

Amplifiers in systems

- **Amplification**

- single gain stage rarely sufficient

- add gain to avoid external noise eg to transfer signals from detector

- practical designs depend on detailed requirements

- constraints on power, space,... cost in large systems

- e.g. ICs use limited supply voltage which may constrain dynamic range

- **Noise will be an important issue in many situations**

- most noise originates at input as first stage of amplifier dominates

- often refer to Preamplifier = input amplifier

- may be closest to sensor, subsequently transfer signal further away

- **In principle, several possible choices**

- V sensitive

- I sensitive

- Q sensitive

Voltage sensitive amplifier

- As we have seen many sensors produce current signals but some examples produce voltages - thermistor, thermocouple,...
op-amp voltage amplifier ideal for these
especially slowly varying signals - few kHz or less
- For sensors with current signals voltage amplifier usually used for secondary stages of amplification

•Signal $V_{out} = Q_{sig}/C_{tot}$

C_{tot} = total input capacitance

C_{tot} will also include contributions from wiring and amplifier

V_{out} depends on C_{tot}

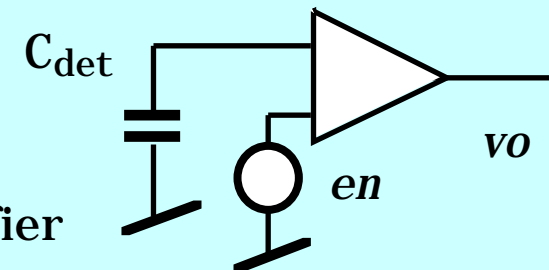
not desirable if C_{det} is likely to vary

eg with time, between similar sensors, or depending on conditions

- Noise to be discussed more later

contribution from amplifier, and possibly sensor

$S/N = Q_{sig}/(C_{tot} \cdot v_{noise})$ can it be optimised?



Current sensitive amplifier

- Common configuration, eg for photodiode signals

$$V_{out} = -AV_{in}$$

$$V_{in} - V_{out} = i_{in}R_f$$

$$V_{out} = -[A/(A+1)] \cdot i_{in}R_f \quad -i_{in}R_f$$

- Input impedance

$$V_{in} = i_{in}R_f/(A+1) \quad Z_{in} = R_f/(A+1)$$

- Effect of C & R_{in} - consider in frequency domain

$$v_0 = i(1/j \quad C \parallel R_{in})$$

$$= i(\quad)R/(1 + j \quad)$$

input signal convoluted with falling exponential

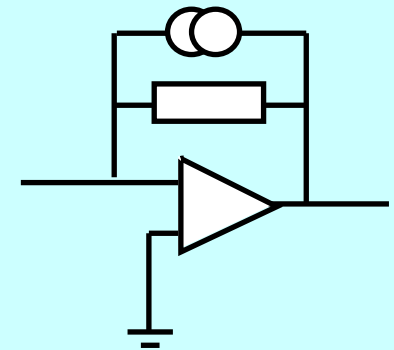
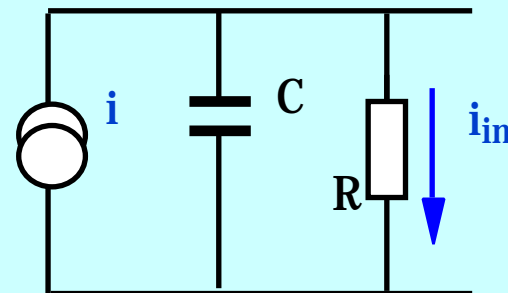
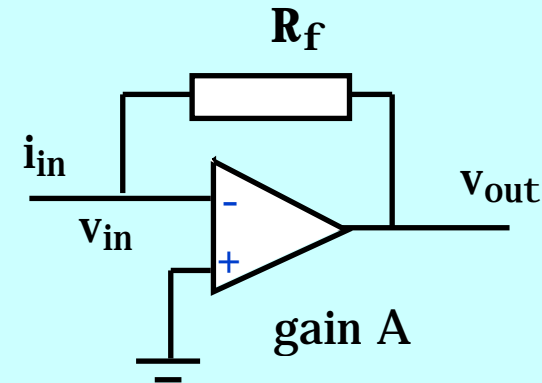
increasing R_f to gain sensitivity will increase

