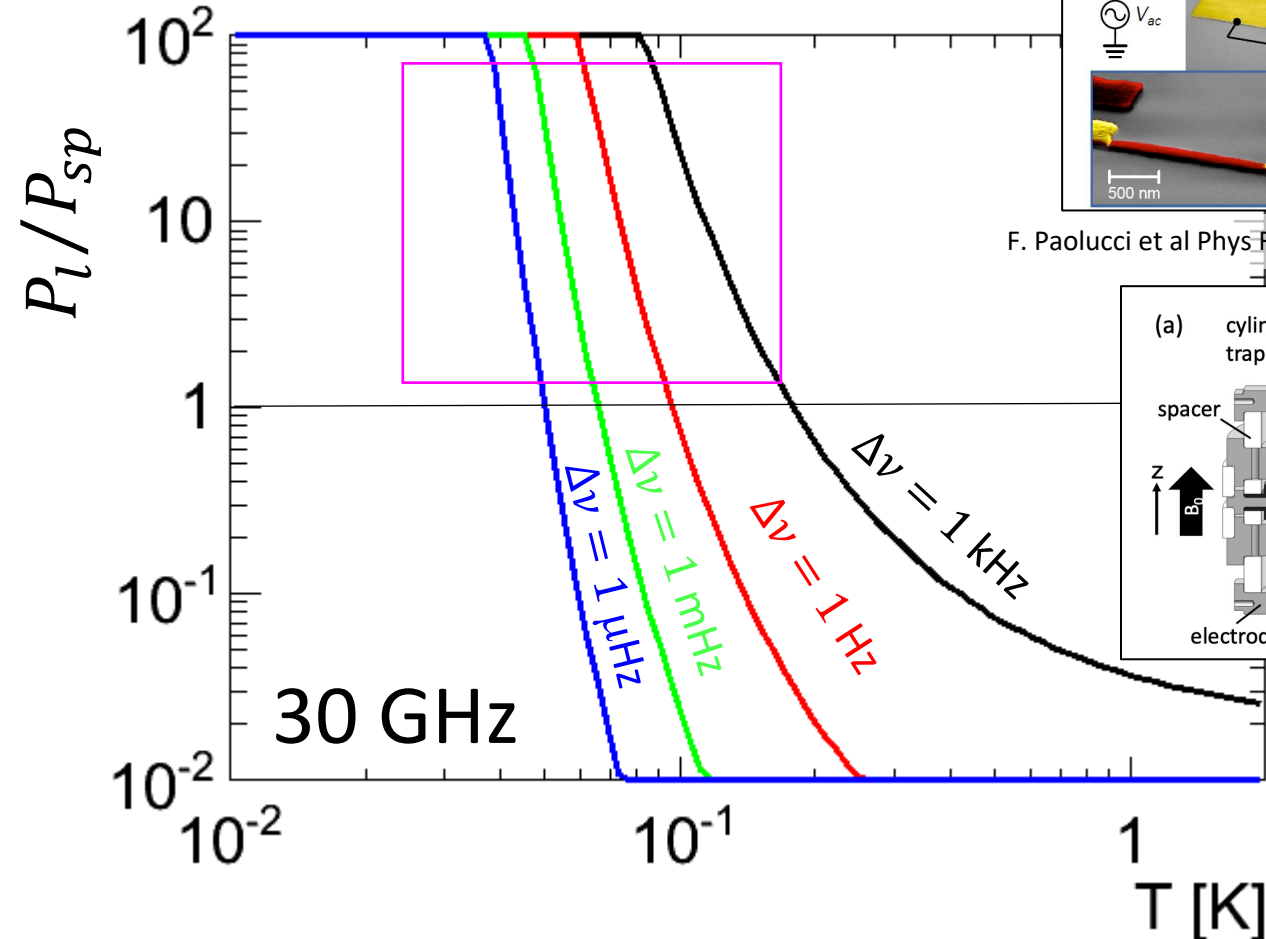
$$P_{sp} = h\nu \sqrt{\frac{\eta \bar{n} Q_c}{2\pi\nu t}} \propto \sqrt{\nu}$$

$$\bar{n} = \frac{1}{e^{h\nu/k_B T} - 1}$$

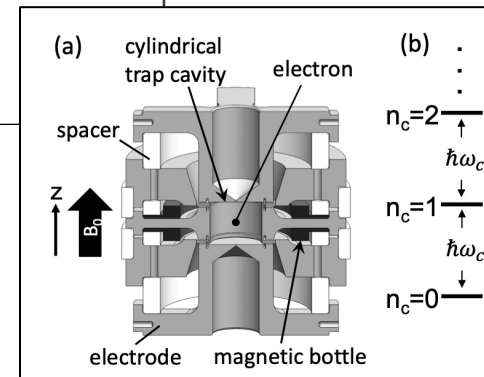
Q_c : cavity quality factor

η : quantum efficiency of the sensor

S.K. Lamoreaux et al Phys Rev D 98 035020 (2013)



F. Paolucci et al Phys Rev Appl. 14 034055 (2020)



X. Fan et al, PRL129, 261801, 2022

Single photon sensors may be a solution in the future

→ Although one loses phase information, zero background at cold may be better

→ Lower noise in **higher frequency** → where is the cross-over? 10 GHz? 100 GHz??

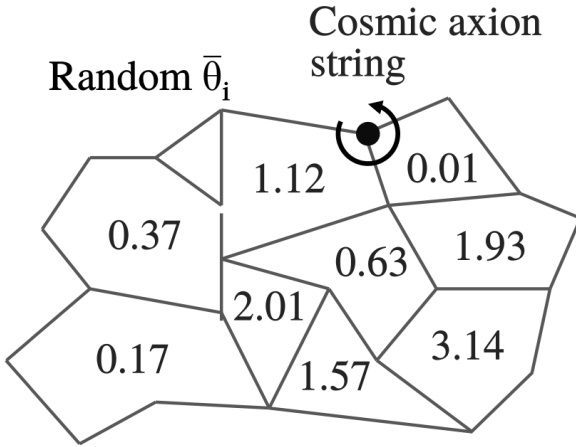
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 - Axion and axion dark matter
 - Particle vs wave
- State of the art
 - ADMX experiment
 - Background noise and quantum limit
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- **New experiments**
 - Challenge toward higher frequency
 - Dish antenna: signal from metal/vacuum interface
 - MADMAX: signal boost with dielectric disks
 - ALPHA: plasma haloscope with wire metamaterial
- Conclusion

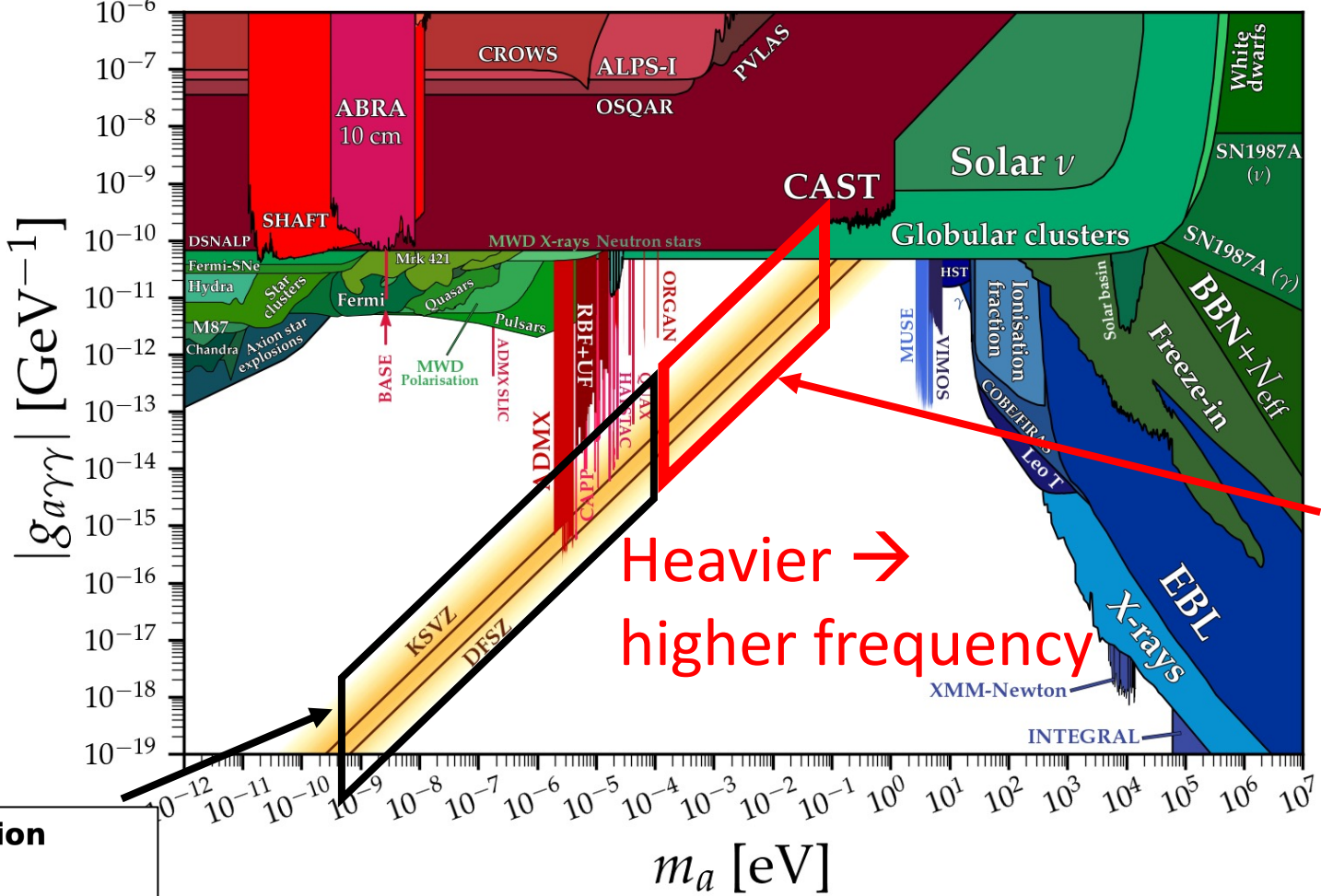
From now

Post-Inflation

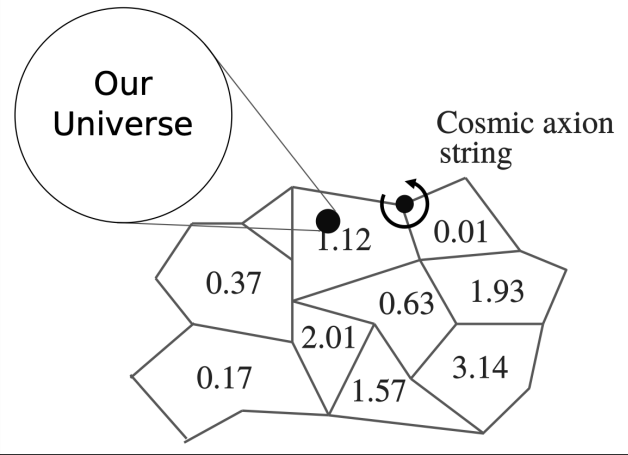
Our Universe:



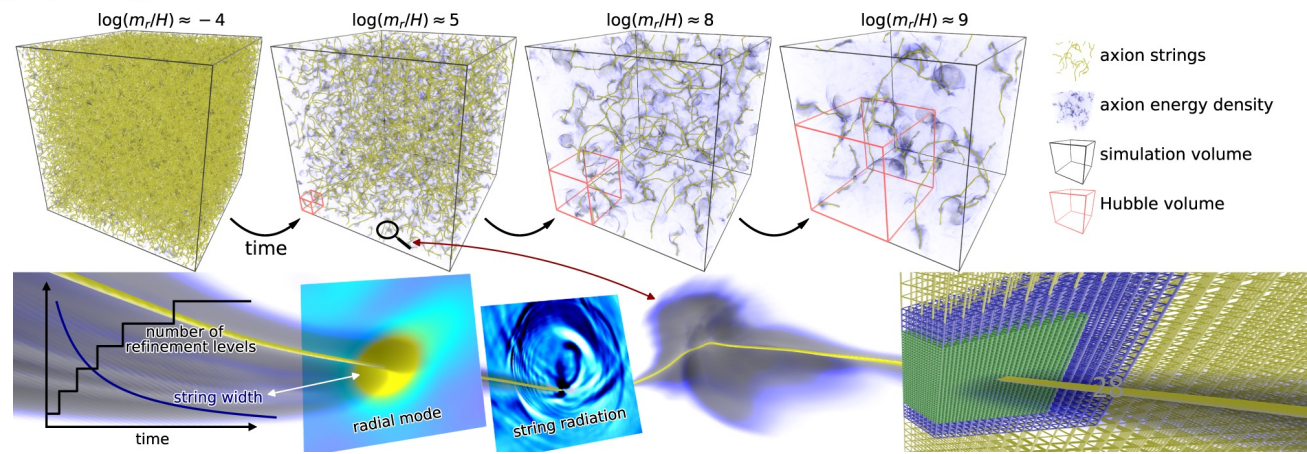
So far



Pre-Inflation

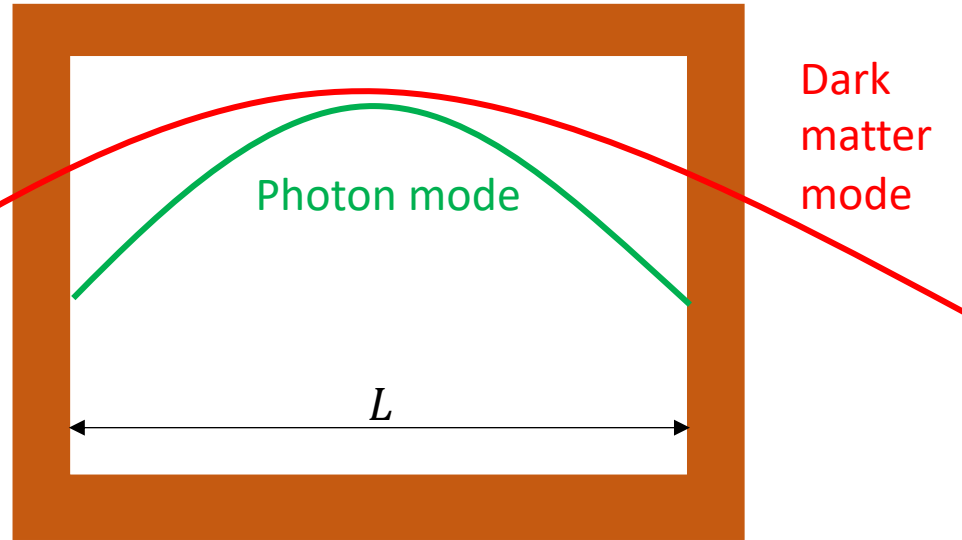


Buschmann, et al. *Nat Commun* **13**, 1049 (2022)



