

Analogue to Digital Conversion

- Turns electrical input (voltage/current) into numeric value
- Parameters and requirements

Resolution

the granularity of the digital values

Integral Non-Linearity

proportionality of output to input

Differential Non-Linearity

uniformity of digitisation increments

Conversion time

how much time to convert signal to digital value

Count-rate performance

how quickly a new conversion can begin after a previous event

Stability

how much values change with time

Resolution

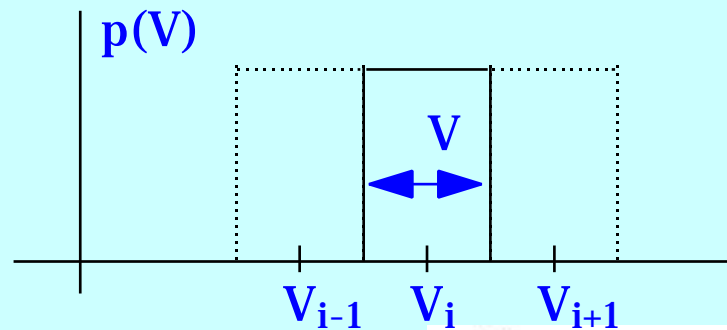
- To convert an analogue value, eg voltage, to digital two parameters are required
range and number of bits

$$\text{quantum} = V = (V_{\max} - V_{\min}) * 2^{-N} \quad \text{referred to as 1LSB (least significant bit)}$$

- eg 10 bits = $2^{10} = 1024$, $V_{\max} - V_{\min} = 1V \Rightarrow V = 1V/1024 \quad 1mV$

- Ideal ADC behaviour

probability vs amplitude

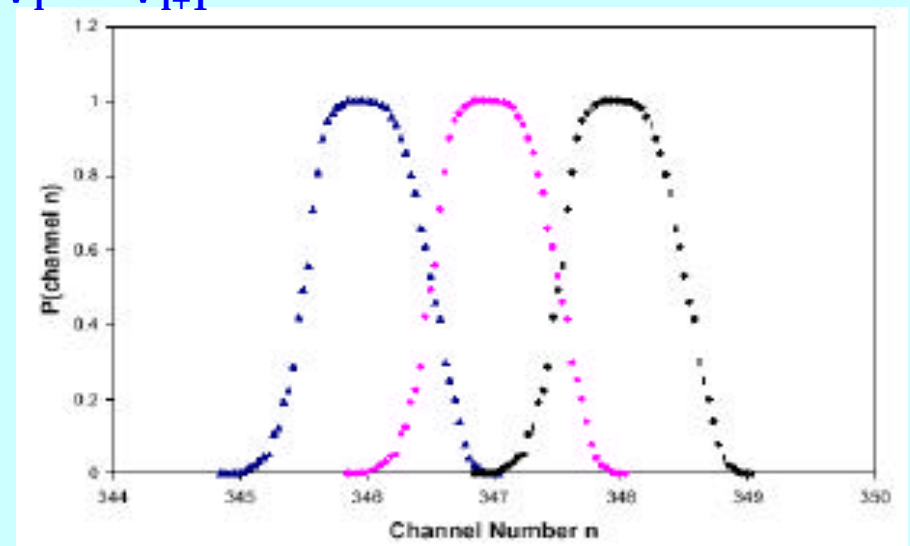


- Real ADC behaviour

noise in digitisation process

smears resolution

$$\text{noise} < V/4$$



Speed vs resolution

•from Analog Devices ADC selection guide

bits per sec (or samples per sec)

| | | Throughput rate (bps) | | | | | |
|-------------------|-------|-----------------------|---------|---------|-------|---------|-------|
| | | <10k | 10-100k | 100k-1M | 1-10M | 10-100M | >100M |
| Resolution (bits) | 17 | | ----- | ----- | ----- | ----- | ----- |
| | 14-16 | | | | | | ----- |
| | 12-13 | ----- | | | | | |
| | 10-11 | ----- | | | | | |
| | 8-9 | ----- | ----- | | | | |
| | 8 | ----- | ----- | ----- | ----- | | ----- |

Maximum speed 200Mbps 12 bits 1.3W single channel

210Mbps 10bits 2.4W single channel

Maximum resolution 24 bits 6.4kbps

•What determines this relationship?

