

**SPECTRAL FUNCTION IN NEUTRINO GENERATORS:
STRUCTURE FUNCTION MEASUREMENT OF ^{40}Ar
via $(E, E'p)$ and ITS IMPACT ON NEUTRINO
OSCILLATING PARAMETERS**

**Chun-Min (Mindy) Jen
(Center for Neutrino Physics, Virginia Tech.)**

NuINT 14'

May 20th, 2014

Outline

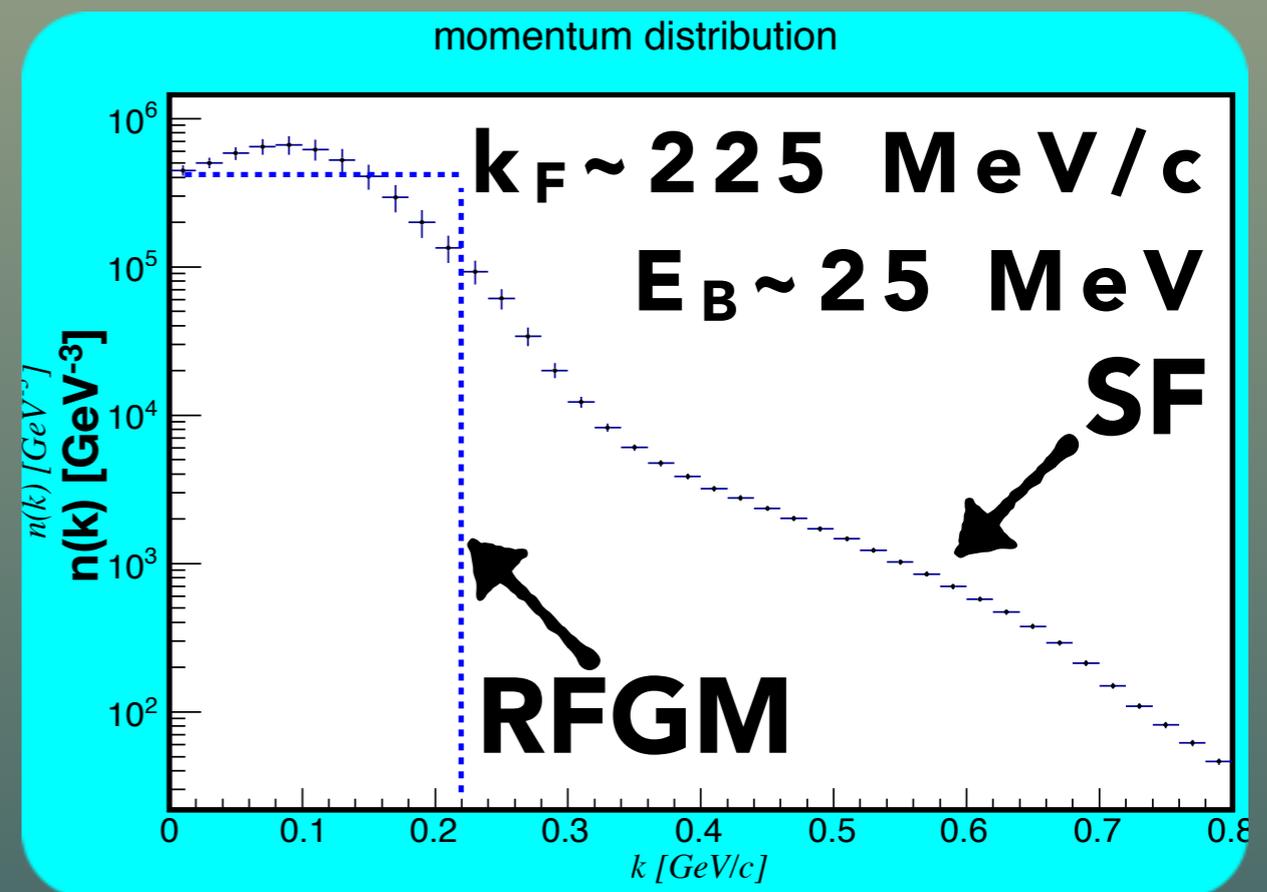
- ✘ Introduction to Structure (Spectral) Functions
- ✘ The Role of Spectral Function in Lepton-Nucleus Cross Section Cal.
- ✘ Electron Cross-section Validation (^{12}C and ^{40}Ca)
- ✘ Neutrino Cross-section Comparison (GENIE, GiBUU, NuWro)
- ✘ Impact on Oscillation Parameters
- ✘ Conclusions

THROUGH ELECTRON SCATTERING, STRUCTURE FUNCTION IS EXTRACTED

- initial-state nucleon's momentum distribution, k_n , is assumed to be flat (no structure) for all shells below the Fermi sea (k_F)
- **the spectral function theory considers the difference in the structure function for each shell and thus is capable of yielding a much better prediction while being compared to the measured electron cross-section than RFGM**

