

Hysteresis

- Add positive feedback (Schmitt trigger)

V_{ref} changes as $v_{out} \rightarrow +V_S$

ie threshold falls once transition is made

preventing immediate fall

positive feedback speeds transition

$$v_{out} = A(V_{ref} - v_-)$$

$$V_{ref} > v_- \Rightarrow v_{out} = V_S \quad V_{ref} = V_{high}$$

$$V_{ref} < v_- \Rightarrow v_{out} = 0V \quad V_{ref} = V_{low}$$

here, signal \Rightarrow logical "1": $v_{out} = 0V$

- Output depends on history

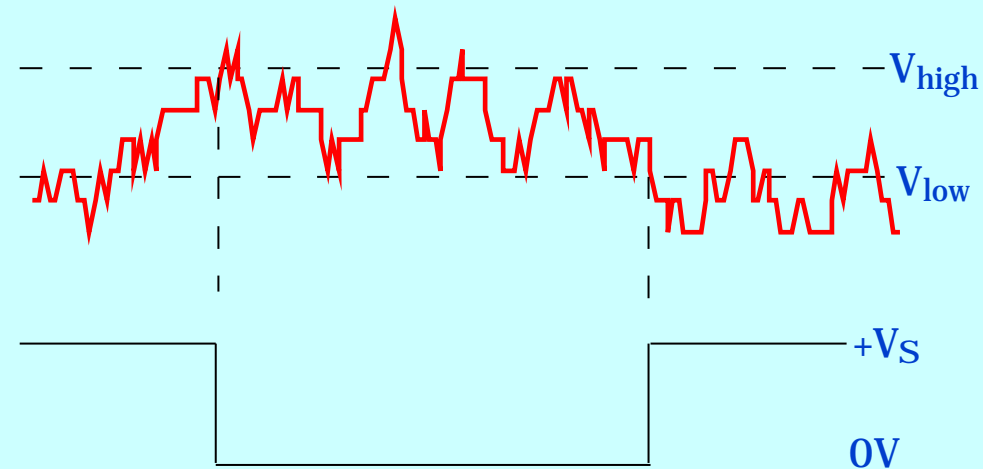
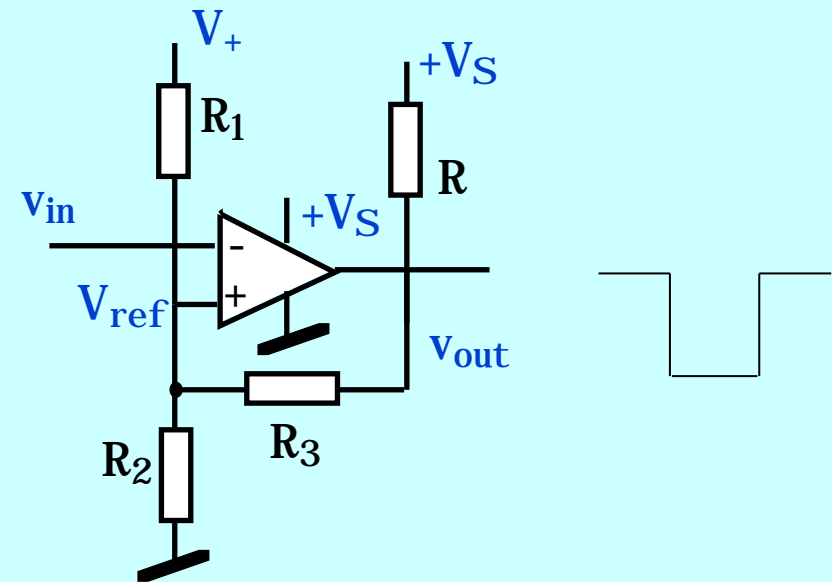
eg $V_+ = 10V$, $V_S = +5V$, $0V$