Integral non-linearity

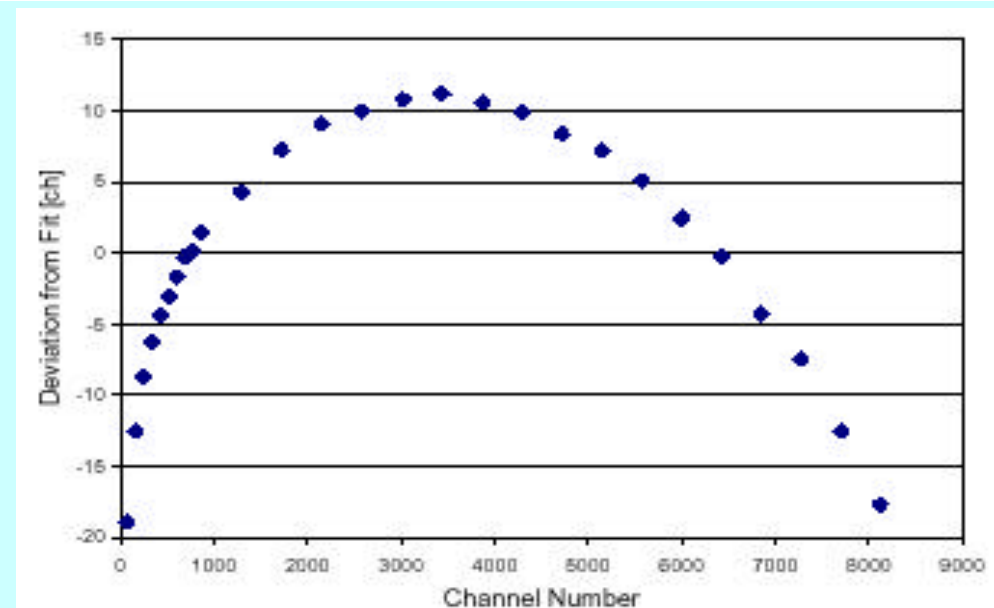
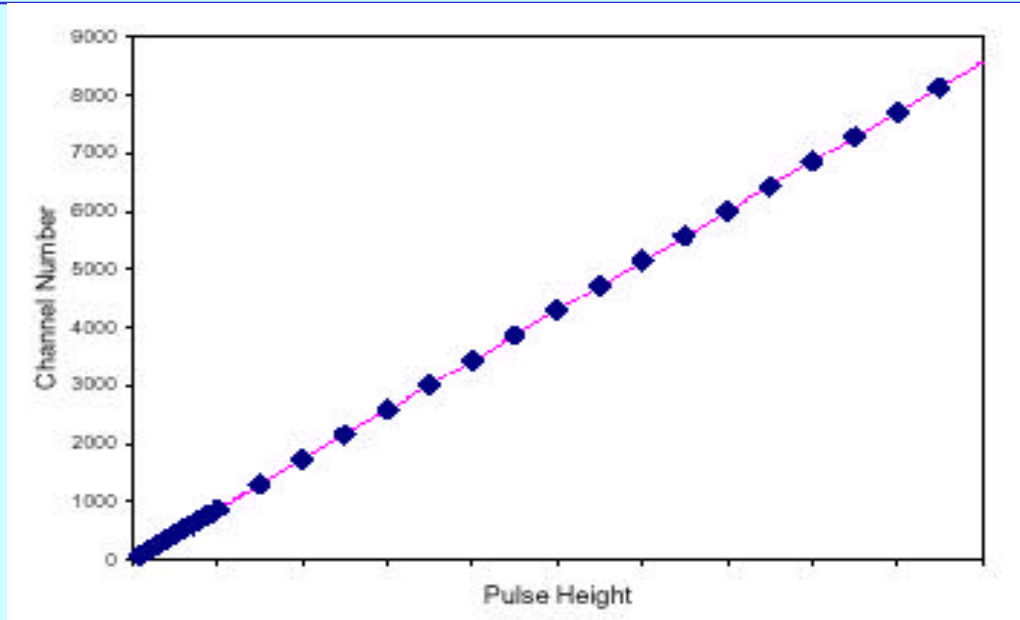
- Output value D should be linearly proportional to V