Issue of high-frequency resonators for dark matter search

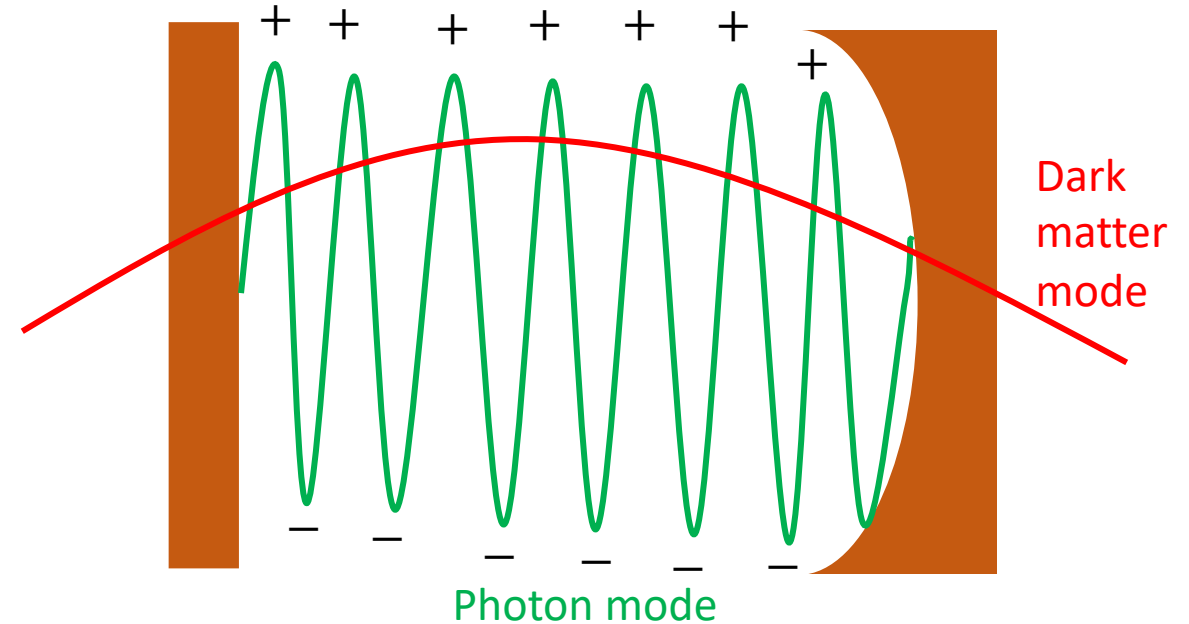
An RF cavity (ADMX-type) becomes $V \sim f^{-3}$



Signal: $\propto VQ$

The signal is lost by higher frequency

An over-sized cavity cancels the signal



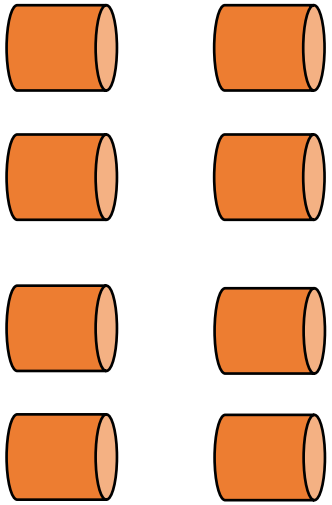
The dark matter is cold \rightarrow De Broglie wavelength is long

Spatial integral is cancelled!

\rightarrow We have needed an idea to keep the resonator size reasonable with high frequency without having polarity changes

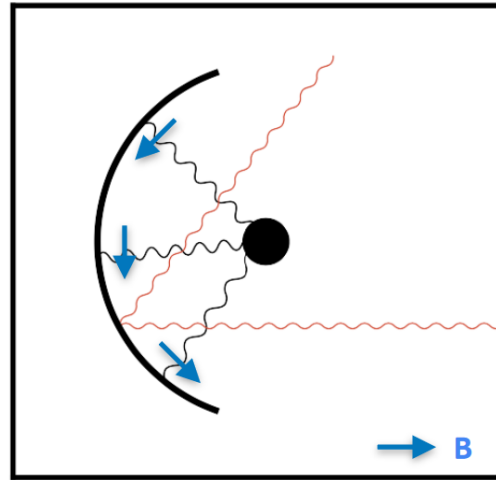
Four ideas toward heavier axion dark matter

Multiple small cavities



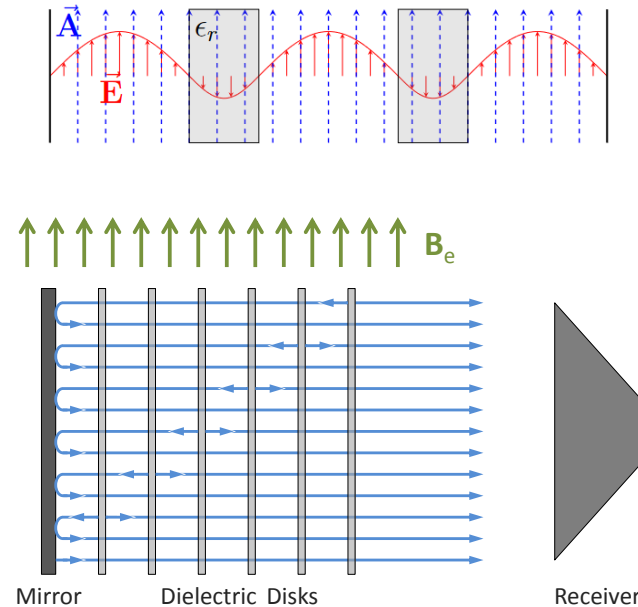
ADMX-EFR @ US
CAST-CAPP @ CERN

Dish antenna



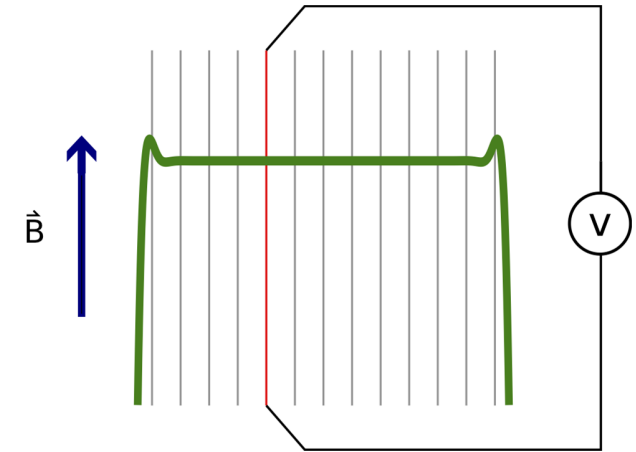
BRASS @ DESY
BREAD @ US

Dielectric disks



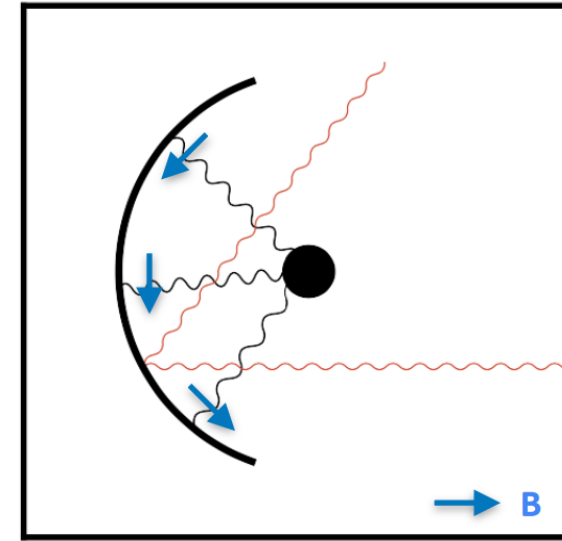
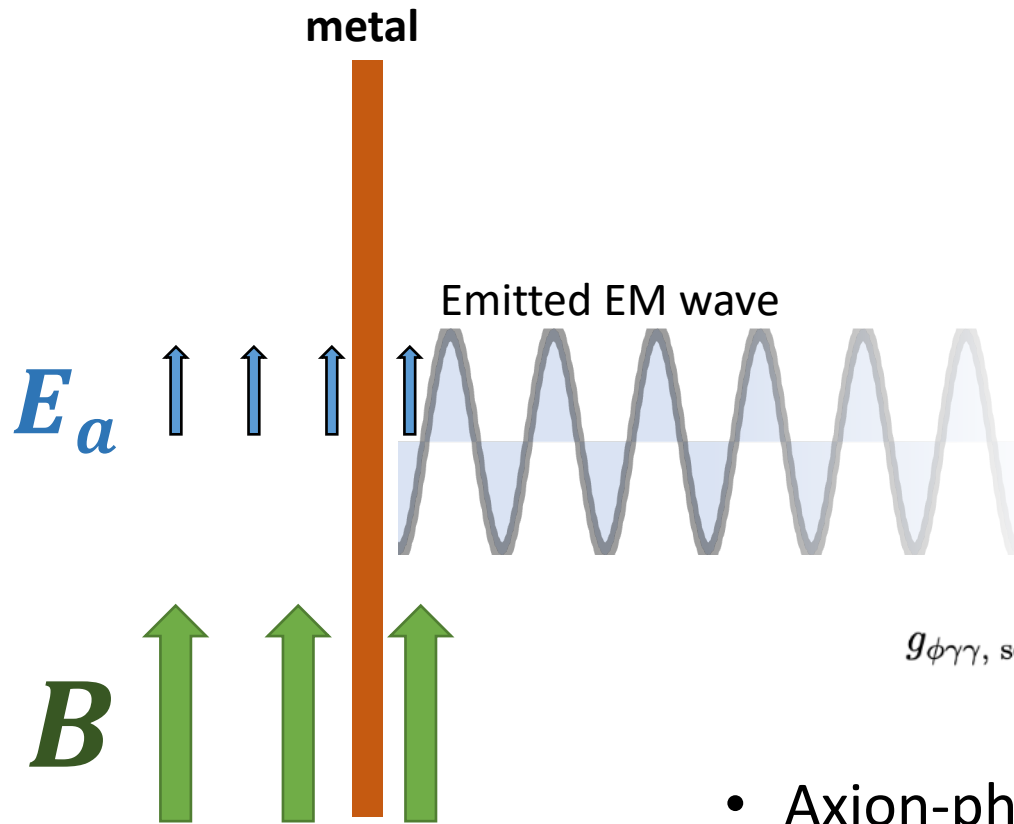
ORGAN @ Australia
ADMX-Orpheus @ US
MADMAX @ DESY

Wire metamaterial



ALPHA @ SU
New projects rising

Dish antenna: mismatch between metal and vacuum

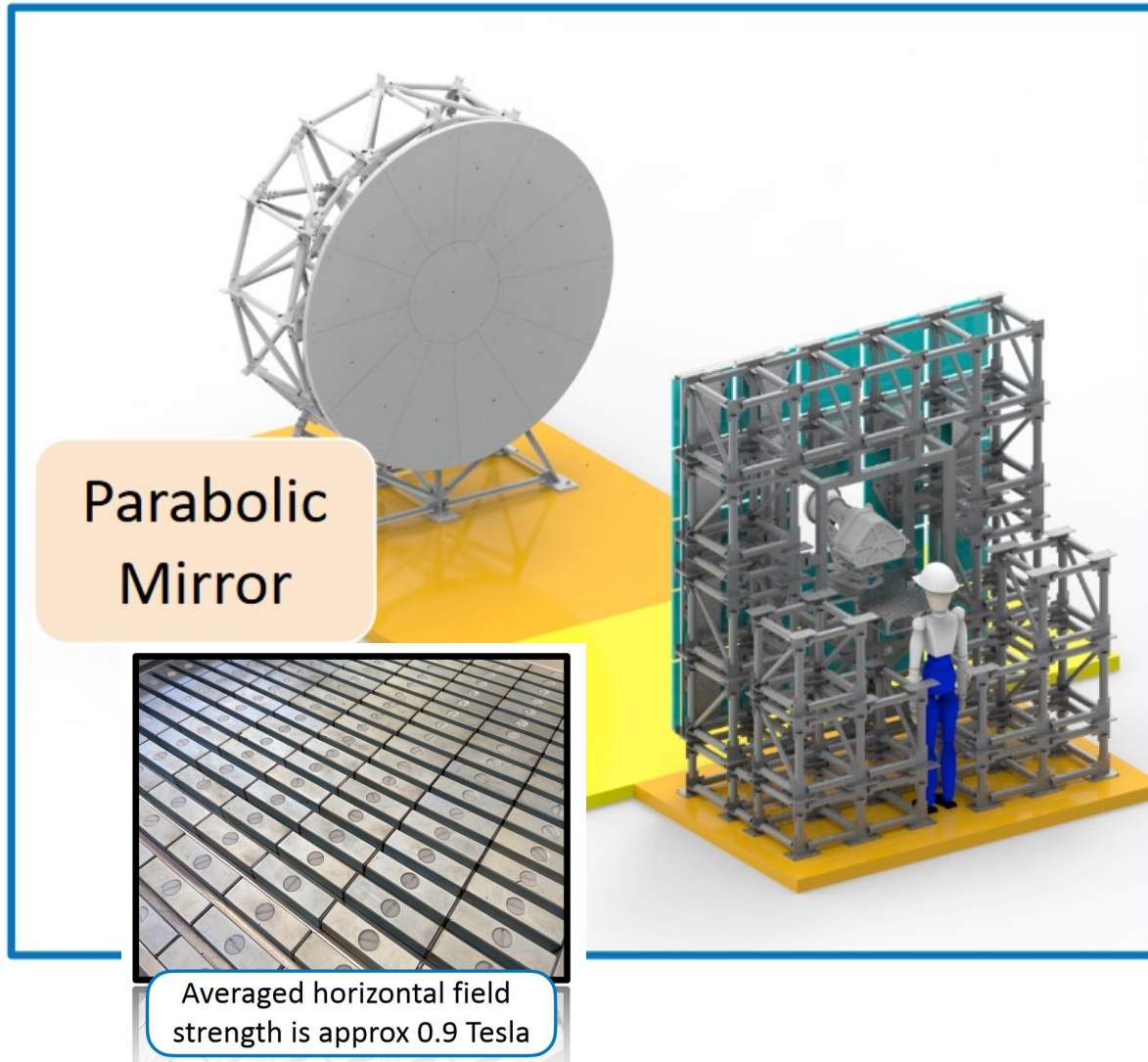


$$g_{\phi\gamma\gamma, \text{ sens}} = \frac{3.6 \times 10^{-8}}{\text{GeV}} \left(\frac{5 \text{ T}}{\sqrt{\langle |\mathbf{B}_{\parallel}|^2 \rangle}} \right) \left(\frac{P_{\text{det}}}{10^{-23} \text{ W}} \right)^{\frac{1}{2}} \left(\frac{m_{\phi}}{\text{eV}} \right) \left(\frac{0.3 \text{ GeV/cm}^3}{\rho_{\text{DM, halo}}} \right)^{\frac{1}{2}} \left(\frac{1 \text{ m}^2}{A_{\text{dish}}} \right)^{\frac{1}{2}}$$