$$R_1 = 10k \quad , \quad R_2 = 10k \quad , \quad R_3 = 100k$$

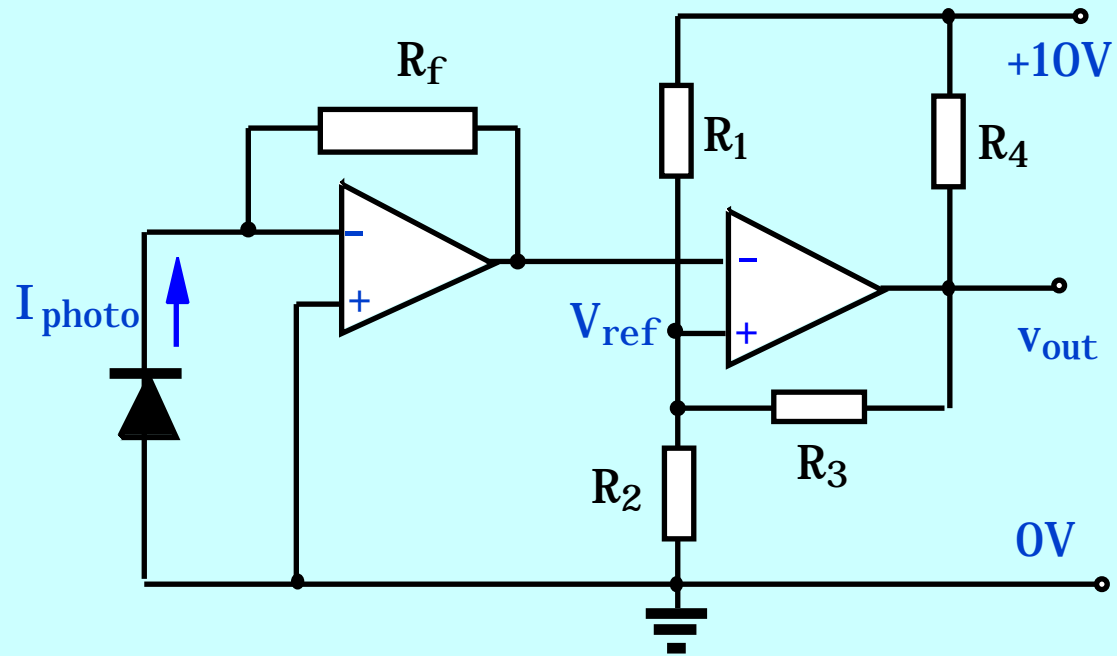
$$V_{out} = 0V, \quad V_{ref} = 4.76V$$

$$V_{out} = 5V, \quad V_{ref} = 5V$$

$$\text{hysteresis} = V_{ref} = 0.24V$$



Example - alarm



Oscillators

- **Basic building block of many systems**

clock or timer, signal generators, function generators, ...
can exploit positive feedback

- **Relaxation oscillator**

charge capacitor C through R $\sim \exp(-t/RC)$

v_- crosses threshold at V_{ref} , $V_{out} \Rightarrow \pm V_S$

V_{ref} changes sign

etc, etc...

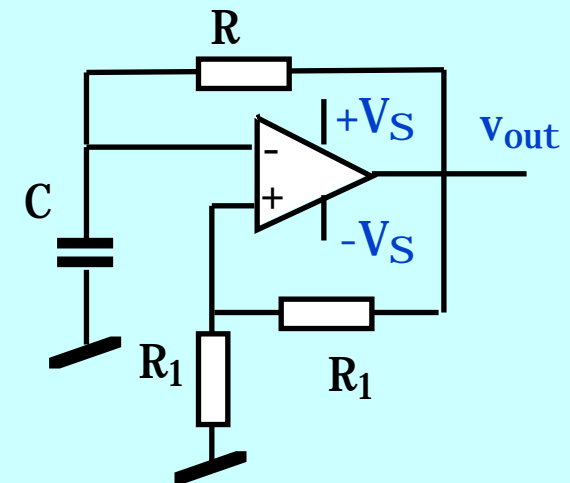
square wave output: $[\pm V_S]$

Period $T = 2.2RC$

- **many more types of oscillator design available**

IC classic = 555 (many versions)

external components set period and duty cycle



Wien bridge oscillator

- **Sine wave oscillators also often required**

favourite circuit for audio test applications:
low harmonic distortion at $f \sim$ few kHz