check with plot

for more precise evaluation of INL

fit to line and plot deviations

plot $D_i - D_{\text{fit}}$ vs n_{chan}



Differential non-linearity

- measures non-uniformity in channel profiles over range

$$\text{DNL} = V_i / \langle V \rangle - 1$$

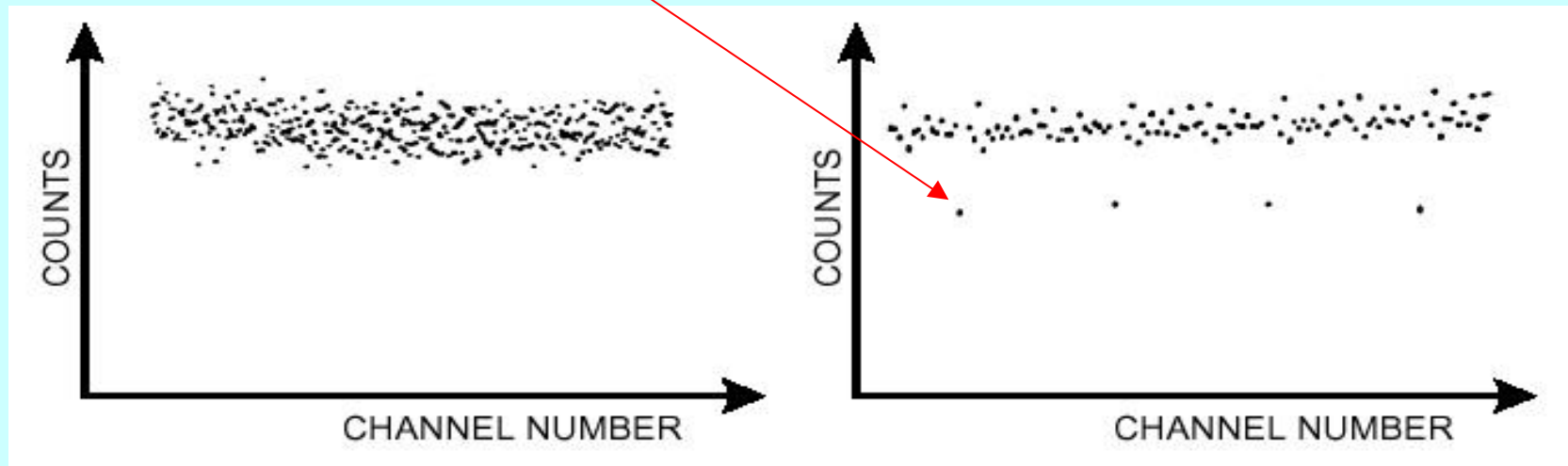
V_i = width of channel i

$\langle V \rangle$ = average width

- rms or worst case values may be quoted

DNL \sim 1% typical but 10^{-3} can be achieved

can show up systematic effects, as well as random



Other variables

- **Conversion time**

- finite time is required for conversion and storage of values

- may depend on signal amplitude

- gives rise to dead time in system

- ie system cannot handle another event during dead time

- may need accounting for, or risk bias in results*

- **Rate effects**

- results may depend on rate of arrival of signals

- typically lead to spectral broadening

- **Stability**

- temperature effects are a typical cause of variations

- **A partial solution to most of these problems is regular calibration, preferably under real operating conditions, as well as control of variables**

Parallel (Flash) ADC

- Input value is compared simultaneously...