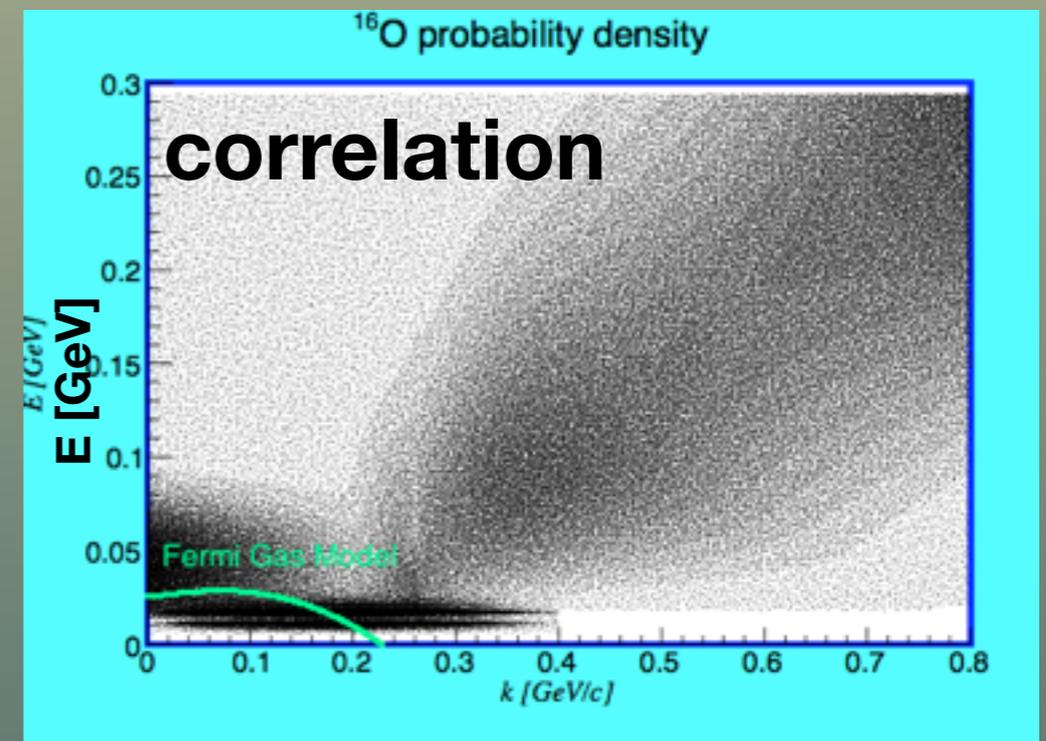
$$n^D = \sigma_{(e,e'p)} / K \sigma_{cc1}$$

DWIA



SEPARATION ENERGY OF EACH NUCLEON WITH ONE SPECIFIC QUANTUM NUMBER IS INDIVIDUAL

- ❖ absence of position correlation in the ground state wave function between each pair of nucleons
- ❖ the energy distribution of each shell is a delta function (discontinuous)
- ❖ all nucleons feel the same force acting on them as a result of a mean field potential
- ❖ N-N (position) correlations are formed by the charge density distribution
- ❖ N-N (position) correlations cause the overlap of energy distributions (continuous)
- ❖ N-N (position) correlations lead to the strong short-range repulsion (back-to-back)
- ❖ N-N (position) correlations affect the momentum distribution of each shell



- RFG model

$$P(|\vec{p}|, E) = \frac{3}{4\pi k_F^3} \theta(k_F - |\vec{p}|) \delta(\sqrt{m^2 + |\vec{p}|^2} - m - E_B + E)$$

step function (no structure) energy-momentum conservation

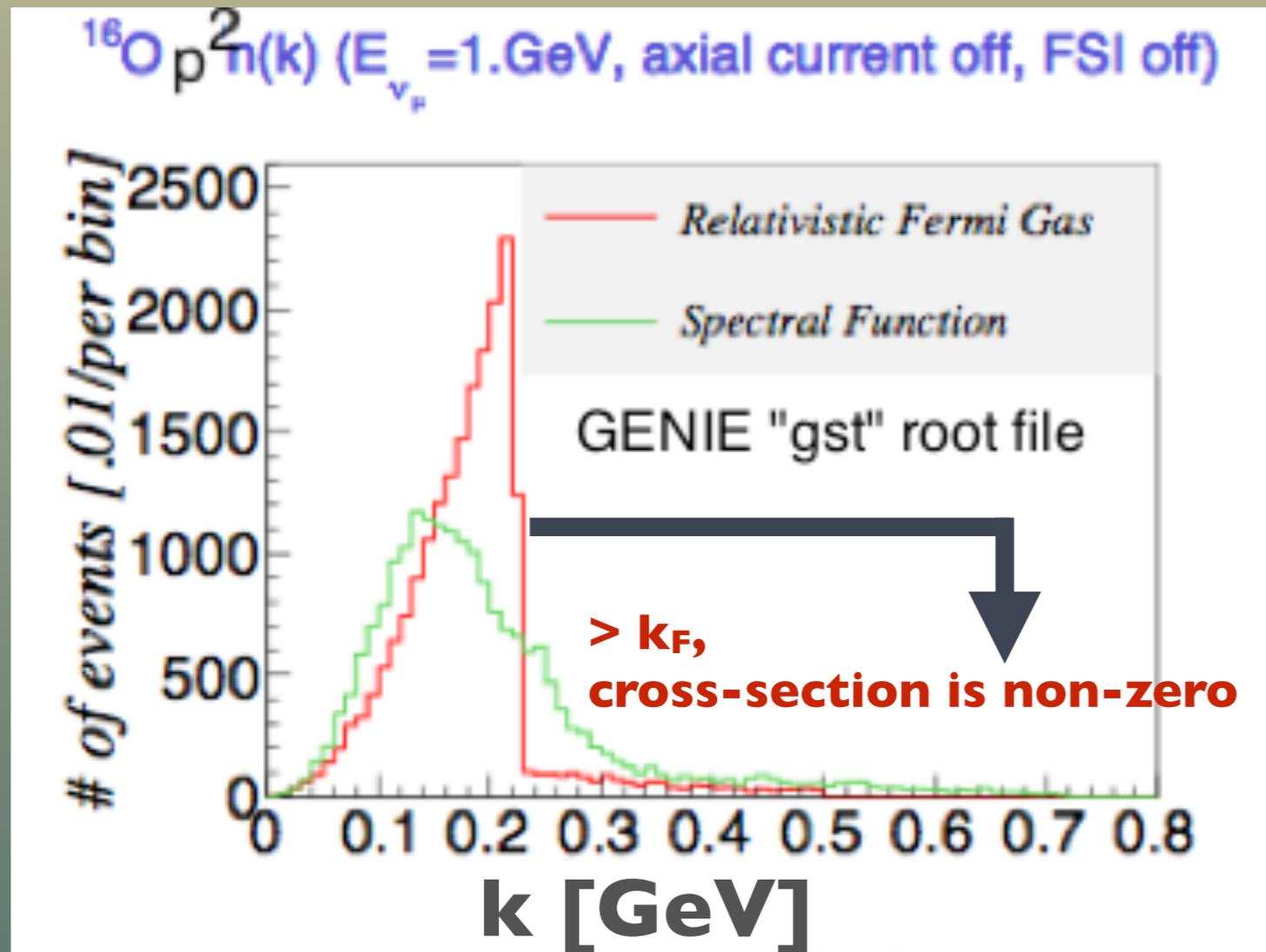
- SF model (1p-1h : the simplest case)