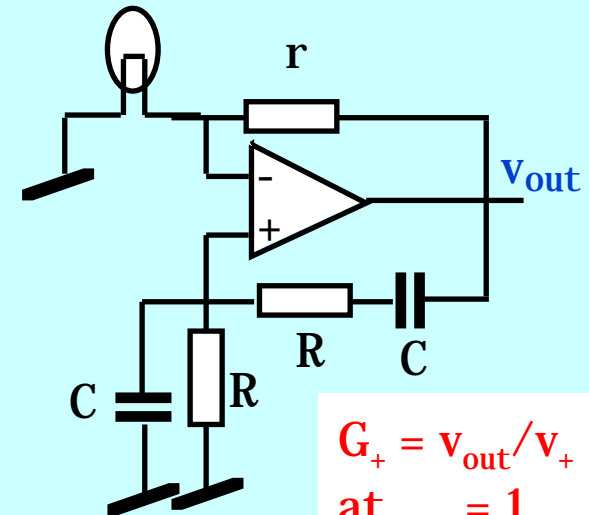
Gain = real at $\omega_0 = 1/RC$

so positive feedback

Lamp provides temperature dependent resistor
so negative feedback controls amplitude

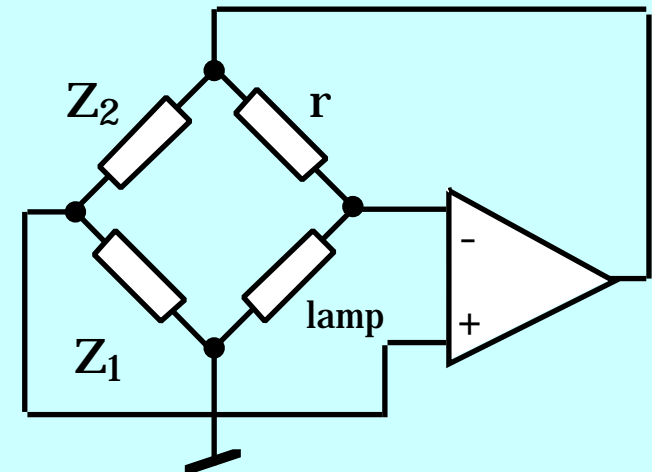
What values to choose for lamp resistance and r ?

What determines amount of harmonic distortion?



$$G_+ = v_{out}/v_+ = 3$$

at $\omega = 1/RC$



Temperature controller

- A frequent requirement - similar to many other control applications

eg cryostat with stable temperature maintained by resistive heater, or oven, ...