- against a set of comparators

2^N comparators required for N bits

Threshold values defined by resistor chain

relative accuracy important,
not absolute values

- Pros

short conversion time

eg 10bits @ 40MHz

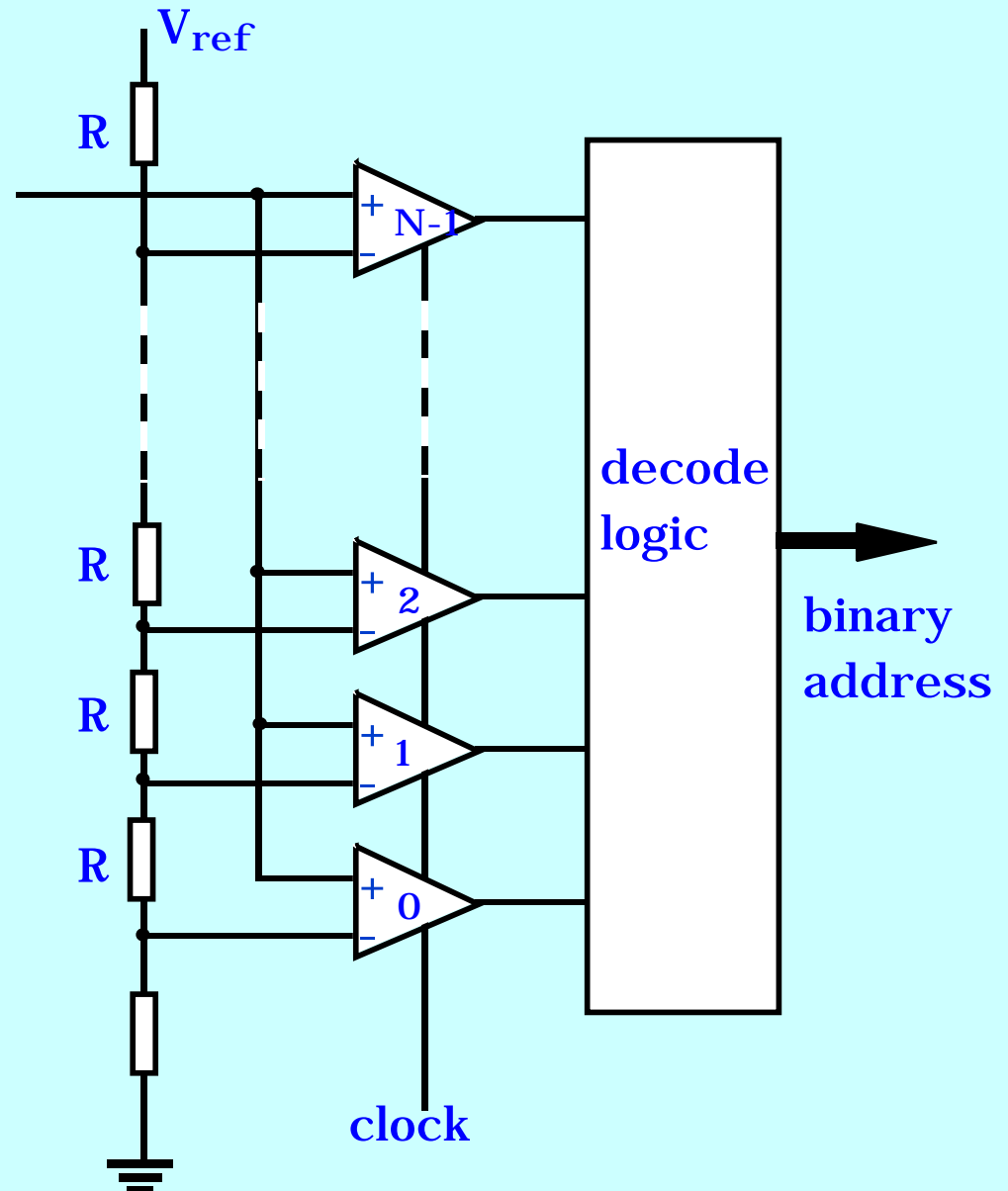
- Cons

limited resolution,

size of IC grows with N

DNL ~ 1%

power consumption



Successive approximation ADC

- analogous to binary search

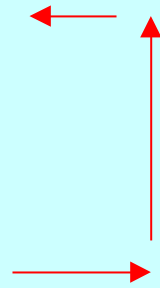
generate $V_{\text{ref}} = V \times (2^{N-1}, 2^{N-2}, \dots 2^0)$ in N steps