$$P(|\vec{p}|, E) = \left| \langle {}^{40}\text{Ar} | {}^{39}\text{Ar}, p \rangle \right|^2 \delta(E_{40\text{Ar}} - E_{39\text{Ar}} - m_n + E)$$

probability amplitude of knocking out one nucleon energy-momentum conservation

Math Form of Spectral Functions
 telling you the “probability” of knocking out one nucleon
 with one specific quantum number

SPECTRAL FUNCTION IN CROSS-SECTION CALCULATION



- in RFGM, nucleons sitting near the Fermi sea are most likely to interact with beam particles
- the spectral function theory, however, demonstrates the non-zero probability of interacting with nucleons with translational momentum above the Fermi sea as a result of N-N interactions

probability of interacting with one nucleon with a quantum number

$$\sigma_{eA} = K \sigma_{ep} P(\mathbf{p} - \mathbf{q}, \omega - T_p)$$

integrating over the entire phase space $\rightarrow dp^3 = p^2 dp$

A more realistic initial-state nuclear shell model for ^{40}Ar is needed

why nuclear physicist cares?

- what is the spectroscopic factor for ^{40}Ar ?
- what is the separation energy of proton and neutron with the specific quantum number on each shell?
- what is the energy-dependence of each shell's momentum?

far beyond nuclear physics

- beam energy/flux are un-determined
- Q^2 at the interaction vertex is not constrained
- no way to detect final-state neutrinos
- hard to do final-state energy reconstruction

why neutrino physicist cares?

- RFGM vs. SF (how different?)
- the energy transfer or Q^2 on the interaction vertex of neutrino-nucleus
- the probability of knocking out one nucleon with one specific quantum number determines the size of neutrino-nucleus cross-section
- non negligible effect on the determination of the neutrino energy either for just CCQE or CC-all
- oscillation parameters determination are affected by neutrino energy reconstruction uncertainties
- fundamental constants like M_a affected by nuclear model - new nuclear model validation

Numerical Implementation of lepton-nucleus interactions and its effect on neutrino oscillation analysis

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²*Department of Physics, Okayama University, Okayama 700-8530, Japan*

³*University of Warwick, Department of Physics, Coventry, United Kingdom*

(Dated: April 4, 2014)