- On-Off control

$$T < T_0$$

set heater to maximum power

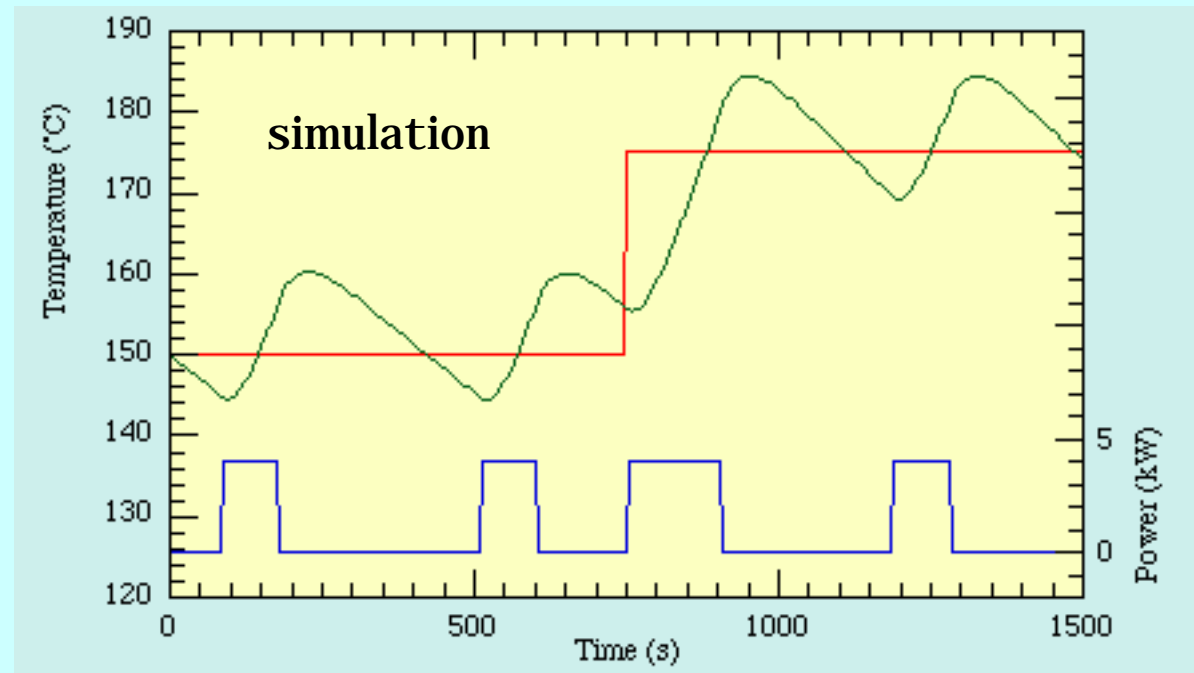
add hysteresis (T_{01} , T_{02})

to prevent noise from switching too rapidly

ok for central heating or

domestic oven but not good