fast pulses will follow input with some broadening

- Noise

will later find that feedback resistor is a noise source

contributes current fluctuations at input $\sim 1/R_f$



Charge sensitive amplifier

- Ideally, simple integrator with C_f
but need means to discharge capacitor - large R_f
- Assume amplifier has Z_{in} very high (usual case)

$$V_{out} = -AV_{in}$$

$$V_{out} - V_{in} = i_{in}/j \omega C_f$$

$$V_{out} = -[A/(A+1)] \cdot i_{in}/j \omega C_f \quad i_{in}/j \omega C_f$$

$$\Rightarrow -Q/C_f$$

- Input impedance

$$v_{in} = i_{in}/(A+1)j \omega C_f \quad C=(A+1)C_f \text{ at low } f$$

so amplifier looks like large capacitor to signal source

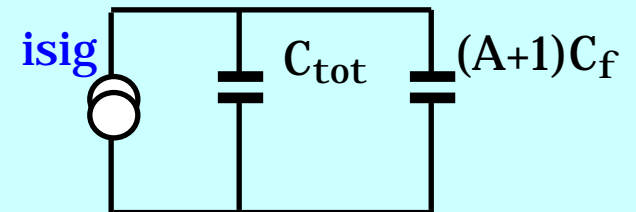
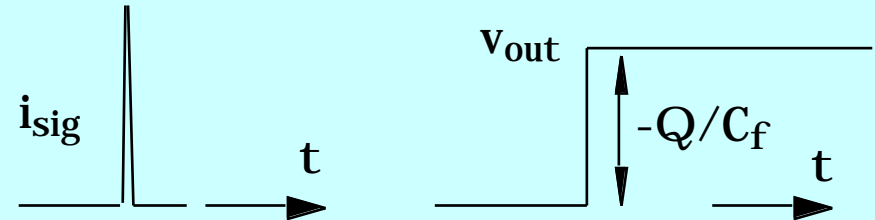
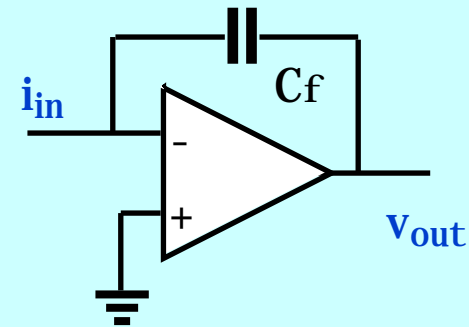
low impedance but some charge lost

$$Q_A = Q/[1 + C_{tot}/(A+1)C_f]$$

e.g. $A = 10^3 \quad C_f = 1\text{pF}$

$C_{tot} = 10\text{pF} \quad Q_A/Q = 0.99$

$C_{tot} = 100\text{pF} \quad Q_A/Q = 0.90$



Feedback resistance

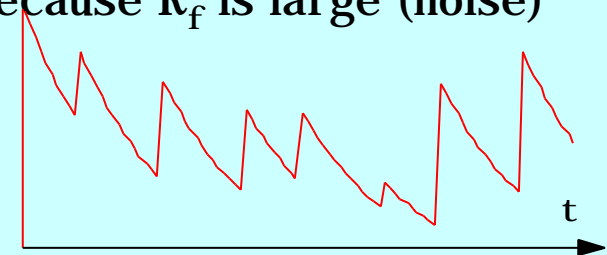
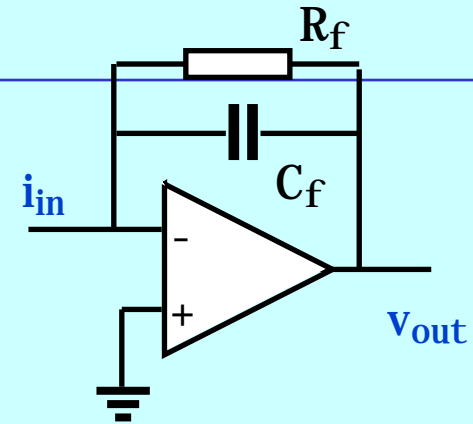
- Must have means to discharge capacitor so add R_f

$$Z_f = R_f || 1/j \omega C_f$$

$$V_{out} = -[A/(A+1)] \cdot i_{in} Z_f$$

$$= i_{in} R_f / (1 + j \omega R_f C_f) \quad \tau_f = R_f C_f$$

step replaced by decay with $\sim \exp(-t/R_f C_f)$ is long because R_f is large (noise)
 easiest way to limit pulse pileup - differentiate
 ie add high pass filter