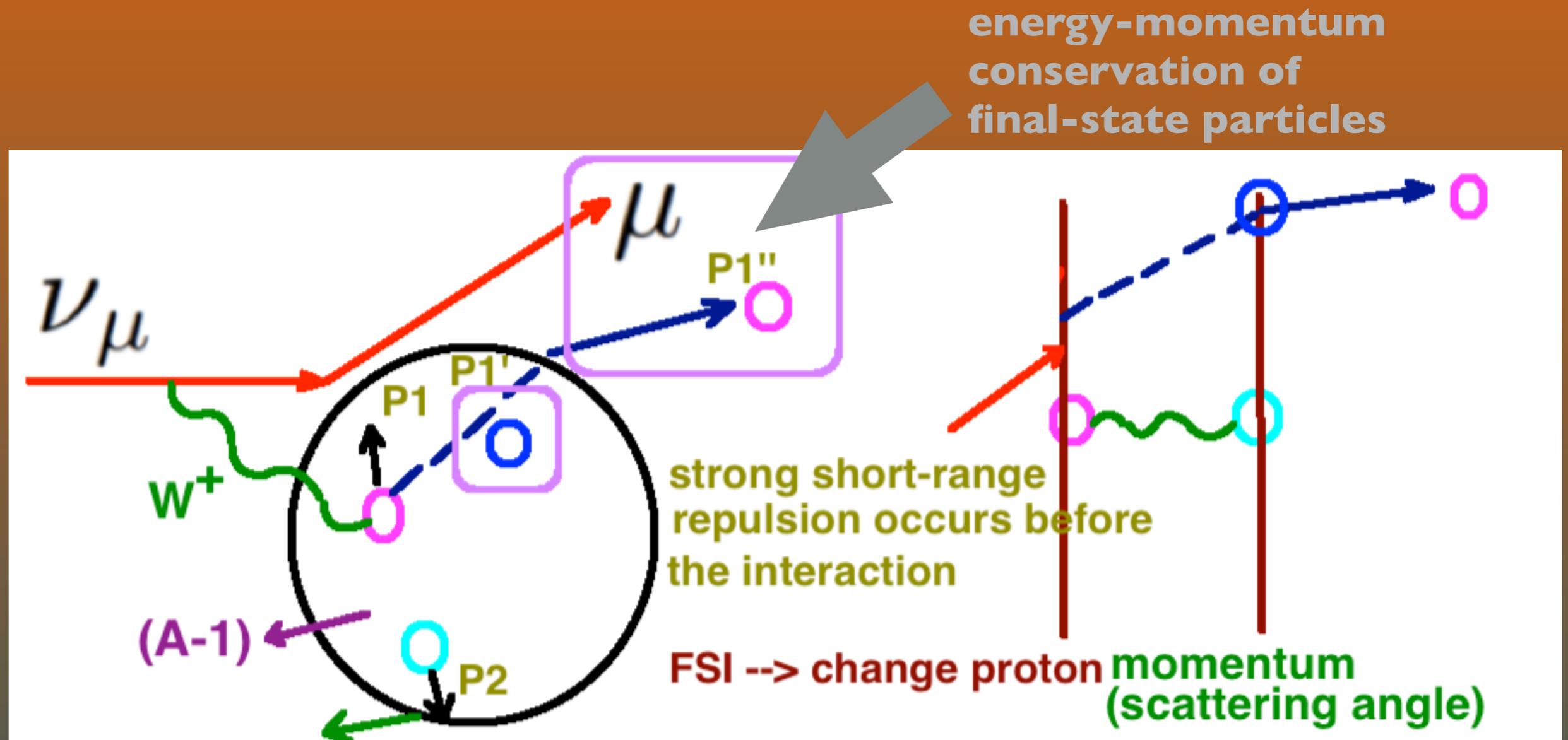
We discuss the implementation of the nuclear model based on realistic nuclear spectral functions in the GENIE neutrino interaction generator. Besides improving on the Fermi gas description of the nuclear ground state, our scheme involves a new prescription for Q^2 selection, meant to efficiently enforce energy momentum conservation. The results of our simulations, validated through comparison to electron scattering data, have been obtained for a variety of target nuclei, ranging from carbon to argon, and cover the kinematical region in which quasi elastic scattering is the dominant reaction mechanism. We also analyze the influence of the adopted nuclear model on the determination of neutrino oscillation parameters.

PACS numbers: 14.60.Pq, 14.60.Lm

structure functions for ^{12}C , ^{16}O , ^{40}Ca and ^{40}Ar (not well-determined yet) are “temporarily” implemented in GENIE at present. all modifications which we made in our studies and generated results from GENIE are identified as GENIE v2.8.0+ “nuVT”

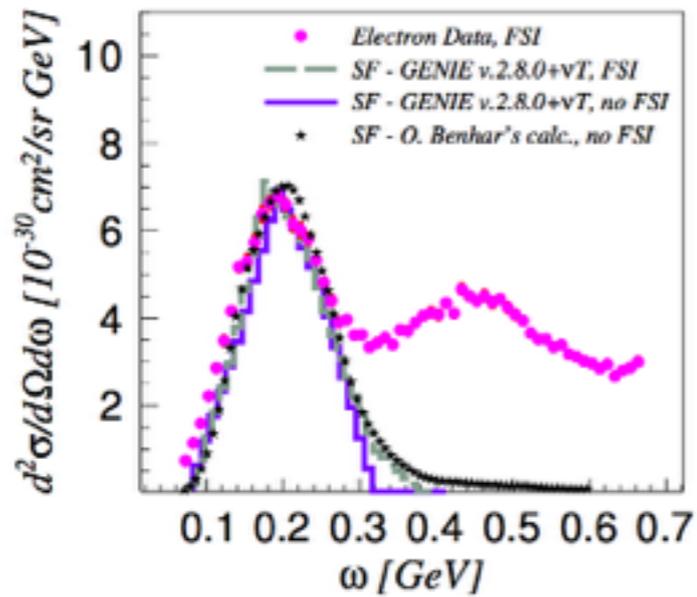
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Final-State-Interactions (FSI)