for stable measurements - try to improve



P & PD Temperature control

- Set heater power, proportional to temperature difference (P)

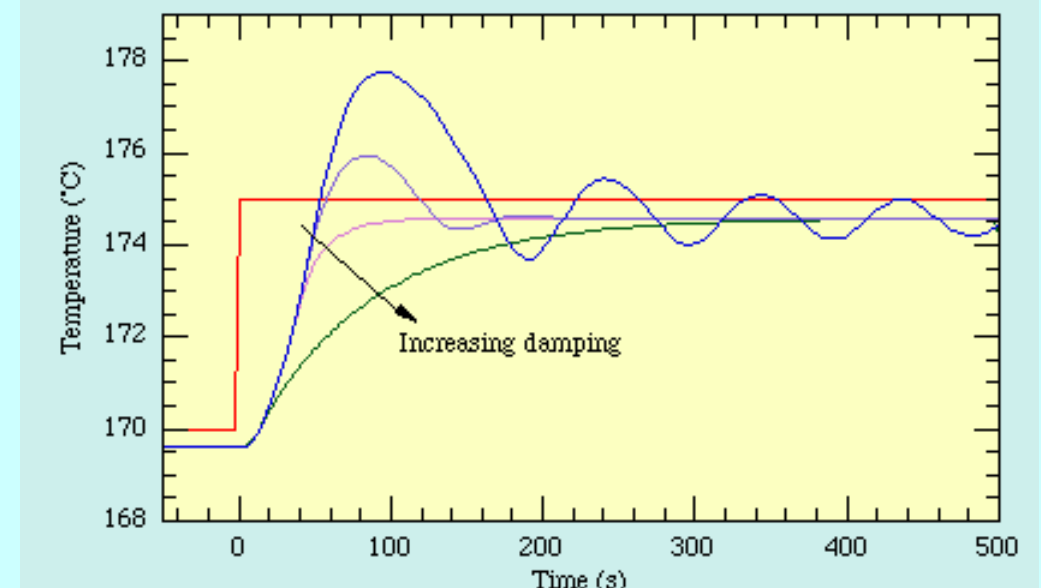
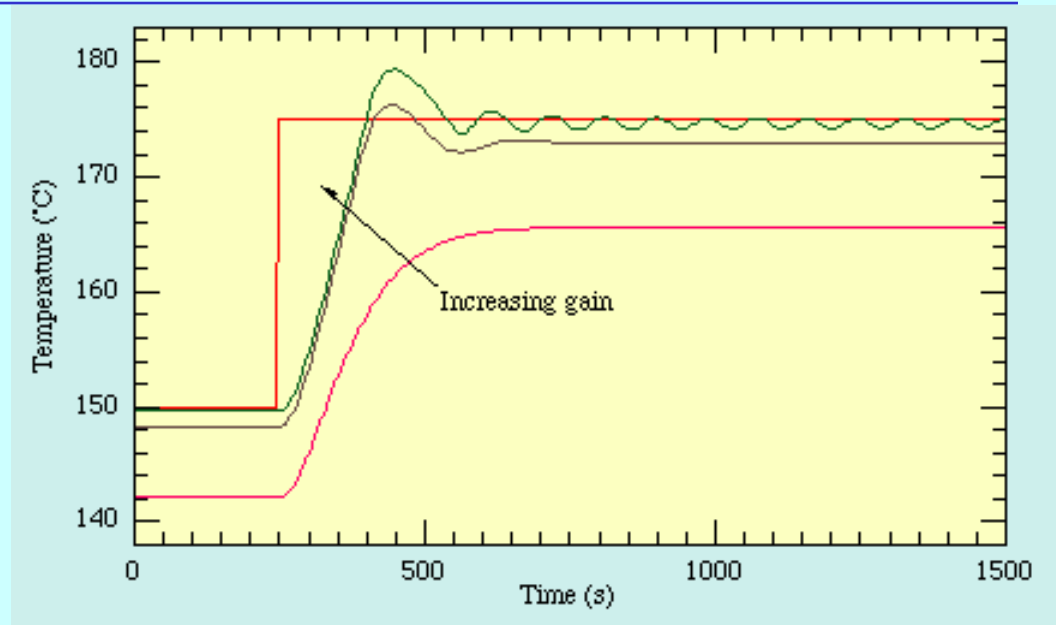
$$W = P(T_{\text{meas}} - T_0)$$