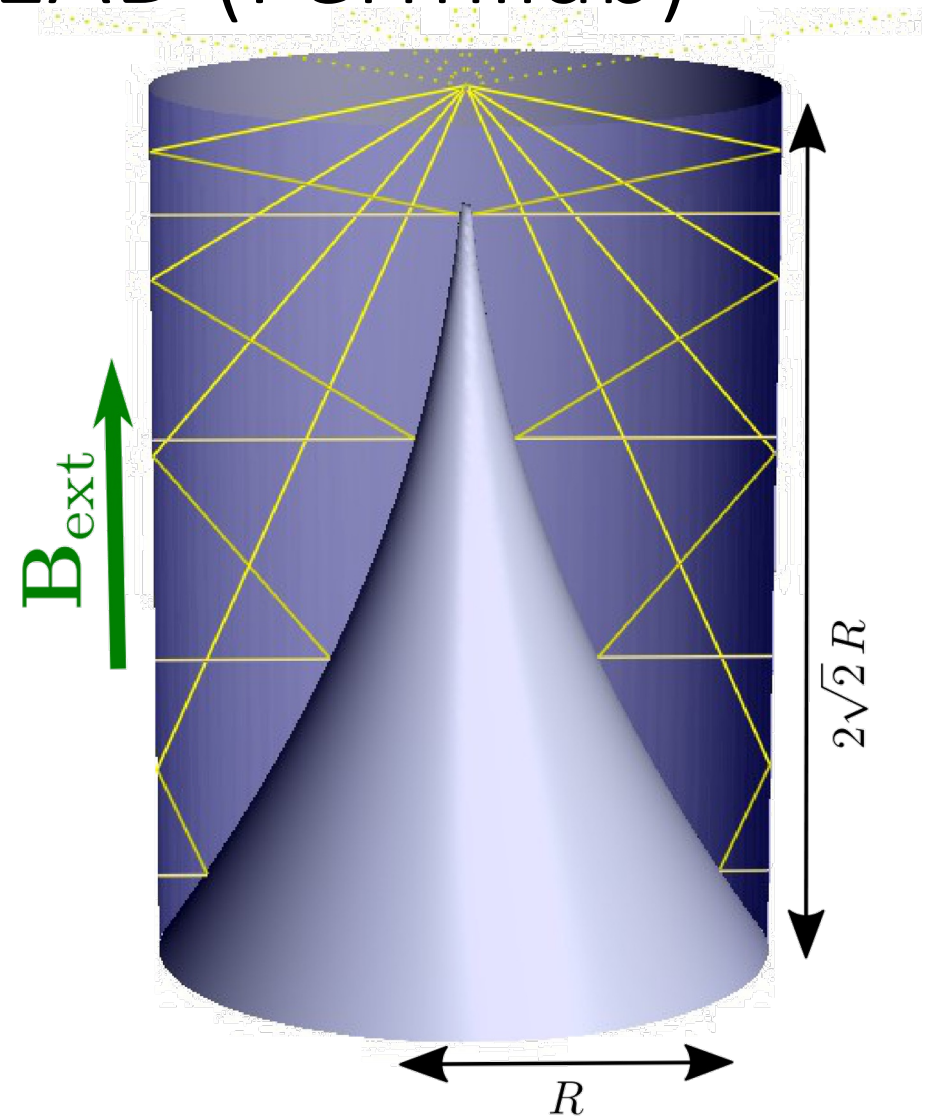
- Axion-photon conversion at the metal-vacuum interface
- Signal enhancement by **larger area**
- Challenge: parallel B-field on the large area of a metal surface

Horns et al, arXiv:1212.2970,
JCAP04(2013)016

BRASS-p (DESY) & BREAD (Fermilab)



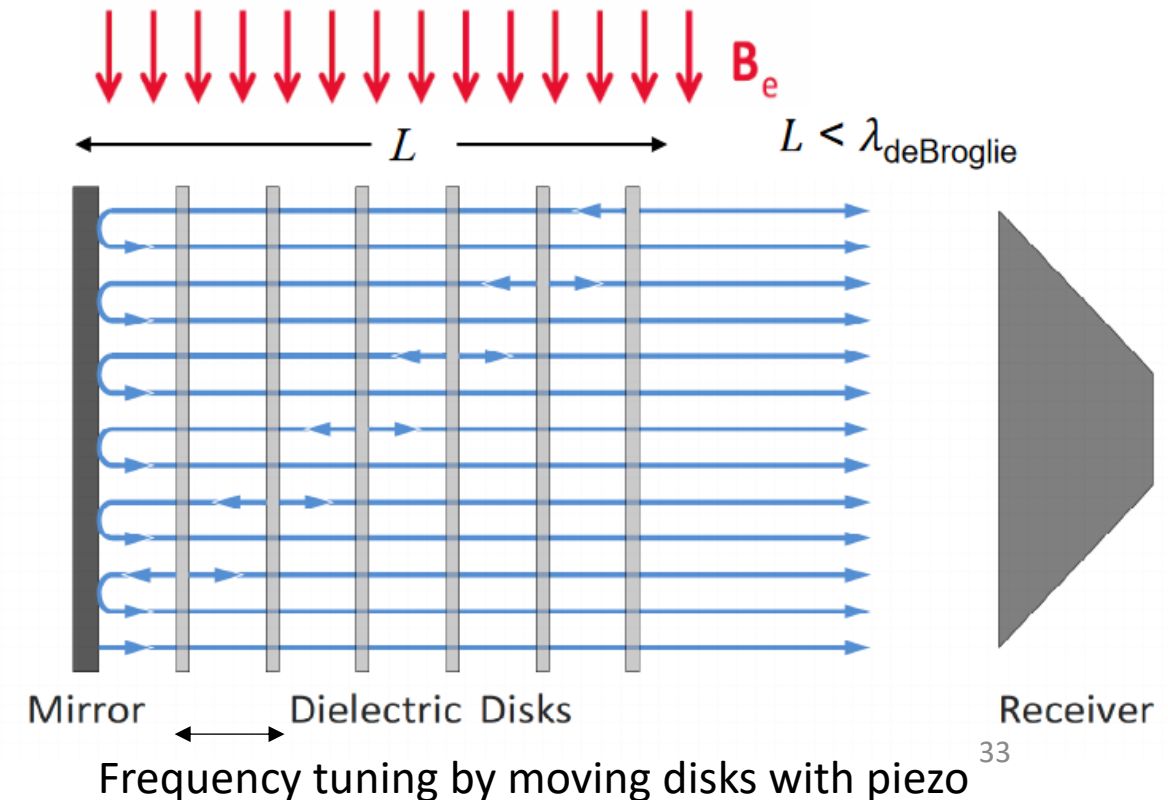
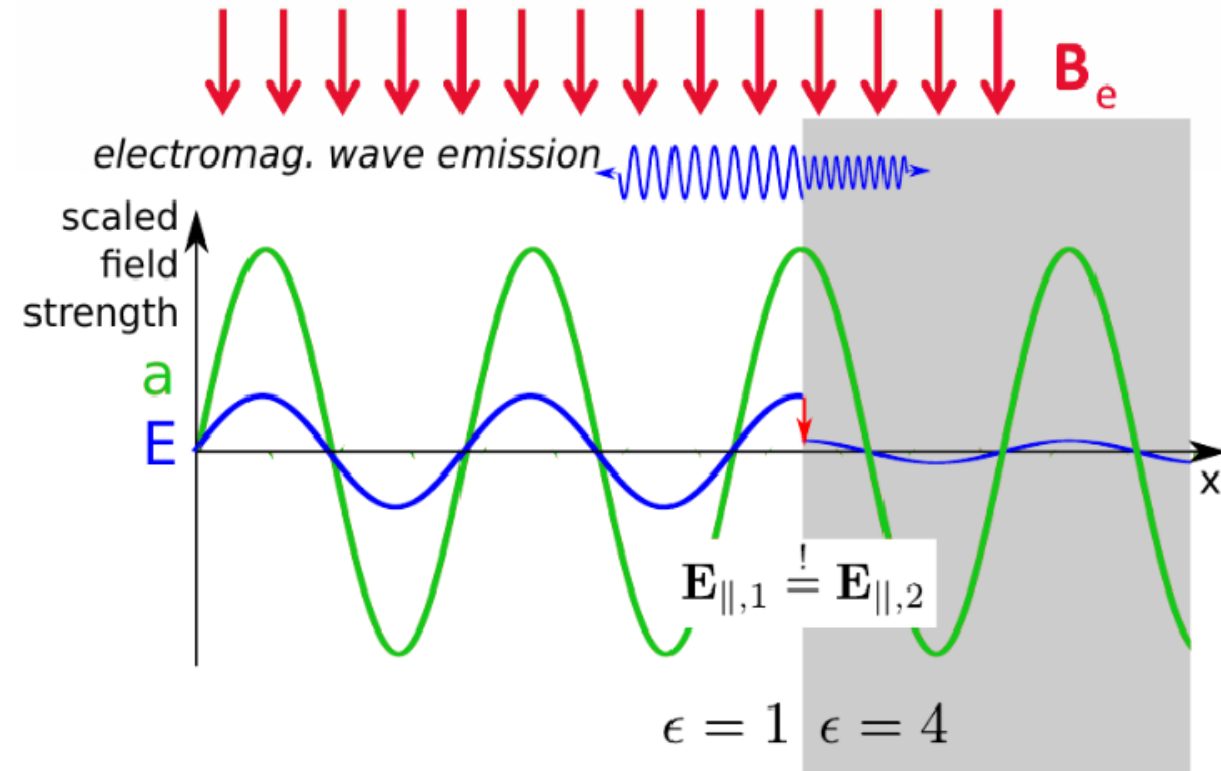
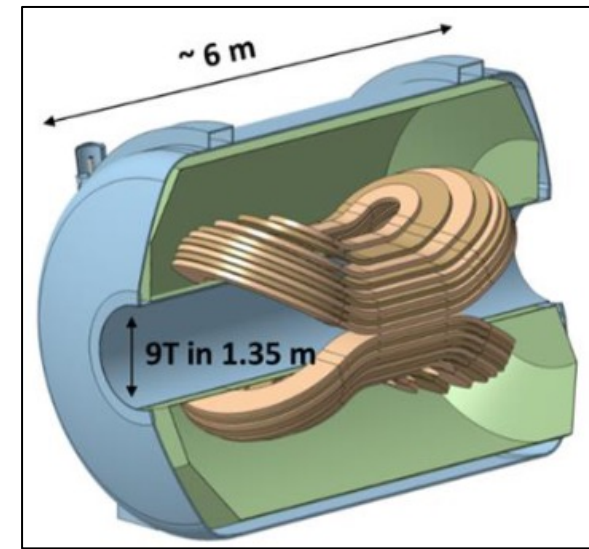
Courtesy: Le Hoang Nguyen, "Development, Calibration and Current Status of the BRASS-p Experiment" PATRAS2022



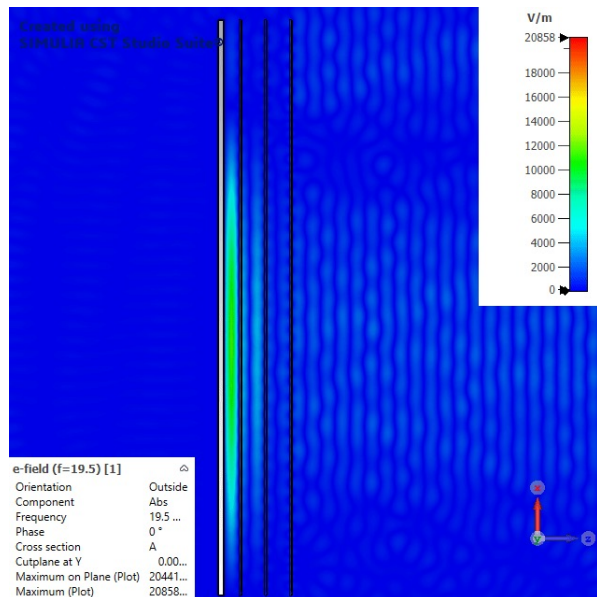
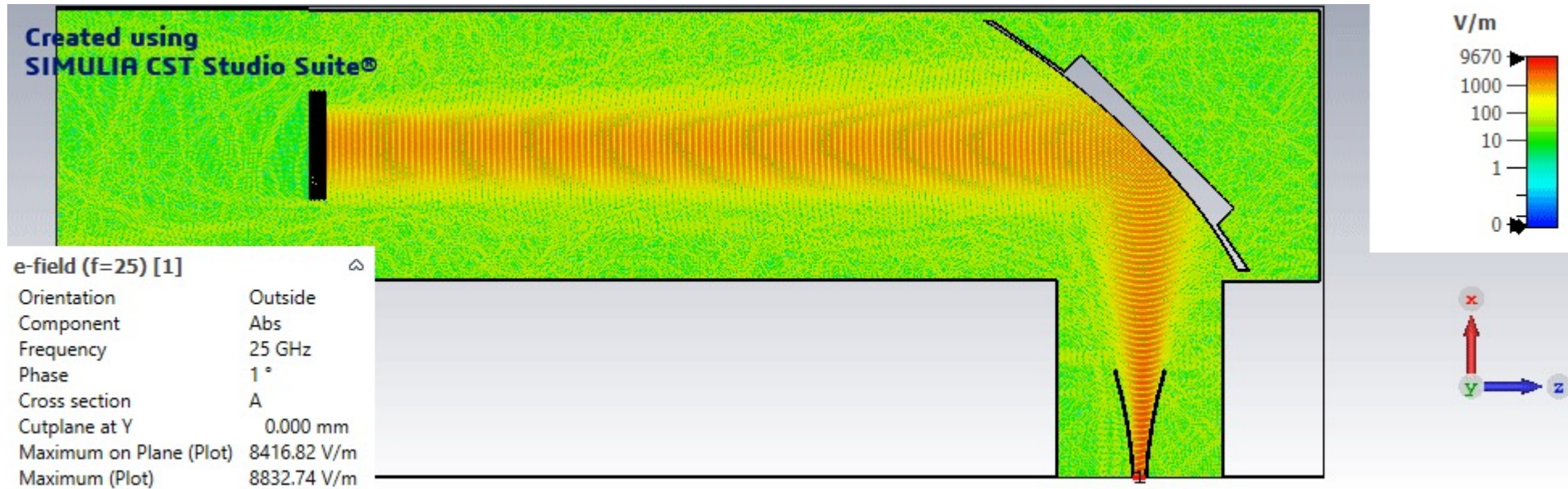
Courtesy: Stefan Knirck, "BREAD: Broadband Reflector Experiment for Axion Detection" PATRAS2022 32