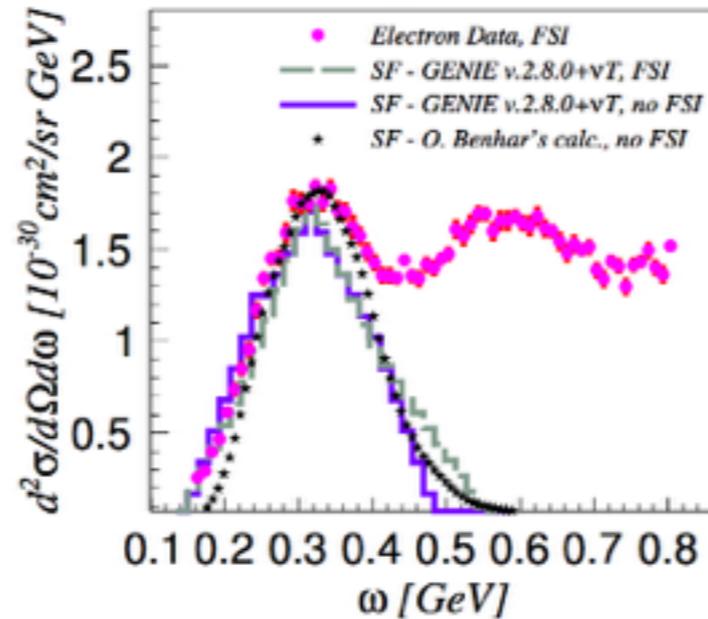


an optical model used to describe FSI incorporates within the spectral function approach

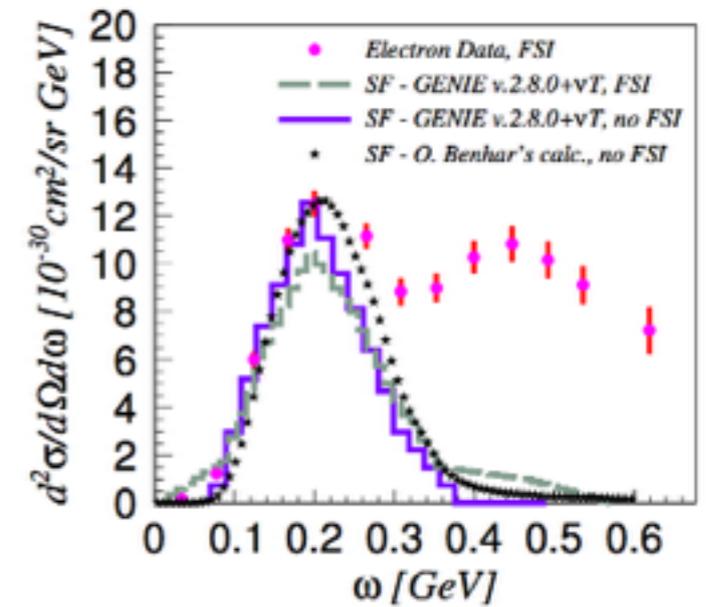
Electron Validation ^{12}C and ^{40}Ca



(a) $e + \text{C} \rightarrow e' + X$, $E_e = 0.961$ GeV, $\theta_e = 37.5$ deg



(b) $e + \text{C} \rightarrow e' + X$, $E_e = 1.299$ GeV, $\theta_e = 37.5$ deg



(c) $e + \text{Ca} \rightarrow e' + X$, $E_e = 0.841$ GeV, $\theta_e = 45.5$ deg

The FSI effects can be consistently described within the spectral function approach. Please see Artur Ankowski's presentation.

Improving the accuracy of neutrino energy reconstruction
in charged-current quasielastic scattering off nuclear targets

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²INFN and Department of Physics, "Sapienza" Università di Roma, I-00185 Roma, Italy

(Dated: April 24, 2014)

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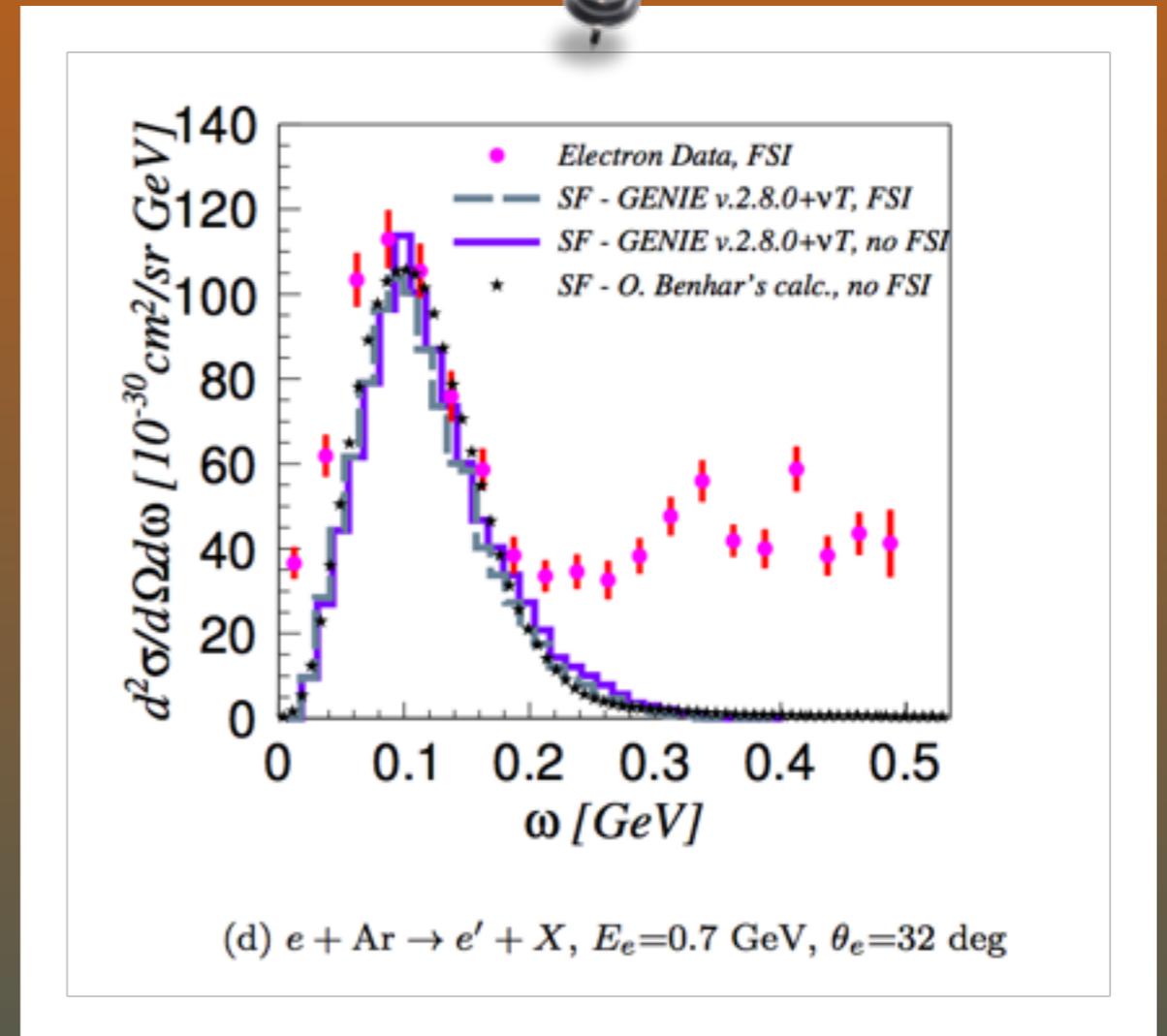
^{40}Ar - a very crude and preliminary structure functions