T still oscillates and
undershoots desired value
unstable if heat too fast

- Add control term proportional to rate of change (PD)

$$W = P[(T_{\text{meas}} - T_0) + Dd(T_{\text{meas}} - T_0)/dt]$$

D too large: overshoot & ringing
D too small: slow response



PID Temperature control

- PD can eliminate ringing & overshoot but undershoot error remains

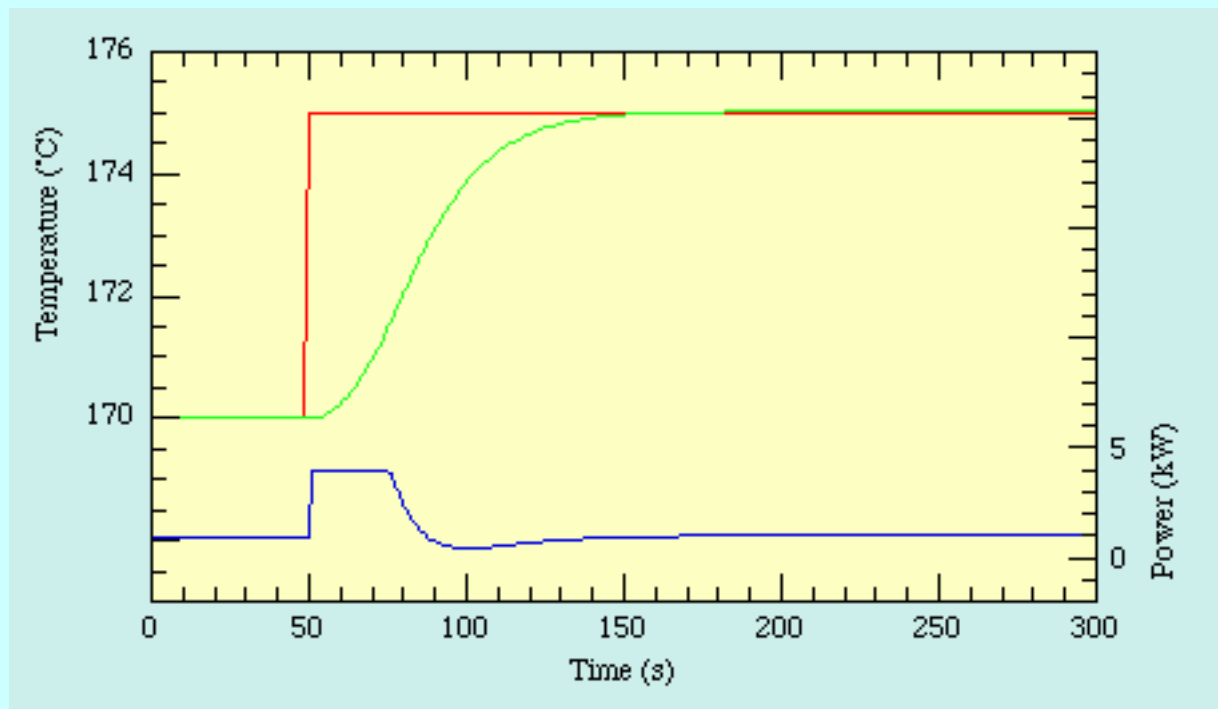
add integral term

- PID control

$$W = P[(T_{\text{meas}} - T_0) + Dd(T_{\text{meas}} - T_0)/dt + I \int (T_{\text{meas}} - T_0) dt]$$

good results but
need to choose coefficients
P, D, I empirically to ensure
stability

