Signal processing

•Now identified: Noise sources Amplifier components and basic design How to achieve "<u>best</u>" signal to noise?

•Possible constraints

power consumption

ability to provide power & extract heat, material for cooling

C_{det}

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layout of system (space, cables,...)
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signal rate

eg. signal "pileup" vs E resolution

•Two methods

Pulse shaping time invariant filter

Pulse sampling

time variant filter

Cf

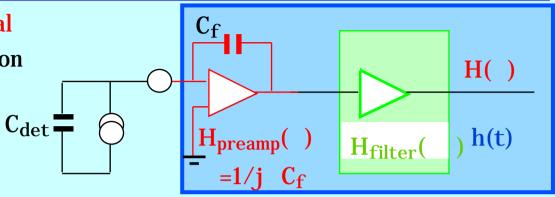
Bandwidth

limiting

filter

Pulse shaping

- •Preamplifier pulse shape is impractical step (exponential) with long duration short, sharp peak
- •Calculate signal and noise in t and f using results so far



•Signal

$$S_{out}() = S_{in}().H_{preamp}().H_{filter}() = S_{in}().H()$$

$$S_{out}(t) = S_{in}(t) * h_{preamp}(t) * h_{filter}(t) = S_{in}(t) * h(t)$$
 convolution

•Noise

$${}^{2} = I_{n}{}^{2}|H()|^{2} df = (e_{n}{}^{2} {}^{2}C^{2}+i_{n}{}^{2})|H()|^{2} df$$

= $e_{n}{}^{2}C^{2} | H()|^{2} df + i_{n}{}^{2} |H()|^{2} df$
$${}^{2} = e_{n}{}^{2}C^{2} [h'(t)]^{2} dt + i_{n}{}^{2} [h(t)]^{2} dt \qquad \text{provided } e_{\underline{n}} \& i_{\underline{n}} \text{ are white } e_{\underline{n}} \& i_{\underline{n}} = e_{\underline{n}} \& e_{\underline{$$

Equivalent Noise Charge

•Noise must be compared with signal - normalisation

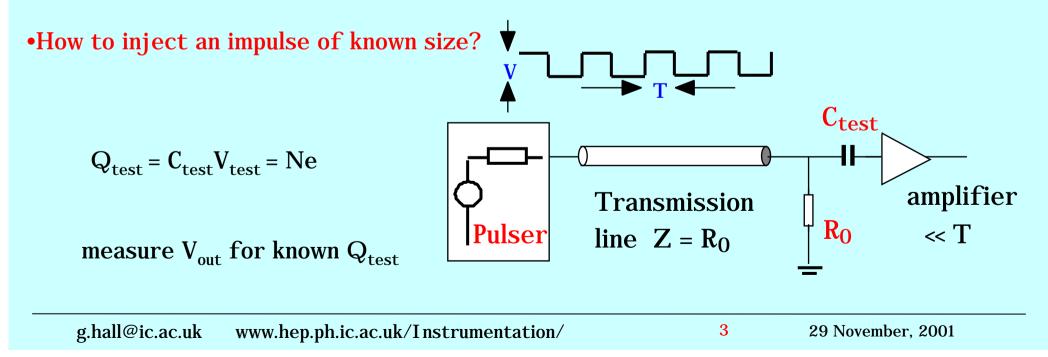
 $S_{out}(t) = Q (u)*h(t-u)du = h(t)$ inject unit impulse ie. Q = 1