Owing to the lack of electron scattering data, the energy-momentum dependence in structure functions of argon is not strongly constrained



JLab Hall-A PAC 4I (Jul. 2014)
electron scattering experiment on ^{40}Ar

UVa / VT / Syracuse / LANL / INFN-Rome / JLab (Hall-A)



Neutrino Cross-Section

RFGM vs. SF

GENIE / Omar Benhar's cal.

Neutrino Cross-Section

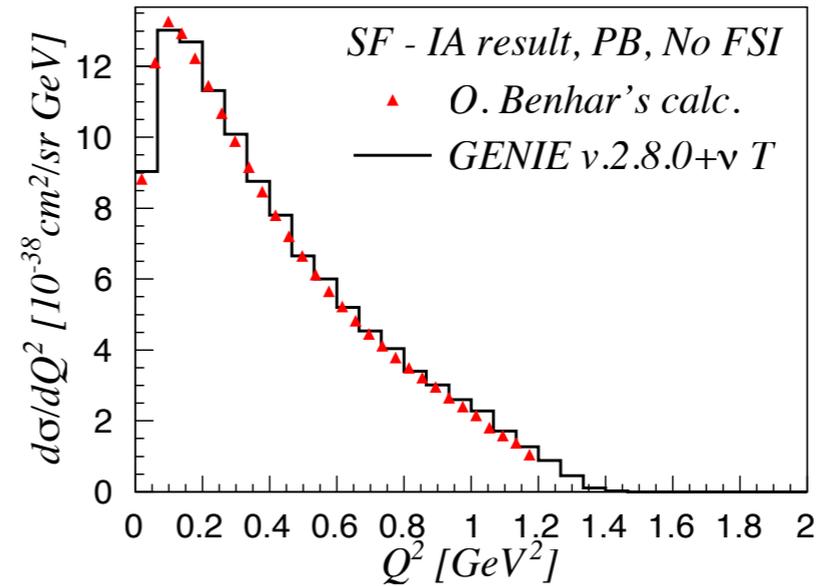
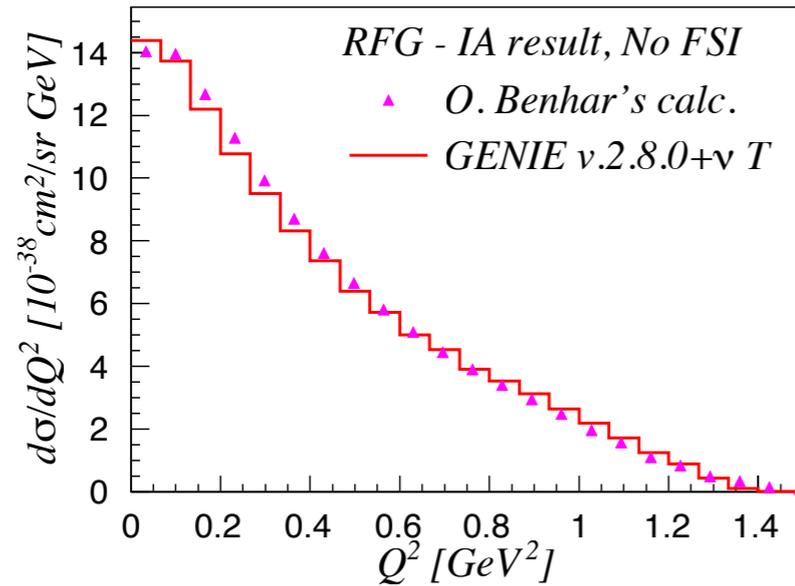
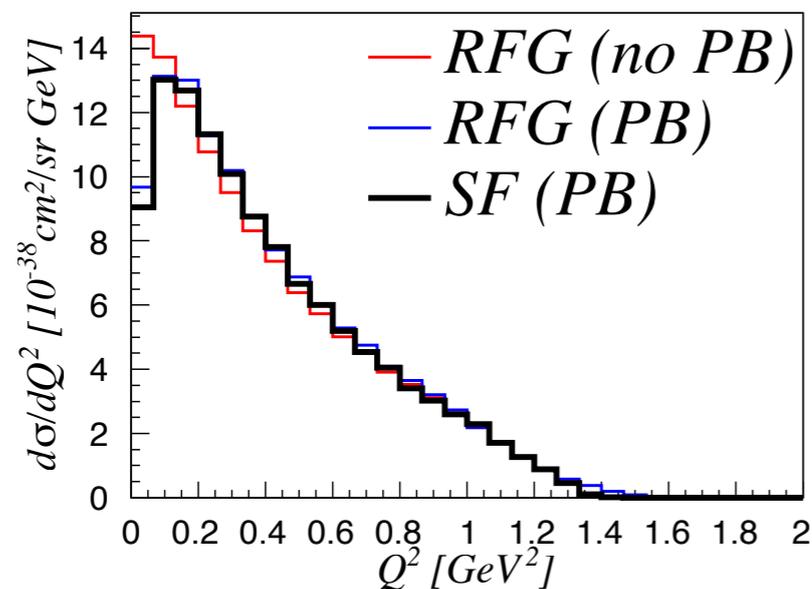