we'll later look at methods
to solve such system
equations using transforms



Temperature control circuit

- Notes

- $R_1 \gg R_2$ to avoid loading

- still need heating circuit

want $W \propto V_{out}$

- Diode ensures $W \geq 0$

$V_{diode}?$

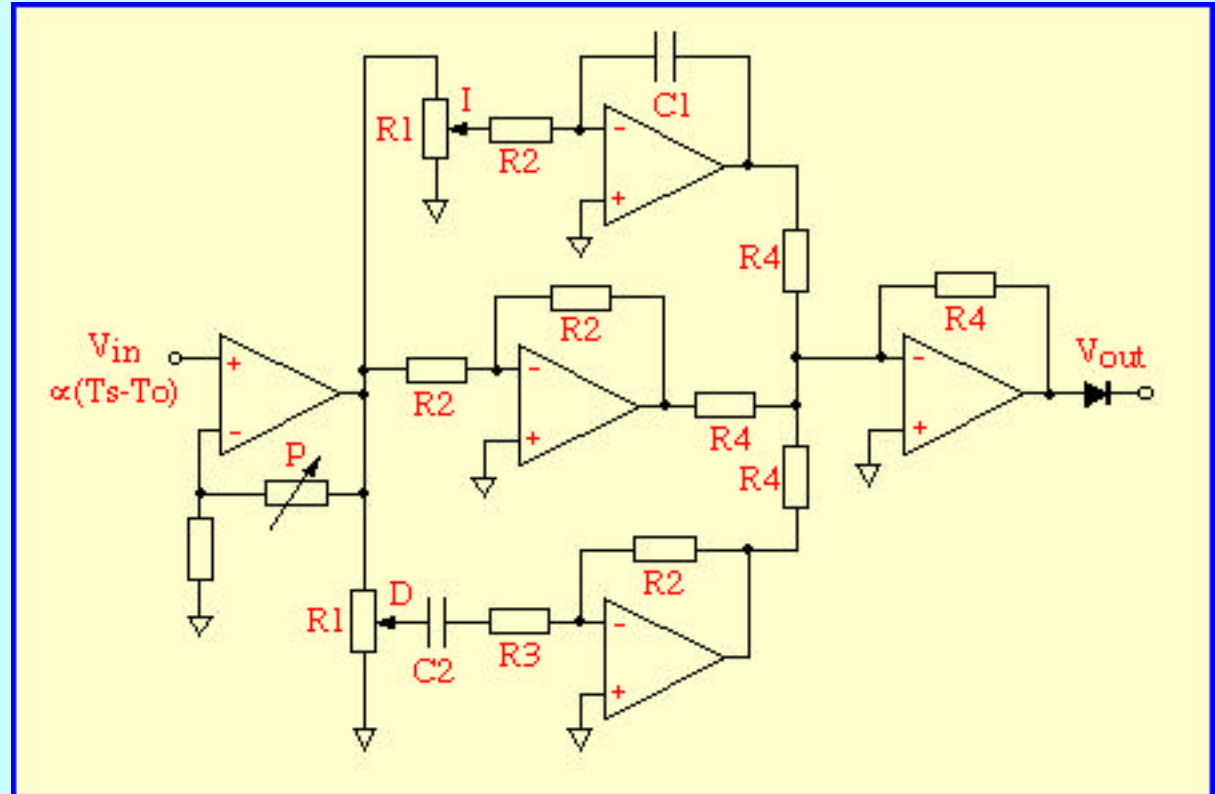
- Time constants to be selected

depend on appliance chosen

commercial devices will recommend values

- Need to consider offset currents and voltages

null, or consider more complex circuit design



Instrumentation amplifier

- **High gain, dc-coupled differential amplifier**

single ended output

high input impedance

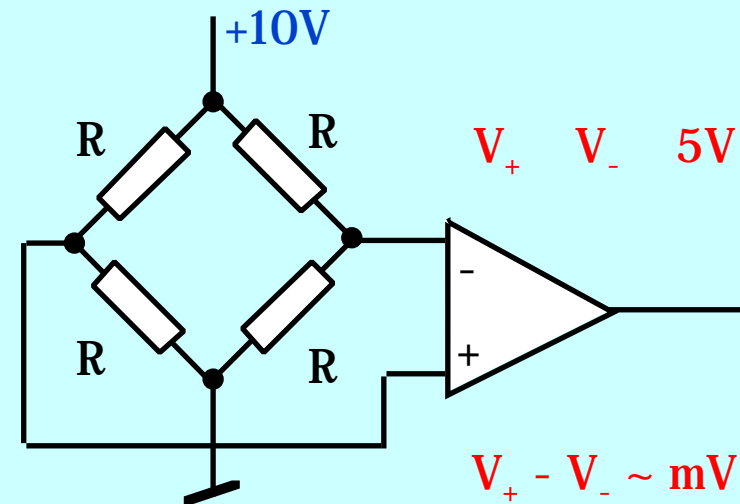
high CMRR

use to amplify small differential signals where large CM signal may be present

but small normal mode

eg strain gauge, other bridge circuits

"weak" voltage source



To measure 5mV signal with
1% error

$$CMRR = 0.05/5000 = 100dB$$

- **Drawback of differential amplifier**

relatively low input impedance

CMRR relies on excellent resistor matching

cheap op-amps may have CMRR ~80dB

Improved differential amplifier

- Add voltage buffers and choose precise resistors

improves input impedance

0.1% resistors available

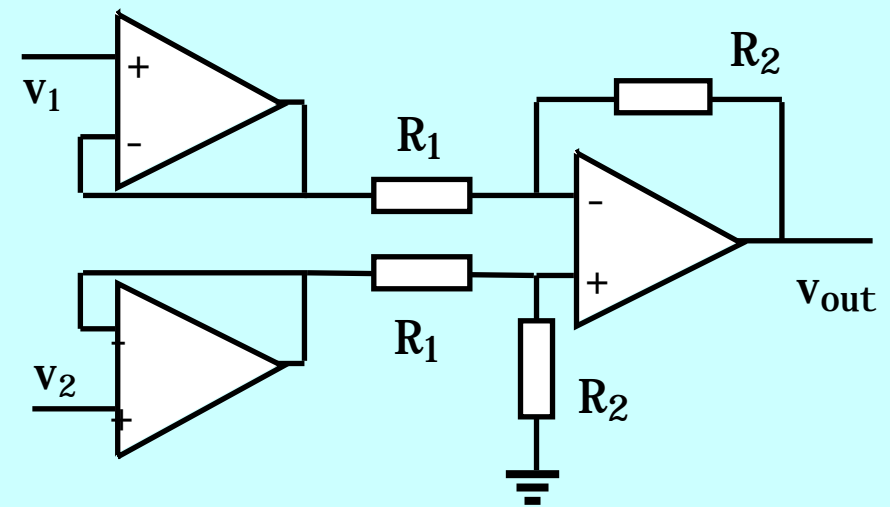