MADMAX: multiple dielectric dishes

- Enhance the coherent microwave signal generated at the dielectric-vacuum surface (**transparent dish antenna**)
- Many disks to **boost** the signal
- Dipole magnet is mandatory



Booster resonance + whole standing wave

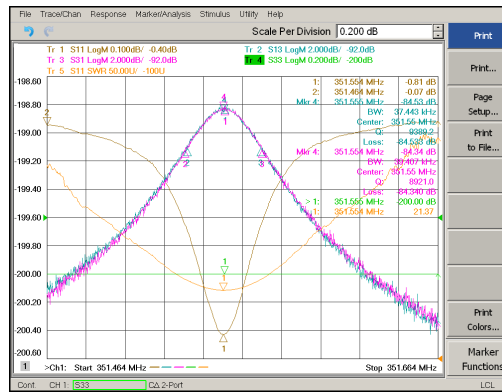
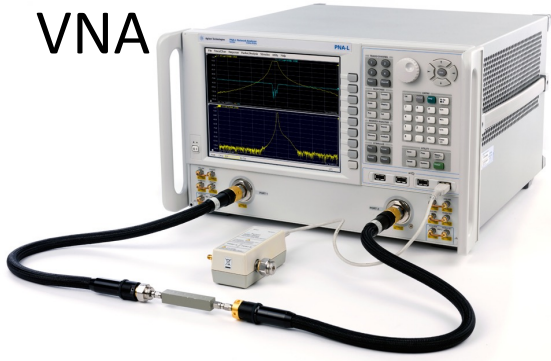


- The resonance inside the booster
- Standing-wave in the whole structure
- White noise resonates (Rayleigh Jeans)
 - Interference to the booster peak
- Very challenging subject in microwave engineering!
 - Enormous mesh in FEM (scale >>>> wavelength)

Boost β in dielectric disks \neq resonance Q in a cavity

Resonant cavity search including plasma haloscope

$$P_S = (1.0 \times 10^{-22} \text{ W}) \times \left(\frac{V}{136L} \right) \left(\frac{B}{6.8 \text{ T}} \right)^2 \left(\frac{C}{0.4} \right) \left(\frac{g_{ay}}{0.97} \right)^2 \left(\frac{\rho}{0.45 \text{ GeV/cm}^3} \right) \left(\frac{f}{650 \text{ MHz}} \right) \boxed{\left(\frac{Q}{50000} \right)}$$



Q: microwave property in a cavity
→ In-situ measurement observable

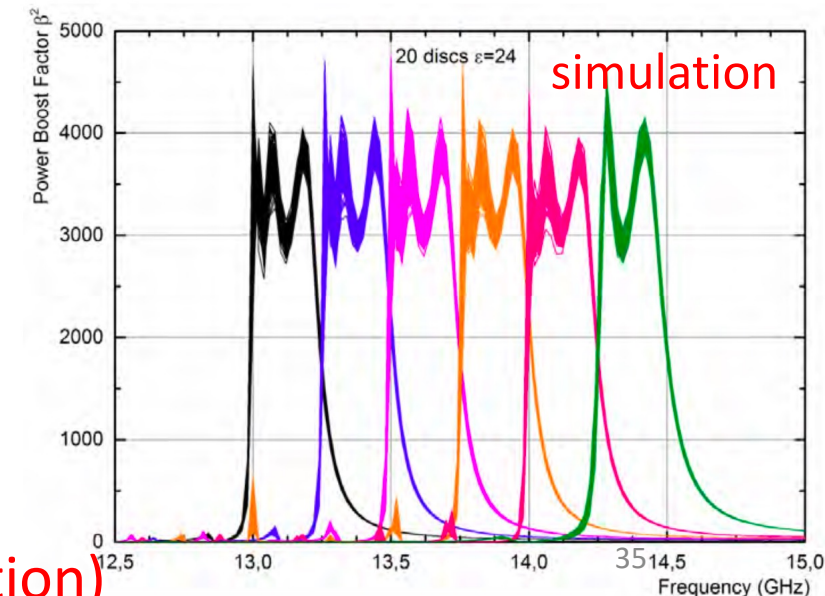
Dielectric-disk haloscope:

$$P_S = (2.2 \times 10^{-27} \text{ W}) \times \left(\frac{A}{1 \text{ m}^2} \right) \boxed{\beta^2} \left(\frac{B}{10 \text{ T}} \right)^2 C_{ay}^2$$

β is defined uniquely for axion interaction not for microwaves

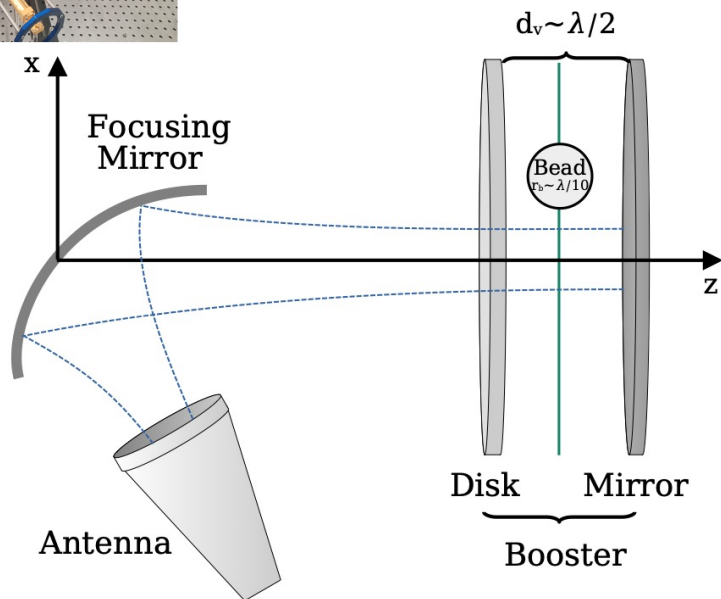
→ Not a direct observable of microwave measurement

→ Indirect calibration and reconstruction via microwave measurements and noise resonance (fitting data with simulation)



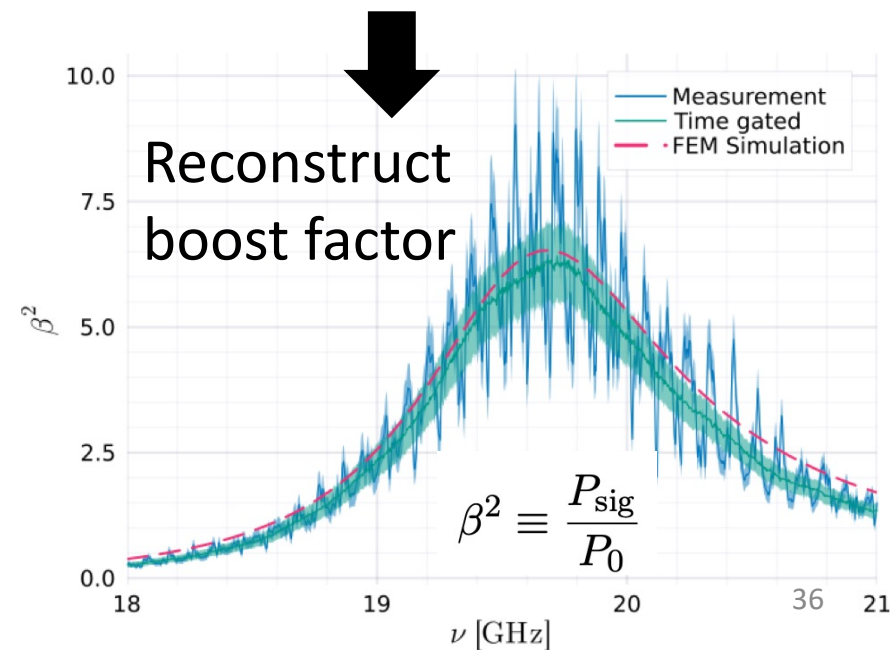
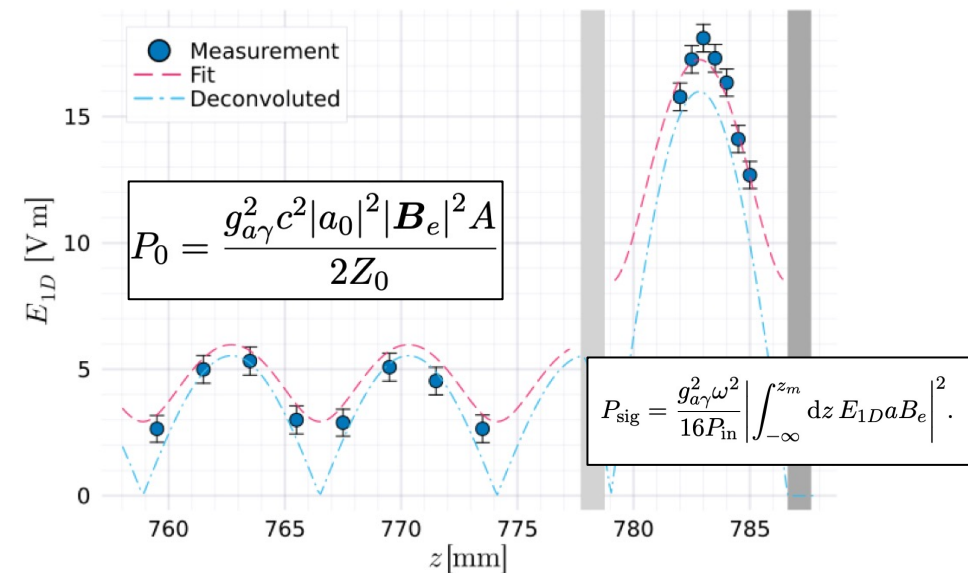
Direct measurement of boost factor

JCAP04(2024)005



Measuring field distribution via bead-pull method

- Direct measurement of microwave field distributions gave consistent results with simulations (Lorentz reciprocity)
- Calibration of boost factor for physics run (to be published):
 - Modeling the system with parameters
 - Fitting reflection data and noise resonance to determine parameters
 - Calculate boost factor (model dependent)
 - was confirmed with this bead-pull method



Prototype experiment at CERN NA

MADMAX at the forefront of the search for axions

The MADMAX experiment at CERN's North Area probes dark matter candidates with two new prototypes

13 MAY, 2024 | By Chetna Krishna

<https://home.cern/news/news/experiments/madmax-forefront-search-axions>

- First physics papers are being prepared
- Dark photon at room temperature, dark photon at cold, axion at room temperature, axion at cold, ...



Stay tuned :-)

Another approach: axion-plasmon mixing in a cavity

$$\boxed{\epsilon} \nabla \cdot \mathbf{E} = \rho - g_{a\gamma} \mathbf{B}_e \cdot \nabla a ,$$

$$\nabla \times \mathbf{H} - \dot{\mathbf{E}} = \mathbf{J} + g_{a\gamma} \mathbf{B}_e \dot{a} ,$$

$$\ddot{a} - \nabla^2 a + m_a^2 a = g_{a\gamma} \mathbf{E} \cdot \mathbf{B}_e ,$$

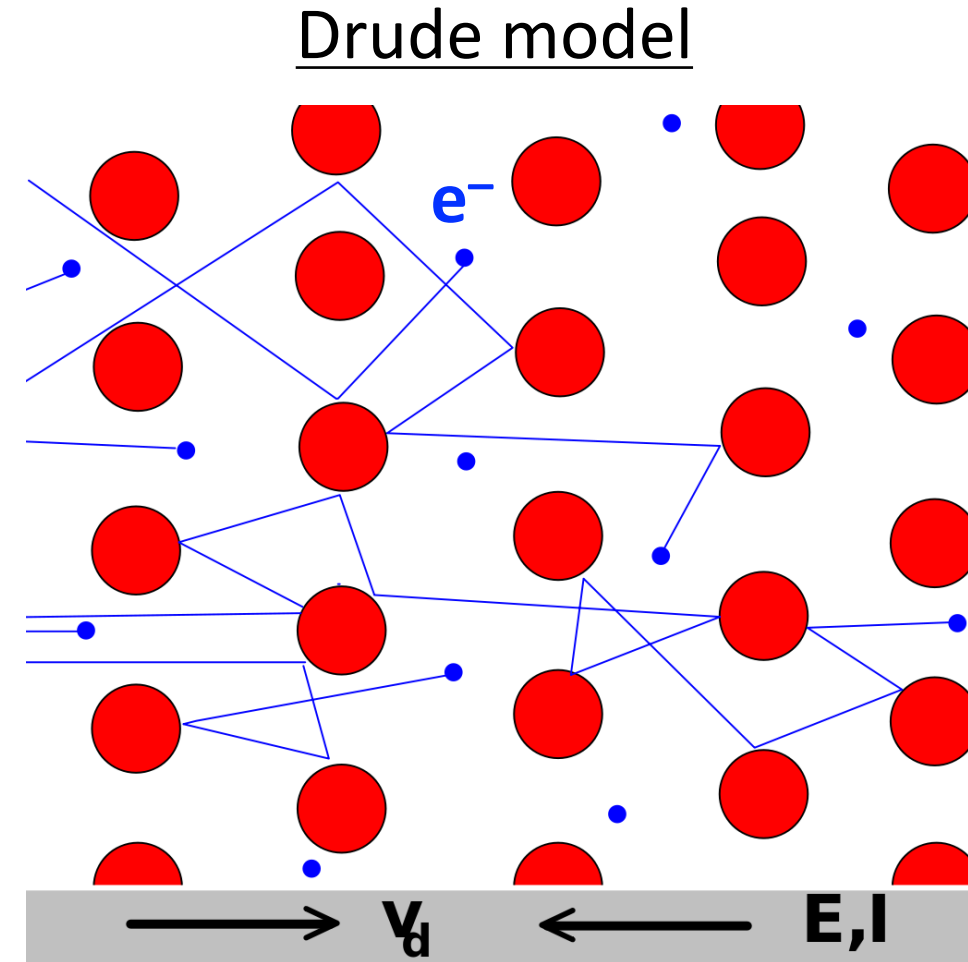
$\epsilon = 0$ gives and resonance inside a plasma

$$\mathbf{E} = -\frac{g_{a\gamma} \mathbf{B}_e a}{\boxed{\epsilon}} = -g_{a\gamma} \mathbf{B}_e a \left(1 - \frac{\omega_p^2}{\omega_a^2 - i\omega_a \Gamma} \right)^{-1}$$