- Pole-zero cancellation

exponential decay + differentiation => unwanted baseline undershoot

introduce canceling network

$$v_0 = 1/(1 + j \omega \tau_f)$$

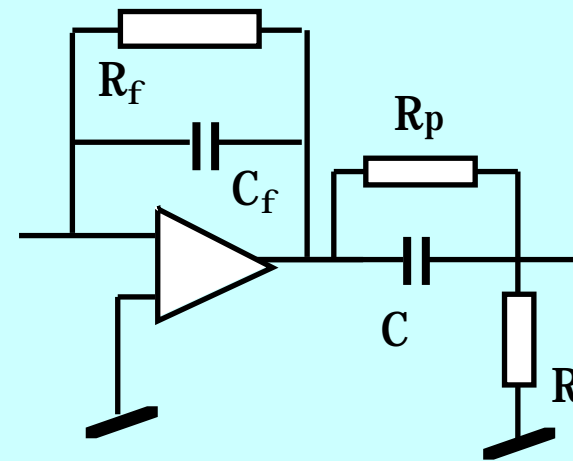
$$v_1 = 1/(1 + j \omega \tau_f)(1 + j \omega \tau_1)$$

$$\tau_1 = RC < \tau_f$$

add resistor R_p so $R_p C = \tau_f$

then

$$v_1' = 1/(1 + j \omega \tau_3) \quad \text{with} \quad \tau_3 = (R || R_p)C < \tau_f$$



Effect of finite bandwidth

• Realistic input stage of amplifier

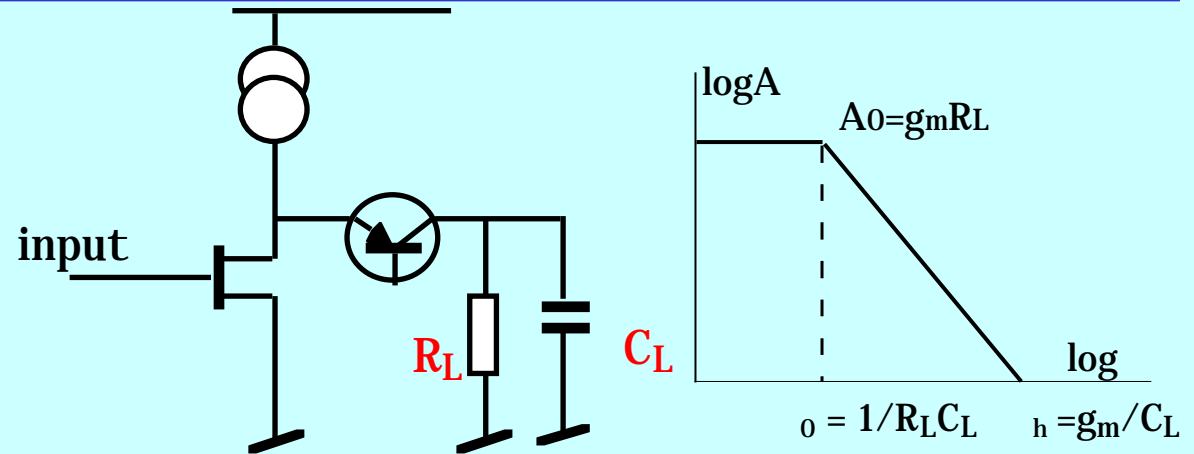
$$v_{out} = i_d(R_L || C_L) \quad i_d = g_m v_{in}$$

$$A = g_m R_L \quad \text{low } f$$

$$A = g_m / j \omega C_L \quad \text{high } f$$

(NB phase change)

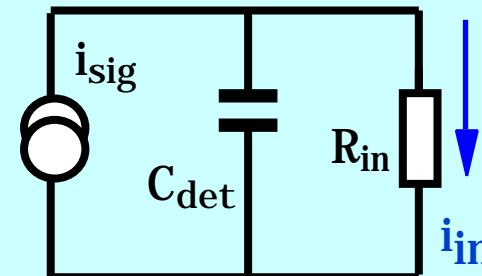
$$Z_{in} = 1/A \quad C_f = C_L / g_m \quad C_f \text{ resistive!}$$