h(t) contains gain

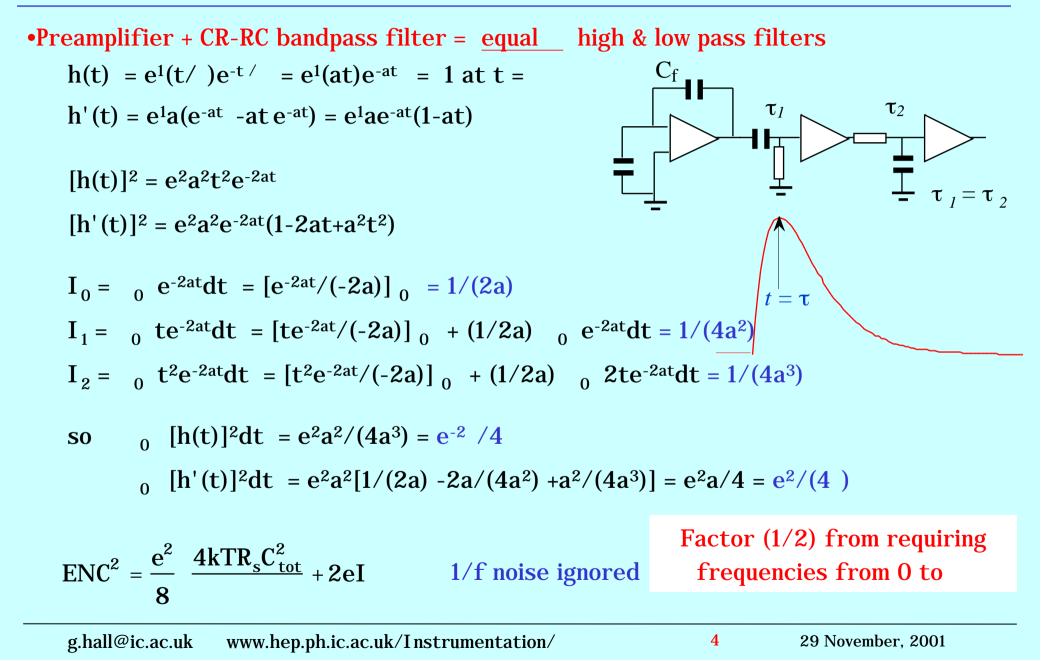
 $ENC^2 = e_n^2 C^2 [h'(t)]^2 dt + i_n^2 [h(t)]^2 dt$ normalised to signal of unit amplitude

•ENC = signal which produces output amplitude equal to r.m.s. noise

desirable to measure in absolute units - e, coul, keV(Si),...



Example noise calculation



Improved time invariant filters

•Optimal filter = infinite exponential cusp

$$h(t) = exp(-|t|/_{opt})$$

gives equal contributions from series and parallel sources, if...

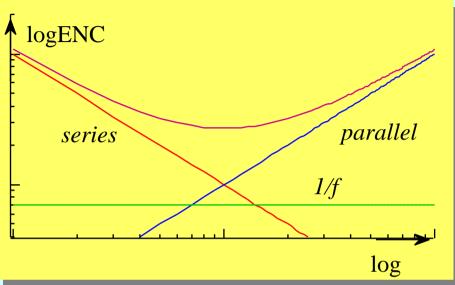
 $_{opt} = C_{tot}^2 R_s R_p$ R_s and R_p are equivalent noise resistances

impractical in real systems

 $\overline{\downarrow}C_2$ •Practical filters - wide range of possibilities ! $CR-RC^n$ type $n \sim 1-2$ C_1 \mathbf{R}_1 *RC* = *low pass filter CR*= *high pass* C_1 easy to implement R_2 R_1 **CR-RC**ⁿ n ~5-7 semi-gaussian ≈ symmetric pulses R(k-1) active filters based on op-amp configurations examples R

Noise after pulse shaping

•General result is $ENC^2 = e_n^2 C^2 / + i_n^2 + C^2$, depend on pulse shape calculate in t or f : 1/f - can be computed in f only



•a minimum noise can be achieved with a given shaping time constant chosen depending on magnitudes of noise sources