set bit = 1

if $V_{\text{in}} > V_{\text{ref}}$

leave

else bit = 0



- Pros

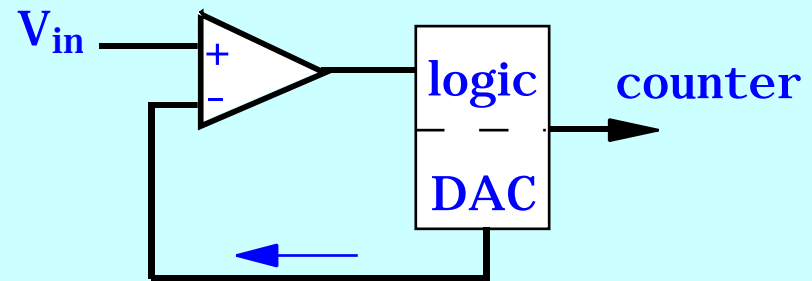
speed ~ μsec

high resolution

- Cons

DNL 10-20%

very precise resistors required with DAC for V_{ref}



DAC = digital to
analogue converter
ie number -> voltage

Single slope (Wilkinson) ADC

- **Single slope conversion**

input signal charges capacitor
discharged by constant current
counter (eg 200MHz) times discharge

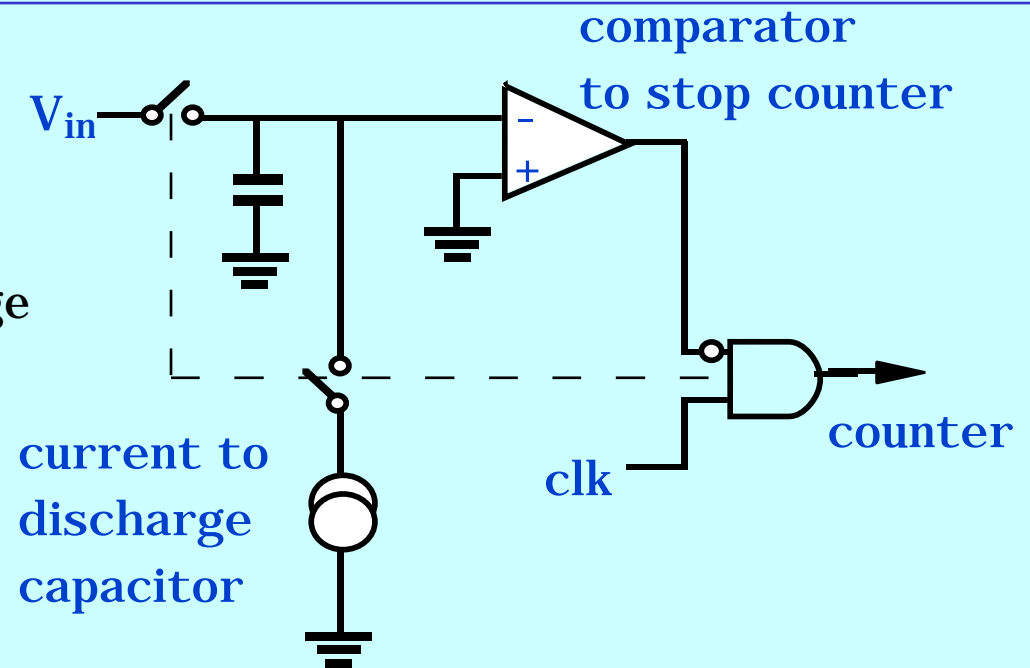
- **Pros**

Excellent DNL

- **Cons**

modest absolute accuracy
slow, and conversion time depends
on amplitude

$$T_{\text{conv}} = nT \quad \text{eg } T = 10\text{ns, } 13 \text{ bits} \quad T_{\text{conv}} = 82\mu\text{s}$$



- **Dual slope conversion reduces systematic (absolute) errors**

charge C with constant current and then measure time for discharge

charge and discharge subject to same comparator and capacitor variations

Sigma-delta ADC

- Digitise the signal with 1-bit resolution at a high sampling rate (MHz).

useful for high resolution conversion of low-frequency signals, to 20bits

low-distortion conversion of audio signals

good linearity and high accuracy.