At the plasma frequency $\omega_p = \omega_a$

$$\omega_p = \sqrt{\frac{n_e e^2}{m_e \epsilon_0}}$$

In the Drude model



From wiki

Cavity filled with 1D wire metamaterial

Free electrons inside wires behave as 1D plasma

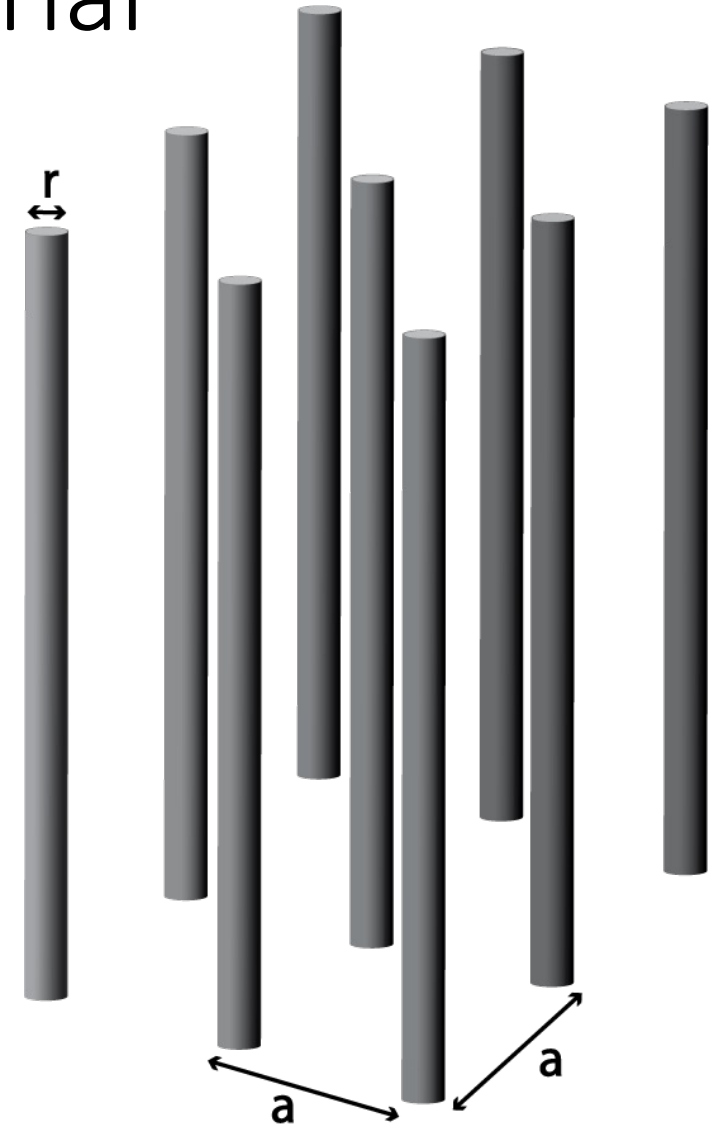
$$n_e = n \frac{\pi r^2}{a^2} \quad ; \quad m_{eff} = \frac{e^2 \pi r^2 n}{2\pi} \log \frac{a}{r} ,$$

$$\omega_p^2 = \frac{n_e e^2}{m_{eff}} = \frac{2\pi}{a^2 \log(a/r)} .$$

For example, $r = 0.5$ mm, $a = 5$ mm gives

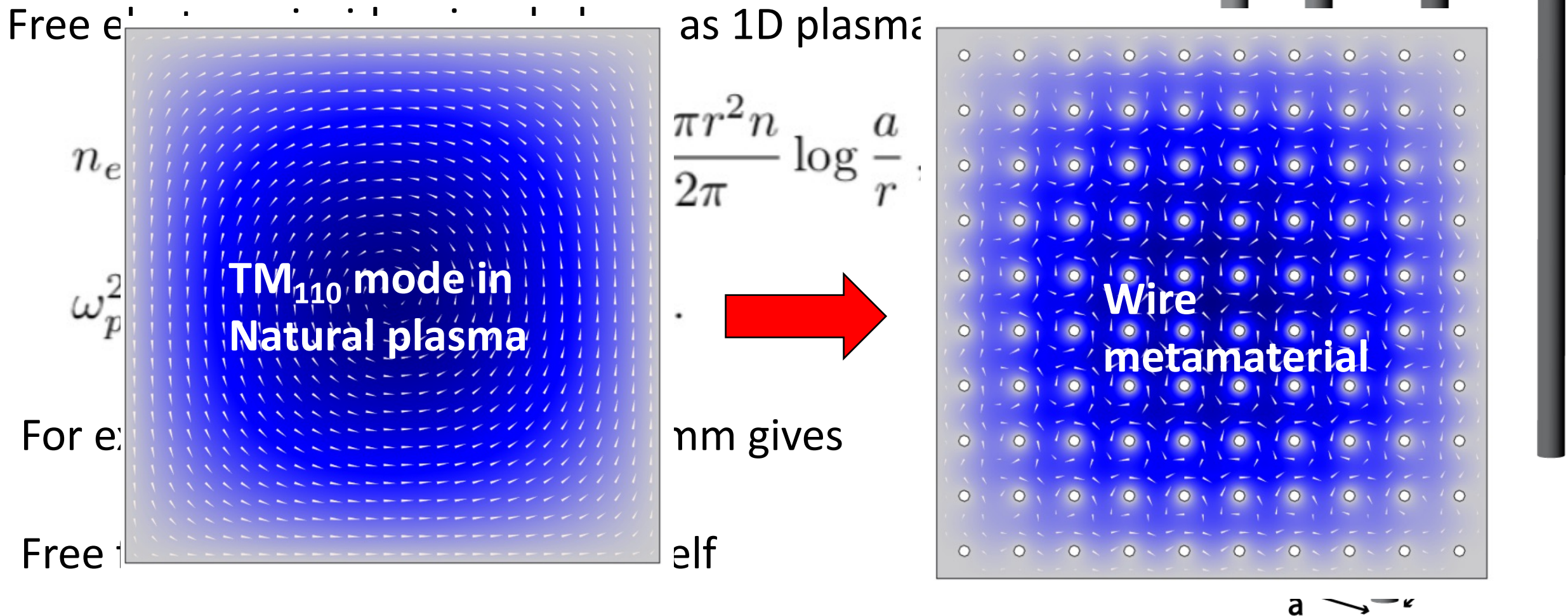
$$\omega_p / 2\pi \sim 16 \text{ GHz}$$

Free from the size of the cavity itself



Changing the spacing a tunes the plasma frequency

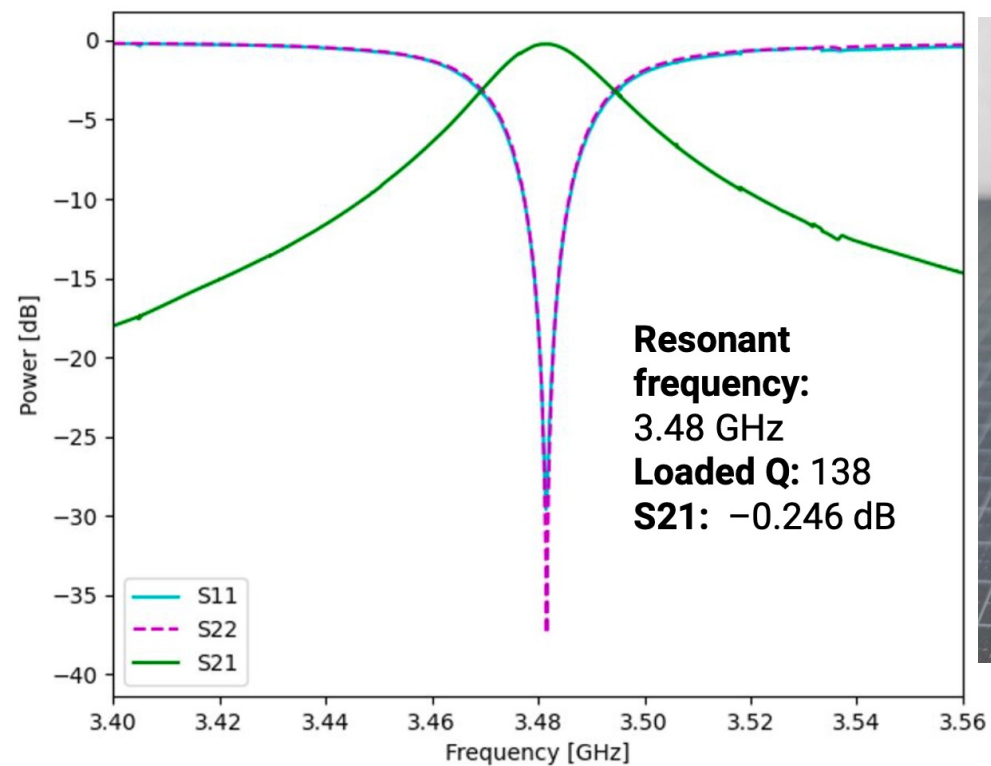
Cavity filled with 1D wire metamaterial



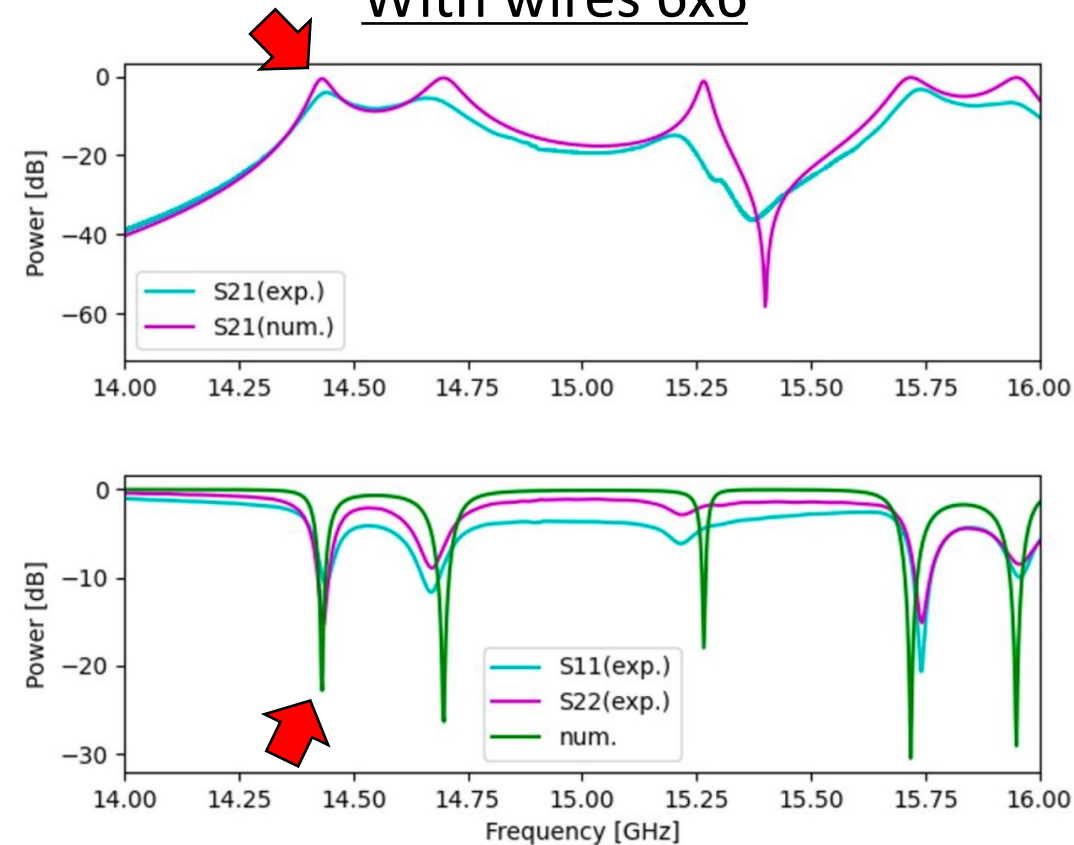
Changing the spacing a tunes the plasma frequency