FIG. 6. (Color online). Comparison of the $d\sigma/dQ^2$ obtained from 2×10^5 CCQE events with $E_\nu = 1$ GeV in oxygen obtained using RFGM and SF.



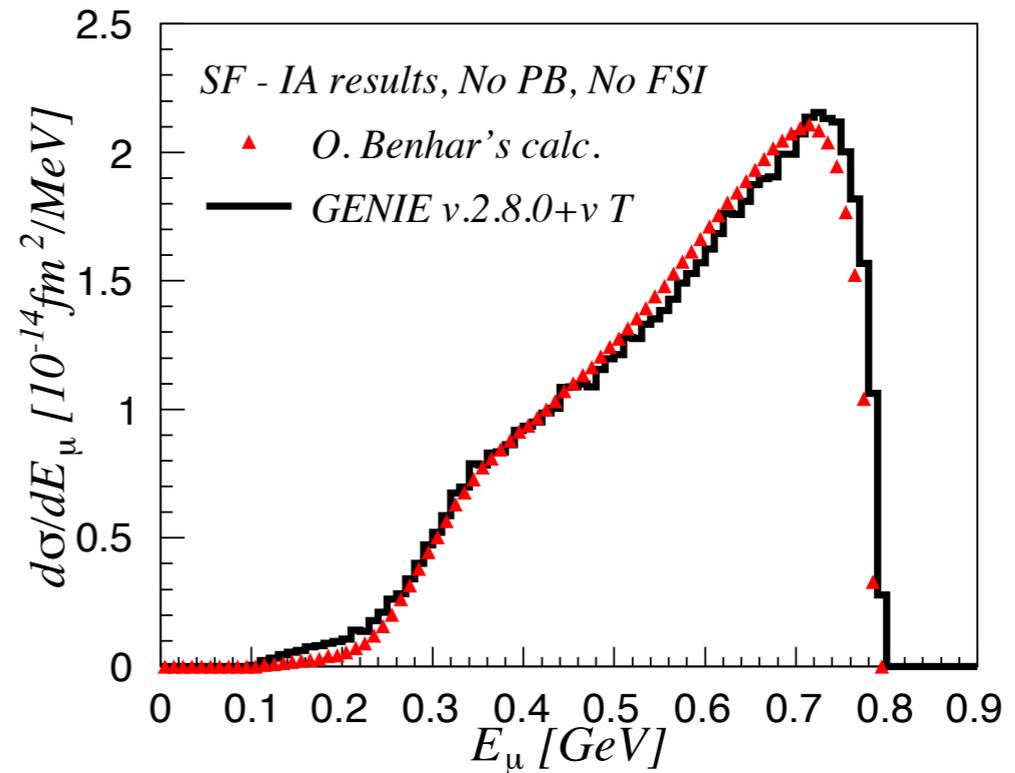
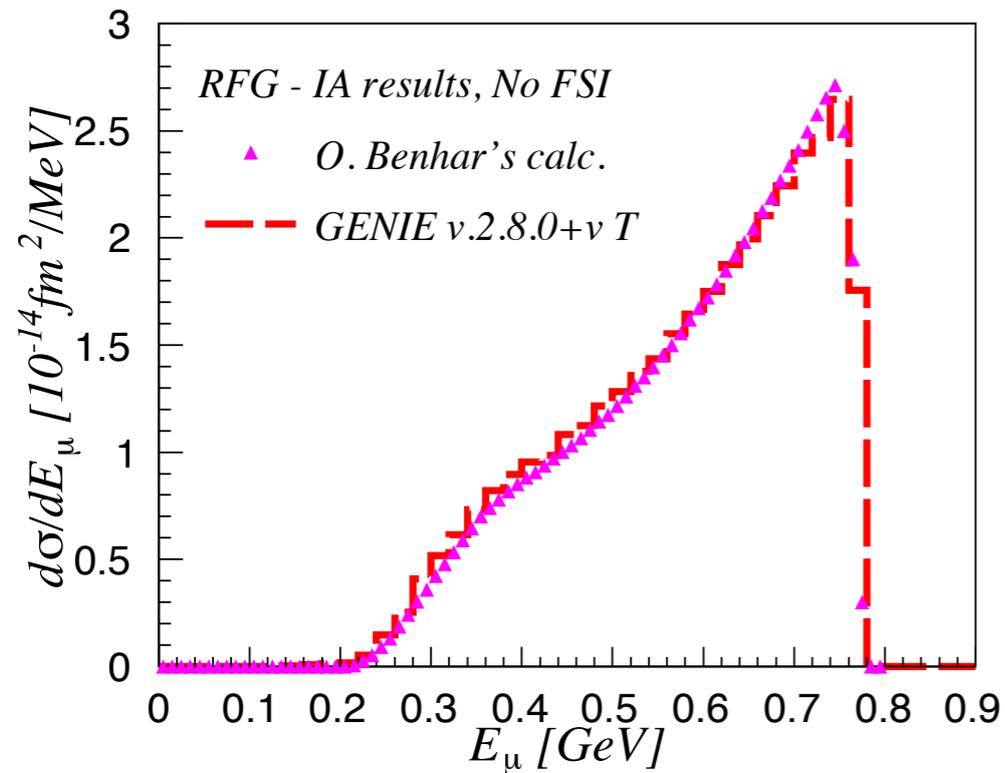
courtesy of O. Benhar, N. Farina,
 H. Nakamura, M. Sakuda, R. Seki
 PRD 72, 053005 (2005)