careful nulling of circuits

still need high CMRR from output amplifier

big demands on R precision

often find restrictions on driving circuit

ie source



Classic instrumentation amplifier

• Input stage differential gain

$$v_{10} - v_1 = iR_2 = v_2 - v_{20} \quad (1)$$

$$iR_1 = v_1 - v_2$$

$$(v_{10} - v_{20}) - (v_1 - v_2) = 2iR_2$$

$$(v_{10} - v_{20}) = 2iR_2 + iR_1$$

$$= (v_1 - v_2)(2R_2 + R_1)/R_1$$

$$G_{\text{diff}} = 1 + 2R_2/R_1$$

• Input stage common mode gain

$$v_1 = v_{\text{CM}} + u_1$$

$$v_2 = v_{\text{CM}} + u_2$$

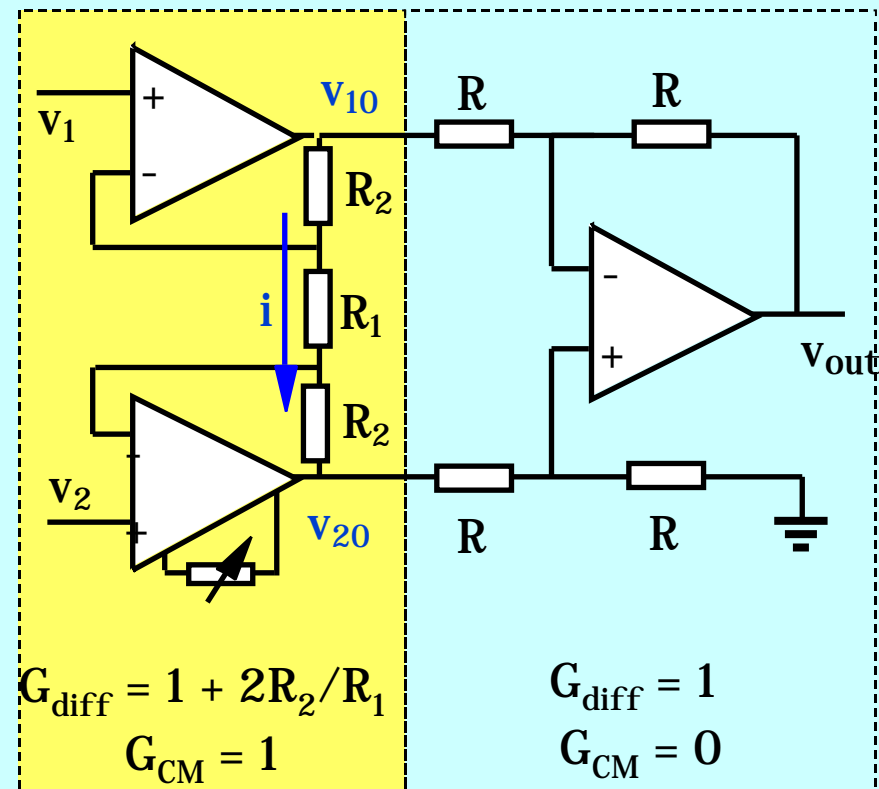
$$2v_{\text{CM}} = v_1 + v_2 \text{ with signal } u_1 = u_2 = 0$$

$$\text{From (1) } v_{10} + v_{20} = v_1 + v_2$$

$$G_{\text{CM}} = 1$$

• Remainder is normal differential amplifier, ($G = 1$ in this case)

Instrumentation ICs available



Reduce requirements on second stage
still choose input amps for good CMRR
and null carefully

The Instrumentation Amplifier in practice

- Can add some more useful features

feed common mode level back as guard

connect to cable shield

reduce effects of cable capacitance, leakage currents

sense voltage at load

allows feedback to correct for losses in wiring

or offset of DC conditions