Prototype wire-filled cavities

Same size, without wires



With wires 6x6



Resonance frequency of the lowest TM mode

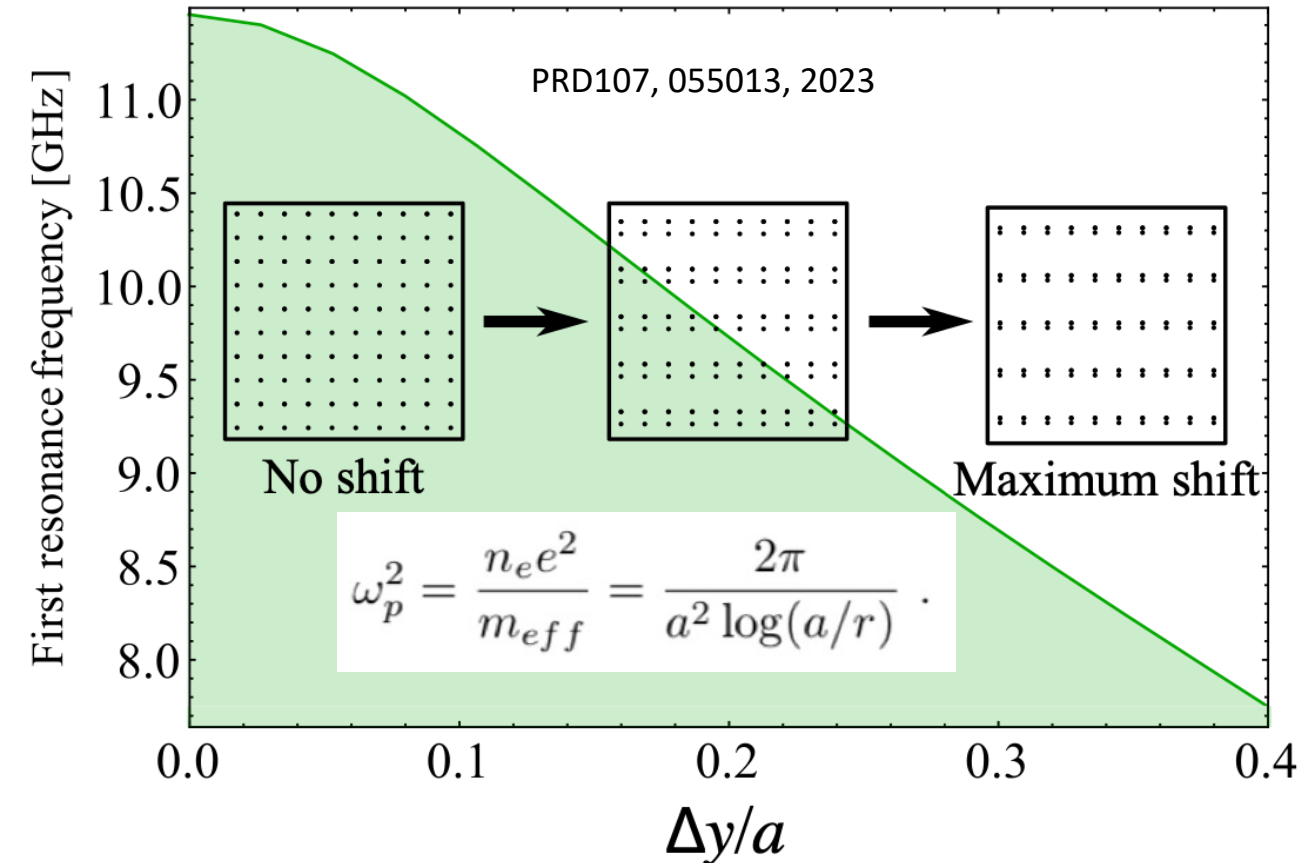
3.48 GHz \rightarrow 14.4 GHz

With the artificial plasma by the wire metamaterial

Courtesy of Gagandeep Kaur

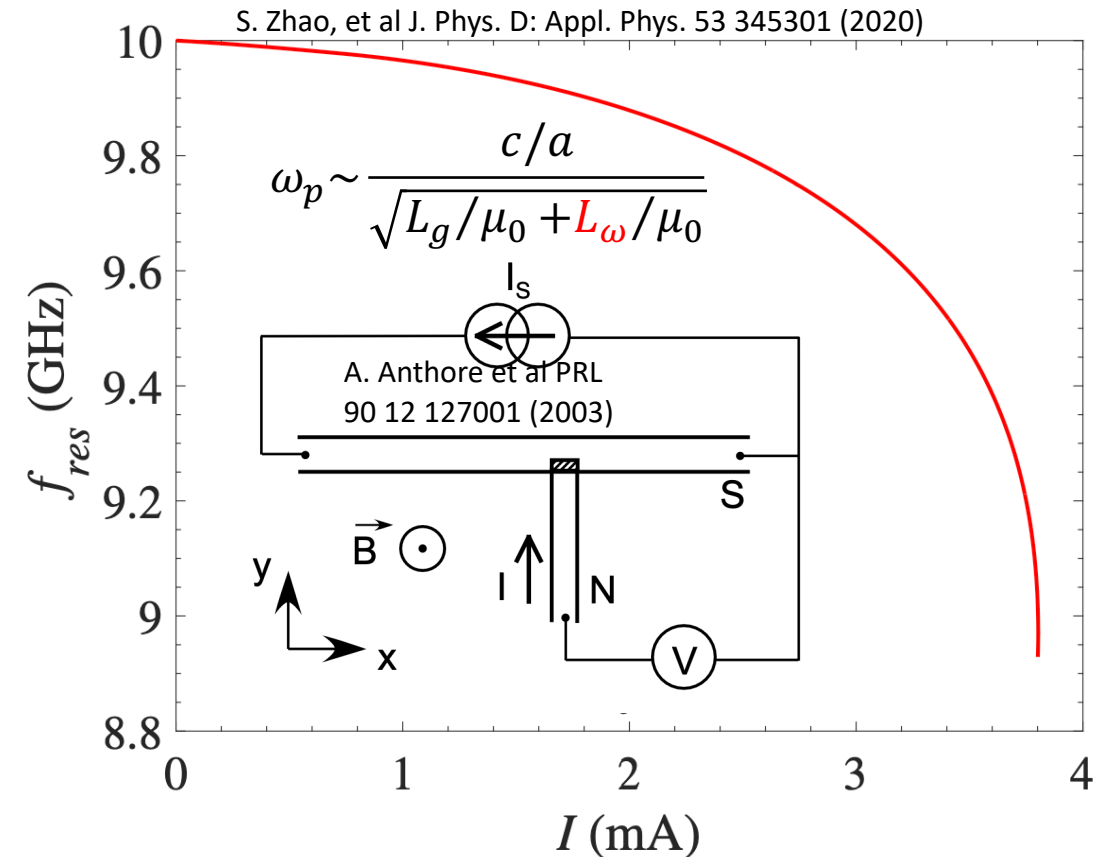
Frequency tuning

Baseline: mechanical tuning



- Copper wires
- Prototyping phase
- First physics run in a few years

Non-mechanical tuning via kinetic inductance



- Superconducting wires + DC current
- Basic R&D for proof-of-principle
- Preliminary studies to be published

Outline

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 - Squeezing (HAYSTAC) and photon counting
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Conclusion

- Microwaves are alternative mean to address new physics
 - Scientific complementarity and technical synergy with accelerator-driven experiments
 - Axion can solve both strong CP problem and dark matter mystery
 - Relatively high-mass dark matter axions may be free from naturalness problems
 - Dark matter axions are treated as classical waves not particles
- Recent dark matter axions searches (< 10 GHz) profit from state-of-the-art microwave detector technology
 - ADMX reached SQL via JPA
 - HAYSTAC introduced phase-sensitive operation of JPA to overcome SQL via squeezing
 - Potential in single photon counting (wave \rightarrow particle)
- One research direction is toward higher frequency
 - Challenge in keeping volume constant while increasing the frequency
 - BRASS/BREAD gives sensitivity proportional to surface area
 - MADMAX boosts the sensitivity via dielectric disks; 1st physics results to be published
 - ALPHA employs artificial plasma frequency via wire metamaterial; R&D on-going towards physics run

backup

Blackbody radiation

$$\bar{n} = \frac{1}{\exp(\hbar\omega/k_B T) - 1}$$

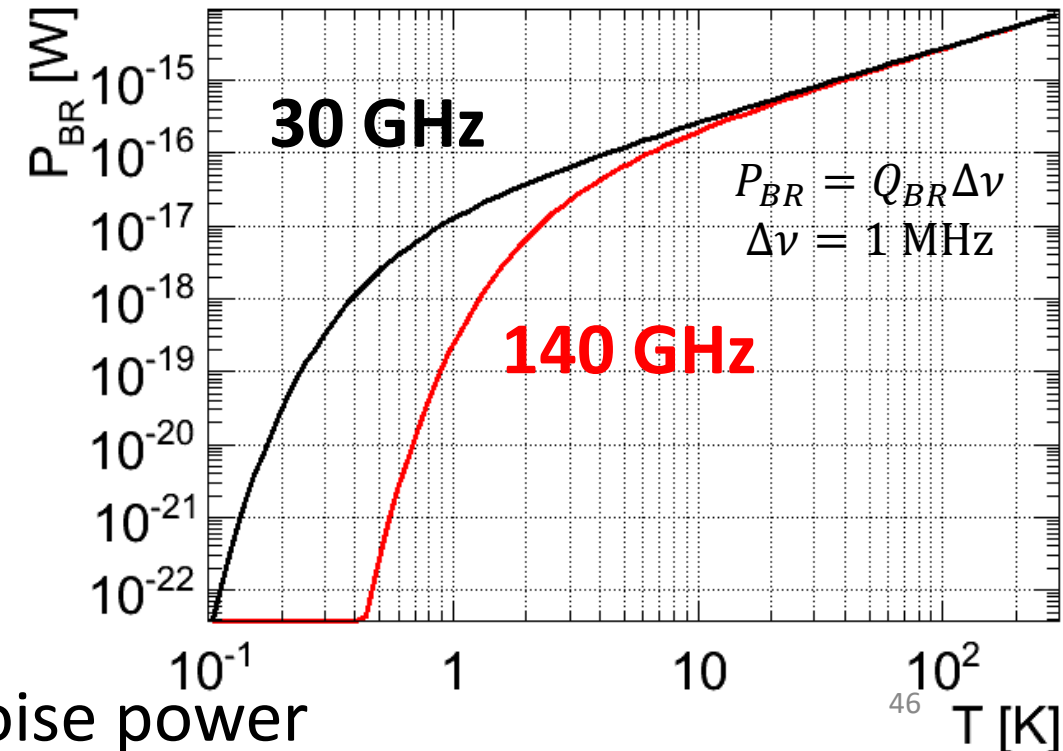
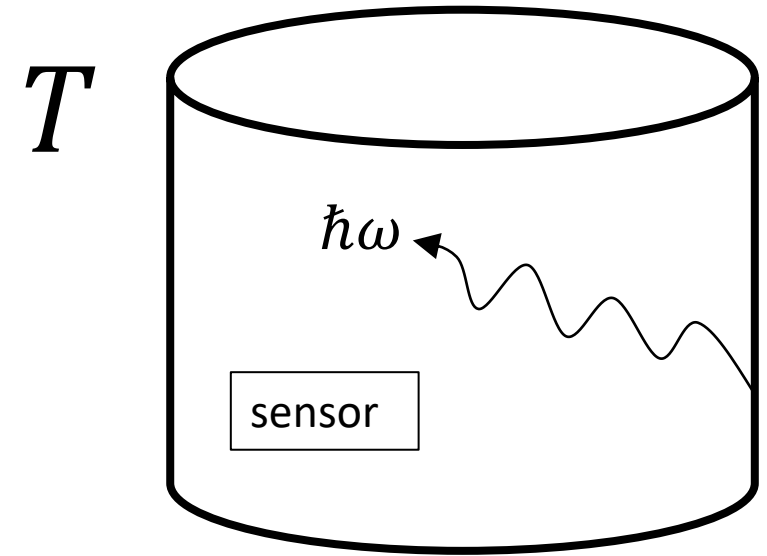
$$\hat{\rho}_{th} = \frac{1}{1 + \bar{n}} \sum_{n=0}^{\infty} \left(\frac{\bar{n}}{1 + \bar{n}} \right)^n |n\rangle \langle n|$$

Noise power spectral density

$$Q_{BR} = \frac{1}{2} \Omega A \frac{2h\nu^3}{\exp\left(\frac{h\nu}{k_B T}\right) - 1} \text{ [W/Hz]}$$

Solid angle Ω [st]

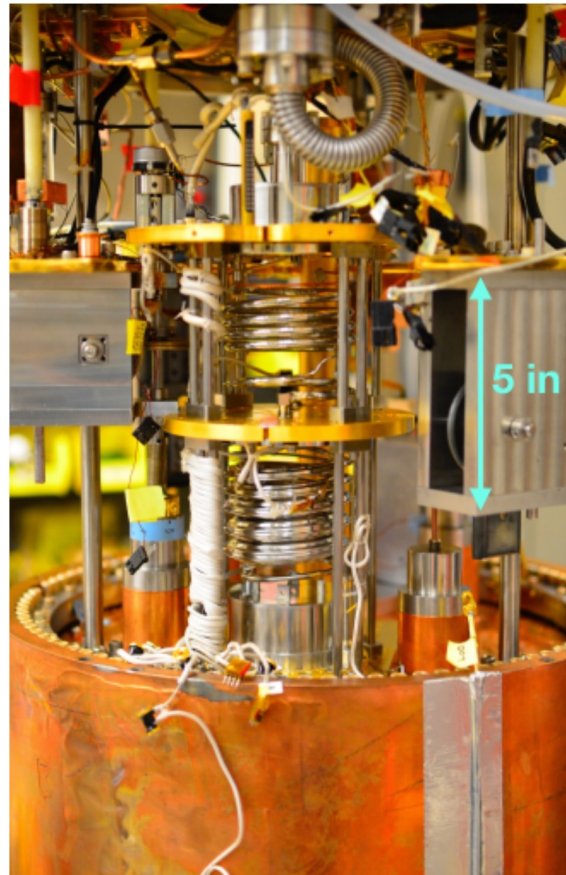
Sensor area A [m^2] \rightarrow Usually, $\Omega A \sim \lambda^2$