- Operation - At $t = 0$, assume $V_{ref} = 0$

V_{out} high

integrator charges -ve

at rate $\sim V_{in}$

comparator flips

counter goes low

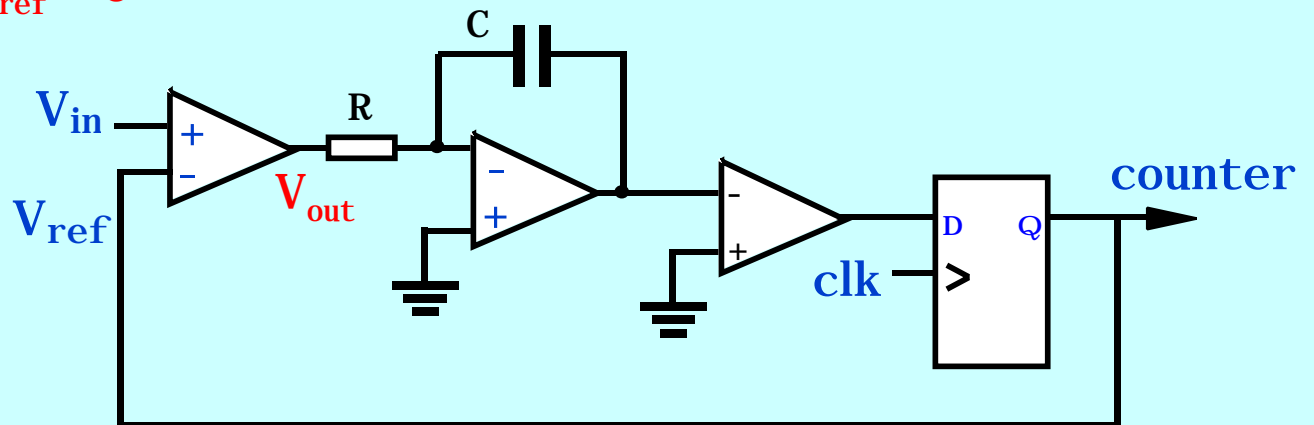
clock increments... etc,...

$V_{in} = 0 \Rightarrow$ output = 000000...

$V_{in} = (1/2)V_{in}(\text{max}) \Rightarrow$ output = 101010...

$V_{in} = V_{in}(\text{max}) \Rightarrow$ output = 111111...

the higher the input voltage, the more 1's at the serial digital output.



Non-linear A-D conversion

- Some high speed systems also need high resolution and dynamic range

however do they need the same resolution at all amplitudes?

- Dynamic range - eg 15 bit

is set by largest and smallest signals to be observed

- Resolution on energy

determined by requirements, noise and physics

eg statistics (counting or E resolution) $\Rightarrow \Delta E_{\text{stat}} = a / \sqrt{E}$

noise(E) = constant so

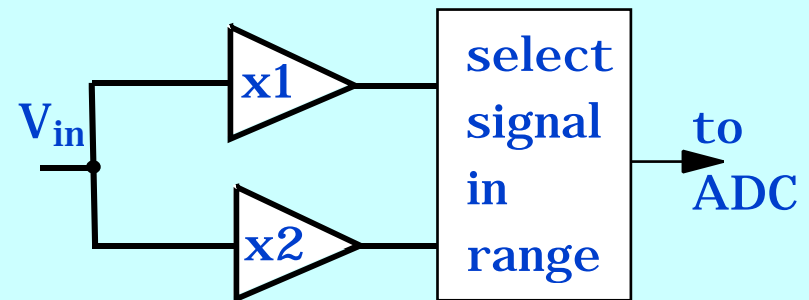
noise = b

Resolution $\Delta E_{\text{total}} = a / \sqrt{E}$

$\Delta E_{\text{total}} = [a^2/E + b^2/E^2]^{1/2}$ a term eventually dominates

- thus build multi-gain system prior to ADC

so smaller signals digitised with lower effective resolution



Example of non-linear ADC

- A integrating system for measuring x-ray photons for crystallography, measuring spots. The most intense spots contain up to $\sim 10^9$ photons, the weakest just a few.
Measure N in spot