•Useful point of comparison: CR-RC bandpass filter

$$ENC^{2} = \frac{e^{2}}{8} \frac{4kTR_{s}C_{tot}^{2}}{8} + 2eI + 4A_{f}C_{tot}^{2}$$

only 36% worse than theoretical optimal filter

6

•An approximate numerical value

ENC²[e²]
$$\frac{24^2 R_s[k] C_{tot}^2[pF]}{[\mu s]} + 100^2 [\mu s]$$

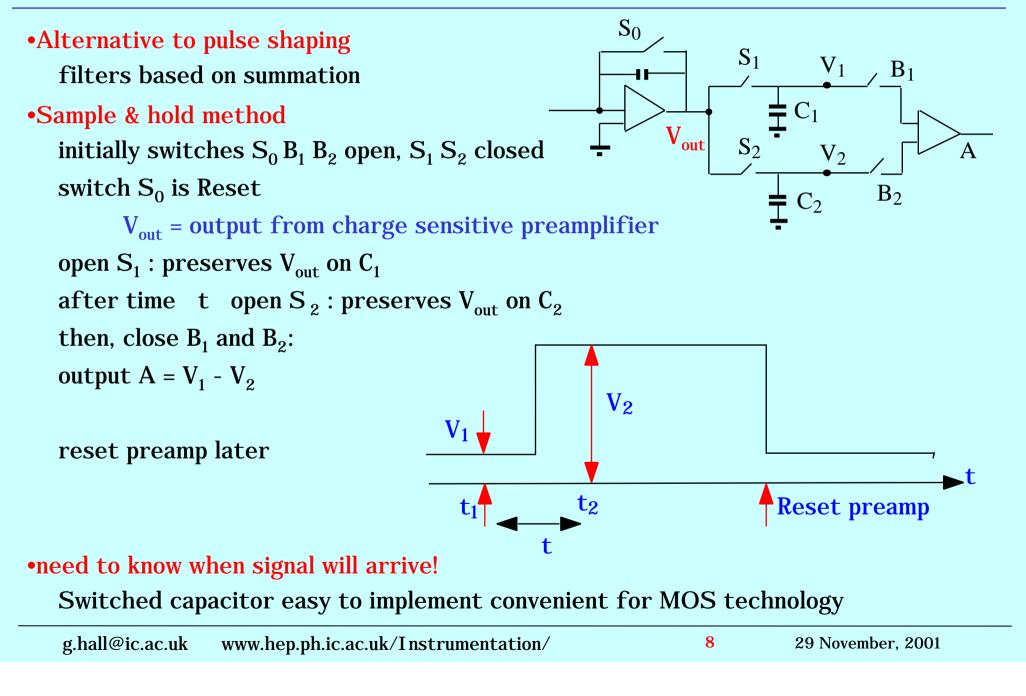
•using CR-RC filter, ignoring 1/f noise

ie

I = 1nA = 1 μ s ENC_p 100e

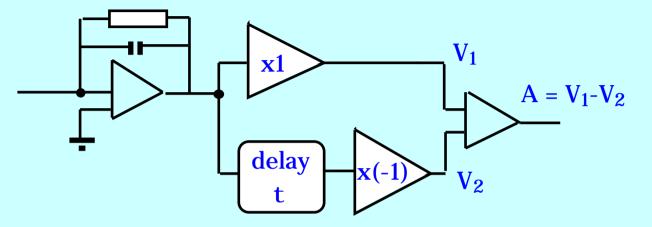
 $R_s = 10$ $C = 10pF = 1\mu s$ ENC_s 24e

Time variant filters

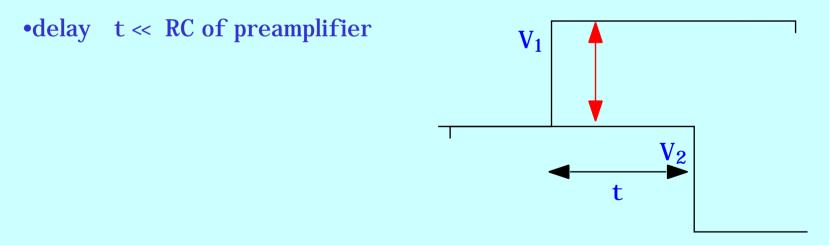


Time variant filters

•Can perform same process with delay line



delay line Double Correlated Sampling



•How to analyse noise performance of time variant systems?

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Weighting function

•What output is produced at T_m by impulse at time t? consider all t - defines weighting function