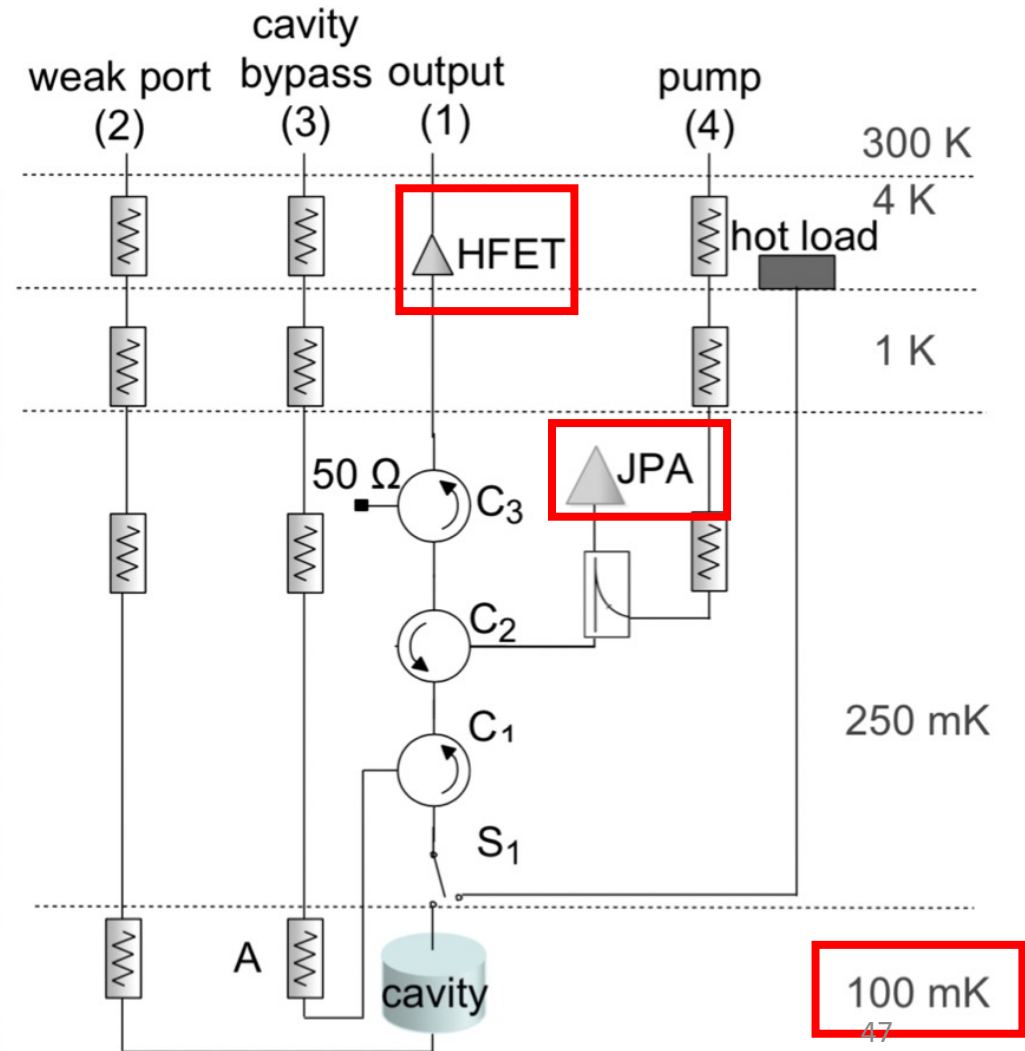
Cooling down the system can decrease the noise power

ADMX again: $T_{SQL} = h\nu/k_B \sim 40 \text{ mK}$

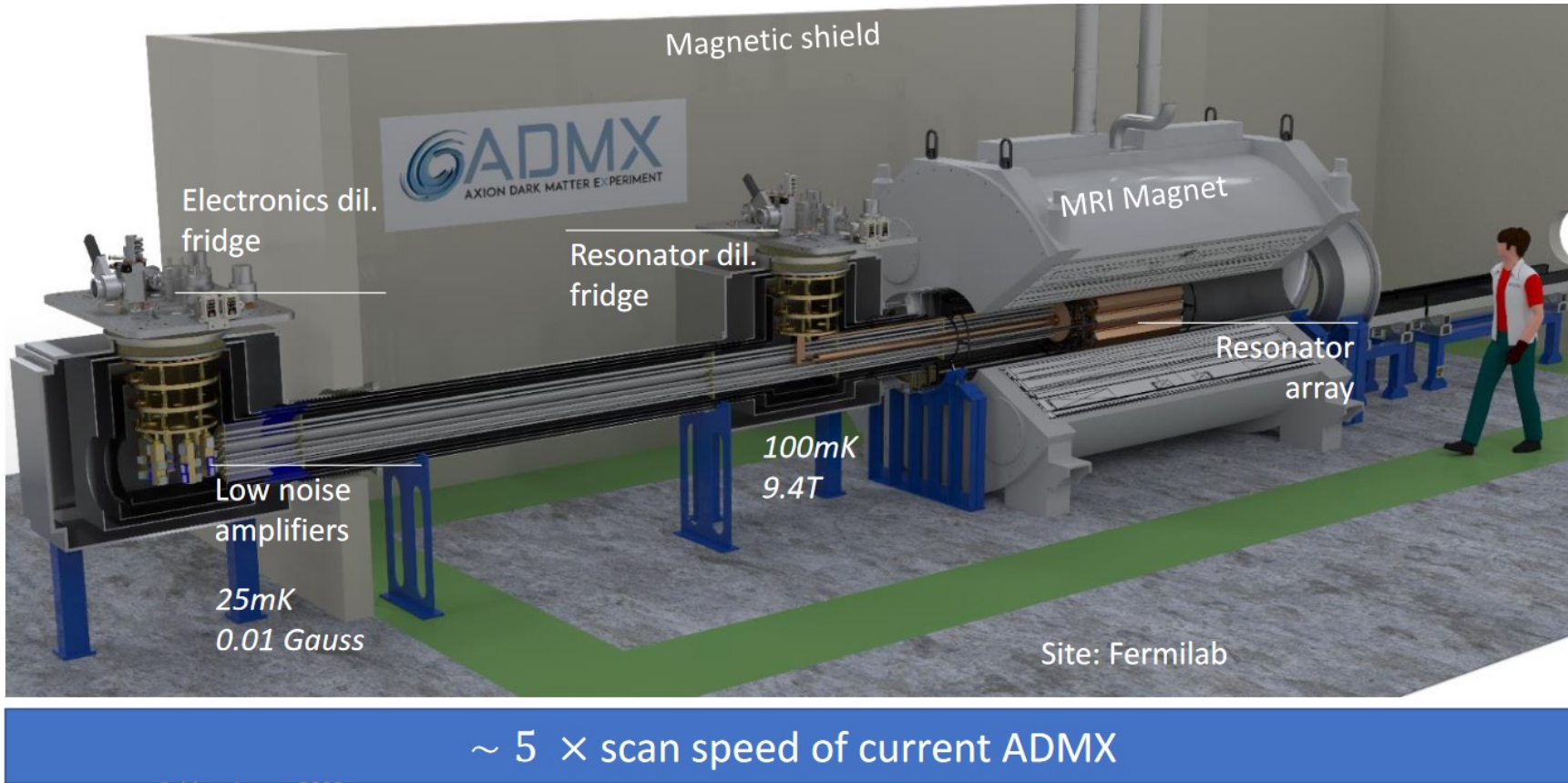
With a dilution refrigerator, the noise level is approaching to the quantum limit
 → Quantum devices have been developed and implemented
 → Toward quantum microwave optics of coherent signals



Run 1B

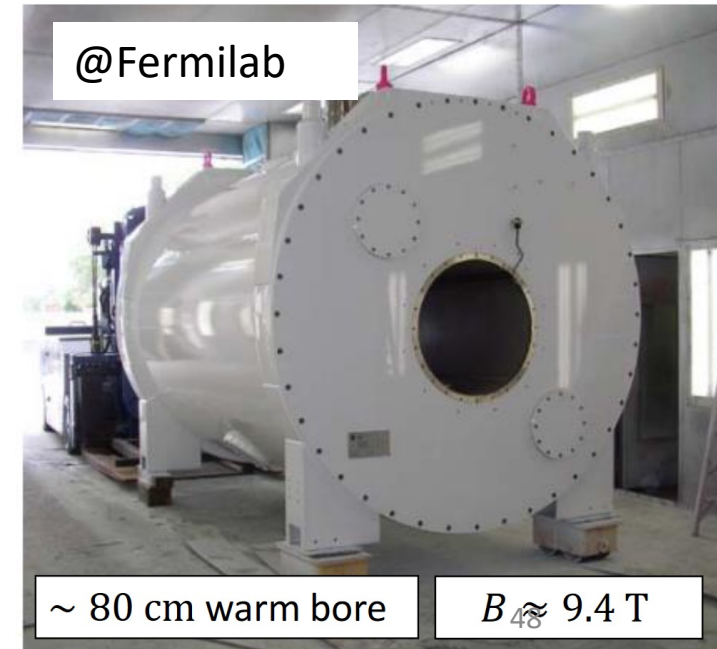


ADMX (Washington University → Fermilab)



ADMX-EFR

Multiple
cavities to
address
heavier axions



Challenge: phase lock of all the cavities (S. Knirck)

CAST-CAPP @ CERN



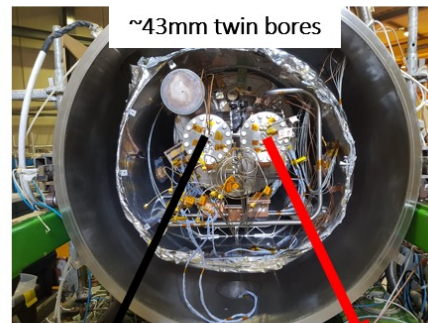
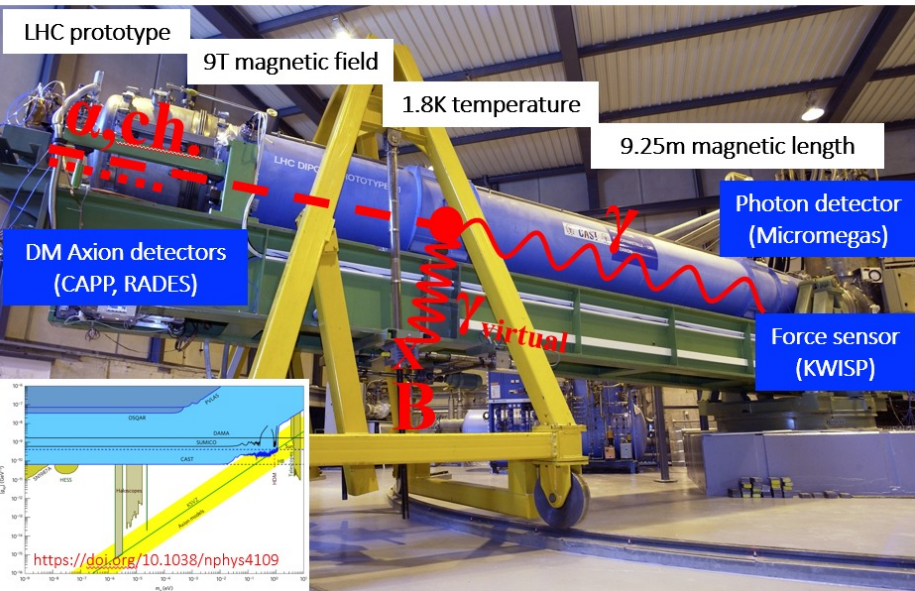
CAST EVOLUTION

3 / 17

Axion Helioscope
(Solar Axions)

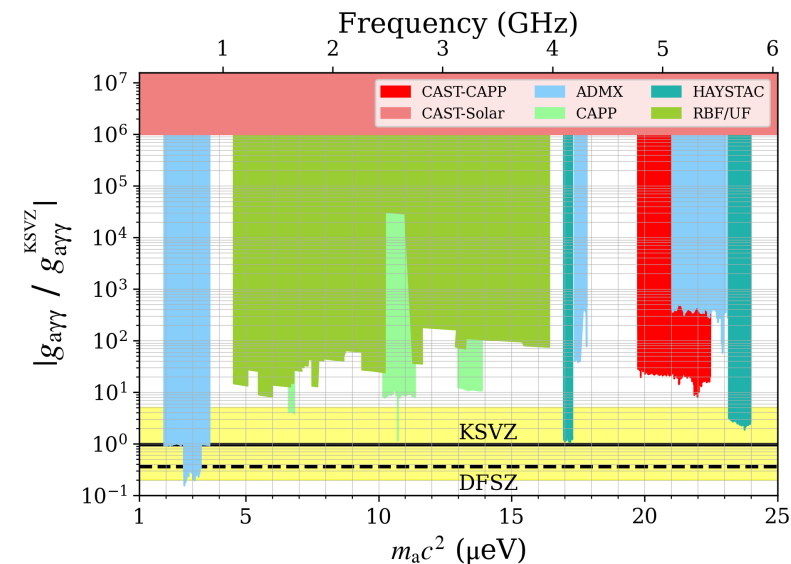
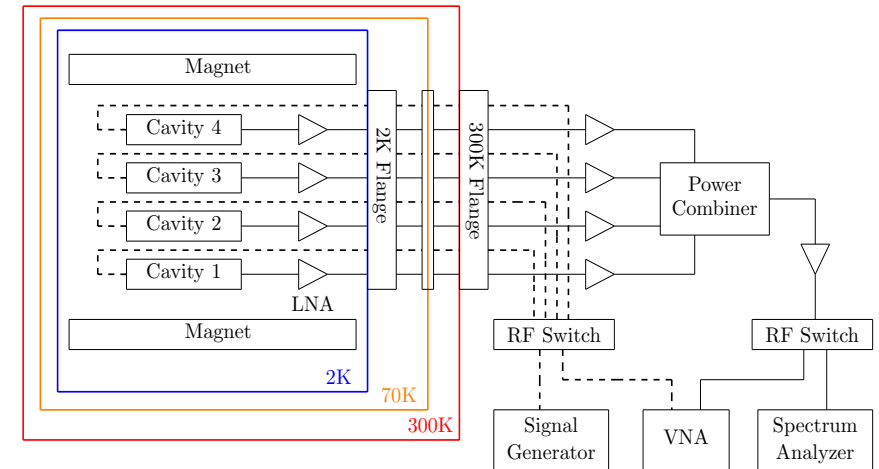
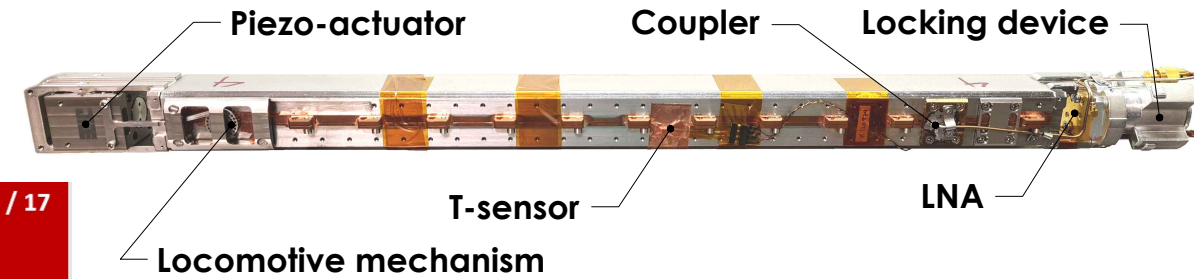
2019

Axion Haloscope
(Dark Matter Axions)



CAST-RADES

CAST-CAPP



Courtesy: Marios Maroudas, "LATEST RESULTS ON DARK MATTER AXIONS WITH CAST-CAPP"