aim: achieve 1% resolution

using a 10-bit ADC (cost)

assume 1V range

1V = largest signal, defines G_1

$N < 10^4$ $(N)/N > 1\%$

defines smallest signals

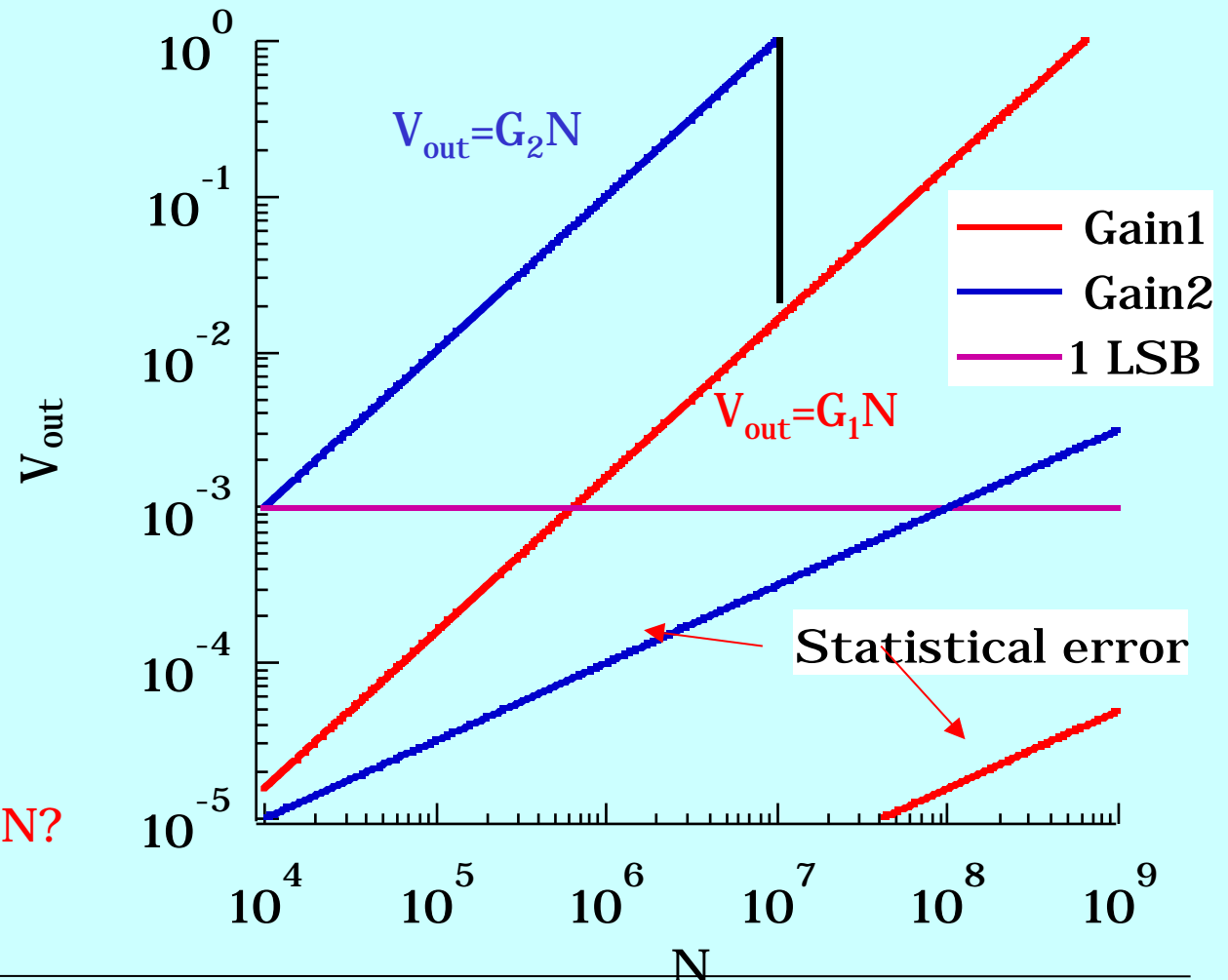
but ADC LSB $>$ signal

Increase small signal gain G_2

Select output in ADC range

- Is 1% resolution achieved for all N ?