Irrespective of detailed design

$$A = A_0 \frac{\omega_h}{j\omega} \quad \omega_h = \text{gain-bandwidth product}$$

$$= 1/A_0 \frac{1}{j\omega C_f}$$



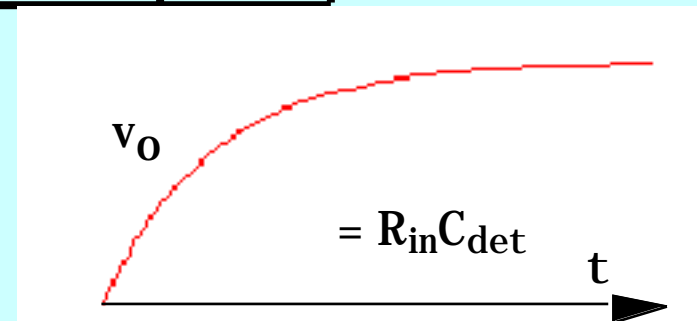
• Effect of R_{in}

signal current shared between R_{in} & C_{det}

$$v_{out} = i_{in} Z_f \quad i/[j\omega C_f(1 + j\omega \text{ rise})]$$

$$\sim 1 - \exp(-t/\tau)$$

high frequencies in leading edge



leading edge of output pulse

Output impedance

- Usual method of varying v_{out} and finding i_{out} - generally messy algebra
- Current sensitive amplifier, open loop gain = A

$$v_{out} = i_2(R_2 + R_{in})$$

$$v_{in} = i_2 R_{in}$$

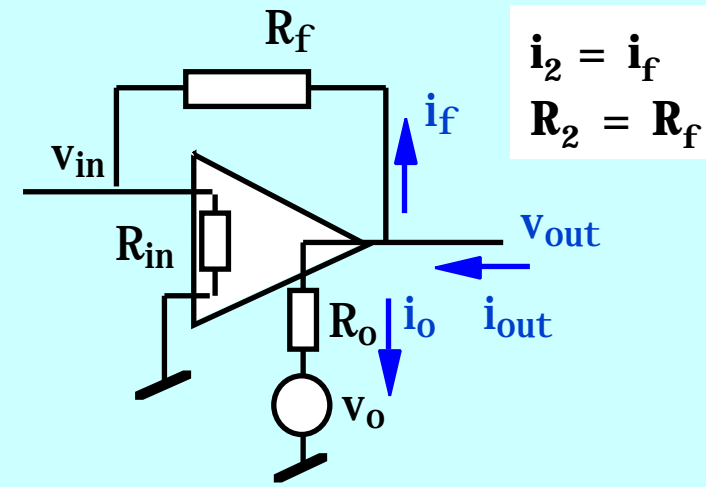
$$v_o = -A v_{in} = -A i_2 R_{in}$$

$$i_o = (v_{out} - v_o) / R_o = (v_{out} - A i_2 R_{in}) / R_o$$

$$Z_{out} = v_{out} / i_{out} = R_o (R_2 + R_{in}) / [R_o + R_2 + R_{in}(A+1)]$$

$$R_o / (A+1)$$

since $R_{in} \gg R_2, R_o$



R_o = open loop output impedance

- In general

$$Z_{out} = R_o / (1+Ab) \quad \text{if voltage is sampled at output} \quad b = \text{feedback fraction}$$

$$Z_{out} = R_o (1+Ab) \quad \text{if current is sampled at output}$$

Comparators

- Frequently need to compare a signal with a reference

eg temperature control, light detection, DVM,...

basis of analogue to digital conversion -> 1 bit

- Comparator

high gain differential amplifier,

difference between inputs sends output to saturation (+ or -)

could be op-amp - without feedback - or purpose designed IC

Sometimes ICs designed with open-collector output so add pull-up R to supply

also available with latch (memory) function

- NB

no negative feedback so $v_- = v_+$

saturation voltages may not reach supply voltages - check specs

speed of transition

- Potential problem

multiple transitions as signal changes near threshold