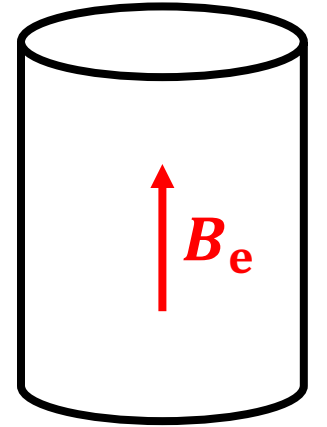
→ Multiple cavity option with a recycled magnet

Natural plasma (ionized gas, free e^- in metal, etc) in a cylinder

$$\mathbf{B} = \mathbf{B}_t + B_z \hat{\mathbf{z}}; \quad \mathbf{E} = \mathbf{E}_t + E_z \hat{\mathbf{z}}; \quad \mathbf{B}_e = B_e \hat{\mathbf{z}},$$

$$\left(\nabla_t + \frac{\partial}{\partial z} \hat{\mathbf{z}} \right) \times (\mathbf{B}_t + B_z \hat{\mathbf{z}}) = -i\omega (\mathbf{E}_t + \epsilon_z E_z \hat{\mathbf{z}}) - i\omega g_{a\gamma} a B_e \hat{\mathbf{z}},$$

$$\left(\nabla_t + \frac{\partial}{\partial z} \hat{\mathbf{z}} \right) \times (\mathbf{E}_t + E_z \hat{\mathbf{z}}) = i\omega (\mathbf{B}_t + B_z \hat{\mathbf{z}}).$$



$$\longrightarrow \frac{\omega^2}{\omega^2 - k^2} \left(r^2 \frac{\partial^2 E_z}{\partial^2 r} + r \frac{\partial E_z}{\partial r} \right) + r^2 \omega^2 \epsilon_z E_z + r^2 \omega^2 g_{a\gamma} B_e a = 0,$$

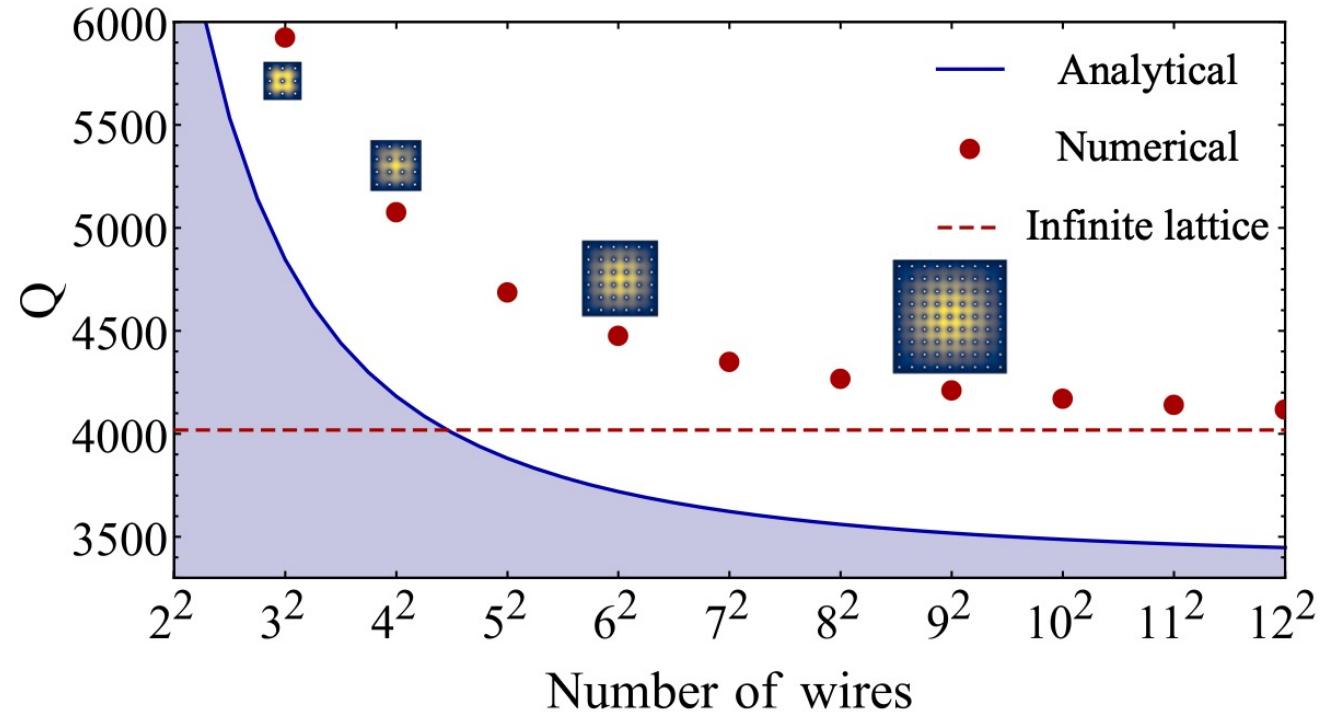
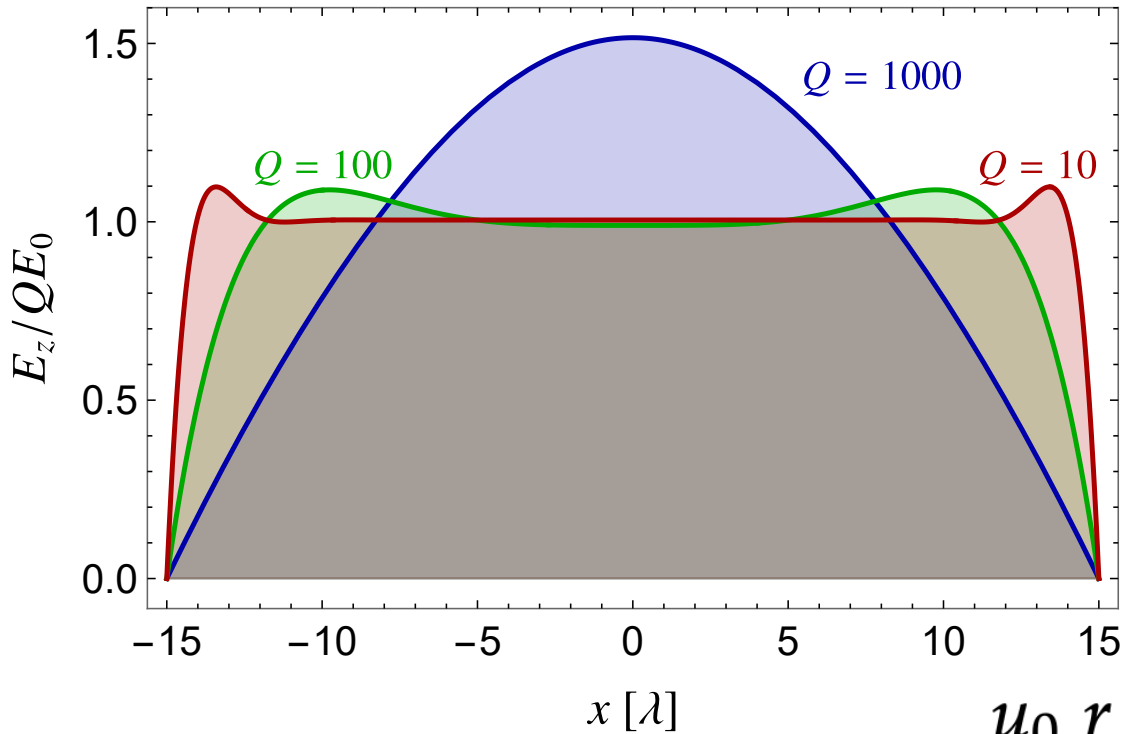
Transverse magnetic mode (TM modes) couples to axions at higher frequency

However, ***natural*** plasma is

- Not suitable in a cryogenic environment
- ω_p is not tunable to scan m_a

} \rightarrow ***Artificial*** plasma by metamaterial ₅₀

Influence of cavity quality factor

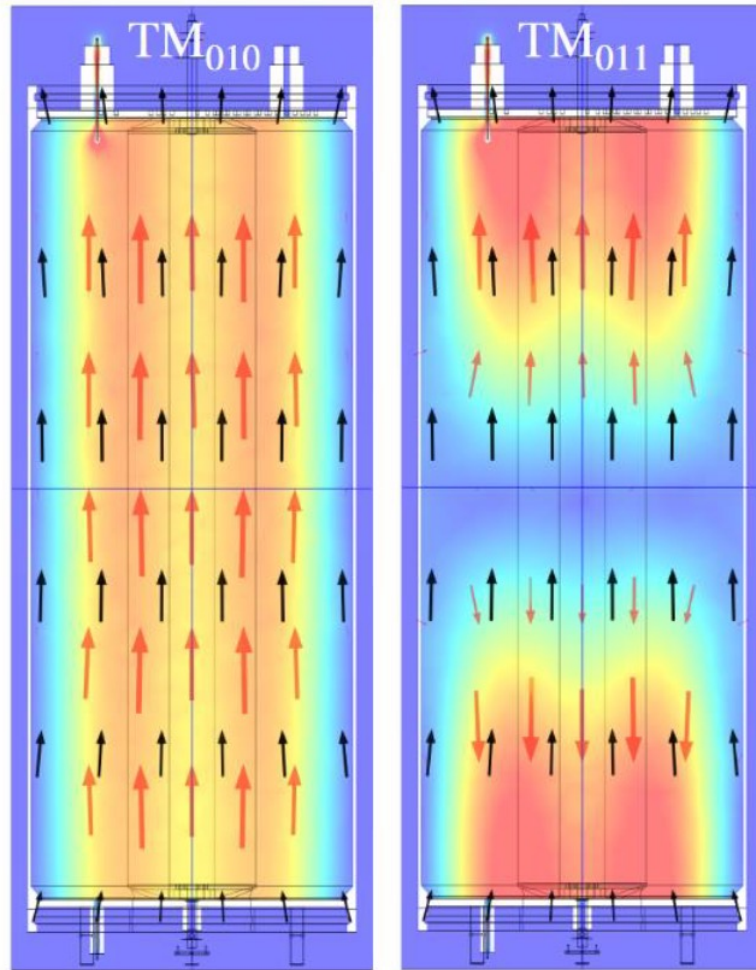


$$Q \simeq 2 \frac{\mu_0 r}{\mu \boxed{\delta}} \left(\log \frac{a}{2\pi r} + F \right)$$

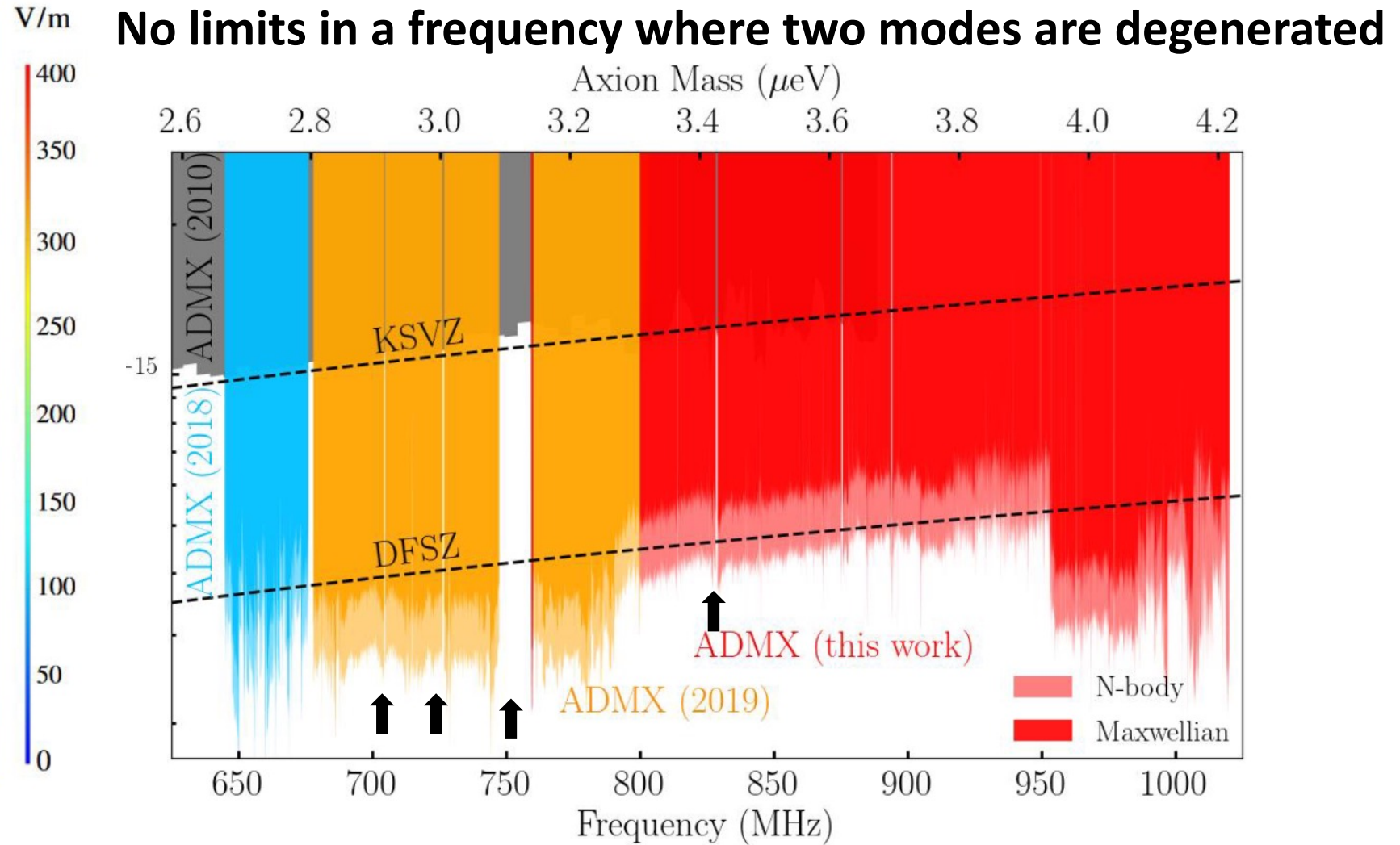
Skin depth

- Denser wires \rightarrow Lower Q dominated by wire loss \rightarrow uniform distribution
- Higher $Q \rightarrow$ Simpler cavity like behavior

One important lesson from ADMX



Courtesy: Gray Rybka, "Current Status and Future Plans of ADMX"



The same and much severer issues in plasma haloscope