If not... ?



Time to Digital Conversion (TDCs)

- Count clock pulses between start and stop pulses

up to ~1GHz, limited by technology so $t \approx 1\text{ns}$

capable of digitising more than one hit in an acquisition

provided logic is sufficient

- Analogue ramp

for greater precision, $t \approx 10\text{ps}$

charge capacitor with constant current source

start pulse: turns on current

stop pulse: turns off

then measure V on storage capacitor using ADC

can't accept more than one signal in digitising period

Digital to Analogue Conversion (DAC)

- Several techniques - generally similar (inverse) to ADC

eg summing amplifier

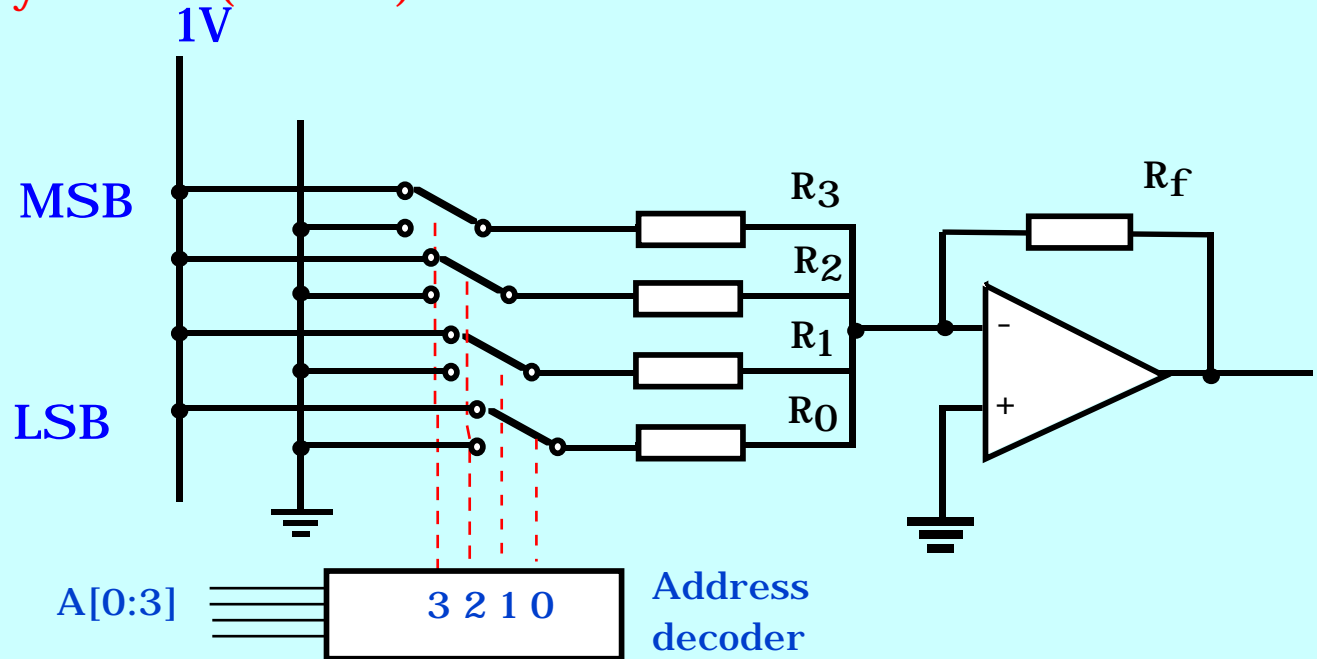
$$\begin{aligned} R_0 &= 2 * R_1 \\ &= 4 * R_2 \\ &= 8 * R_3 \end{aligned}$$

but precision of smallest resistor must be better than LSB

$$\text{MSB} = (V/R_3) < \text{LSB} = V/R_0$$

OK for a few bits but becomes difficult for N large

other techniques required... eg



R- 2R converter

- relies on matching of resistor values

consider point on resistor divider

switch open or closed

always see $2R$ in parallel with $2R$

= R to ground

(start from right and work left)