very good agreement between
 simulation and theoretical
 calculation on Q^2

Neutrino Cross-Section

$\nu + O \rightarrow \mu + X$, GENIE 2.8.0 + νT , no Pauli Blocking, no FSI

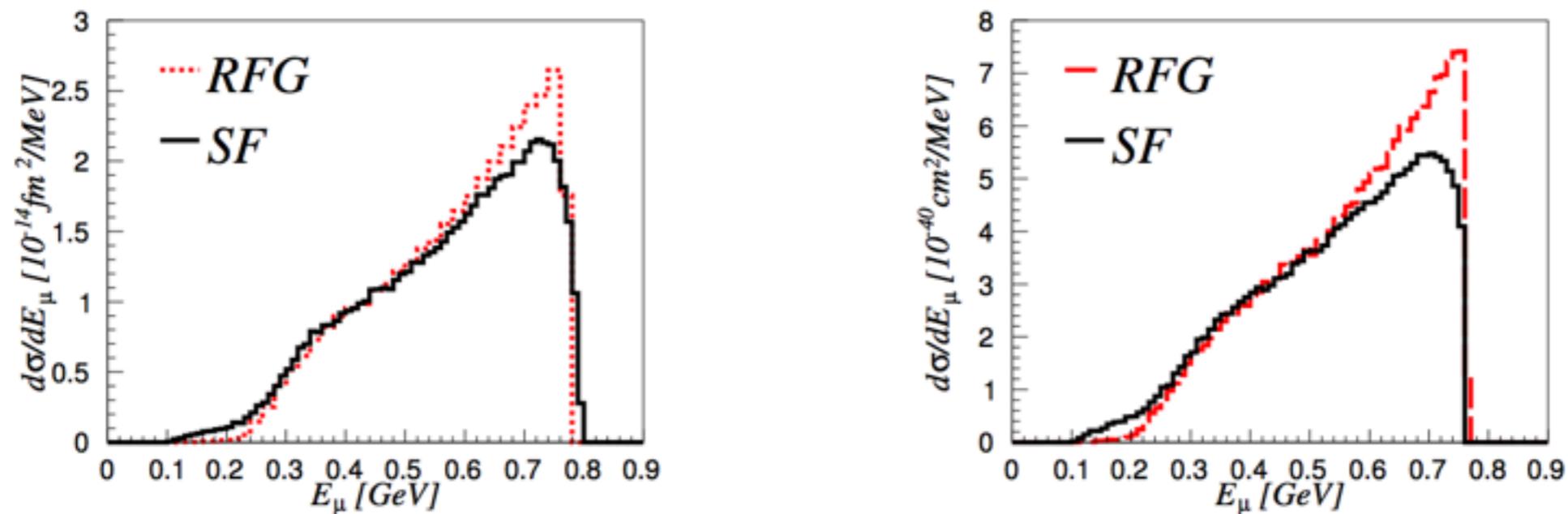
courtesy of O. Benhar, N. Farina, H. Nakamura, M. Sakuda, R. Seki
PRD 72, 053005 (2005)



Neutrino Cross-Section

courtesy of A. M. Ankowski nucl-th/0608014v1 4 Aug 2006

courtesy of A. M. Ankowski, Jan T. Sobczyk PRC 77, 044311 (2008)



(a) $\nu + O \rightarrow \mu + X$, GENIE 2.8.0 + νT , no Pauli Blocking, no FSI (b) $\nu + Ar \rightarrow \mu + X$, GENIE 2.8.0 + νT , Pauli Blocking and FSI included

FIG. 7. (Color online). Comparison of the differential CCQE cross sections $d\sigma/dE_\mu$ of oxygen (a) and argon (b) at neutrino energy $E_\nu = 800$ MeV, obtained using GENIE 2.8.0 + νT with RFGM and SF.

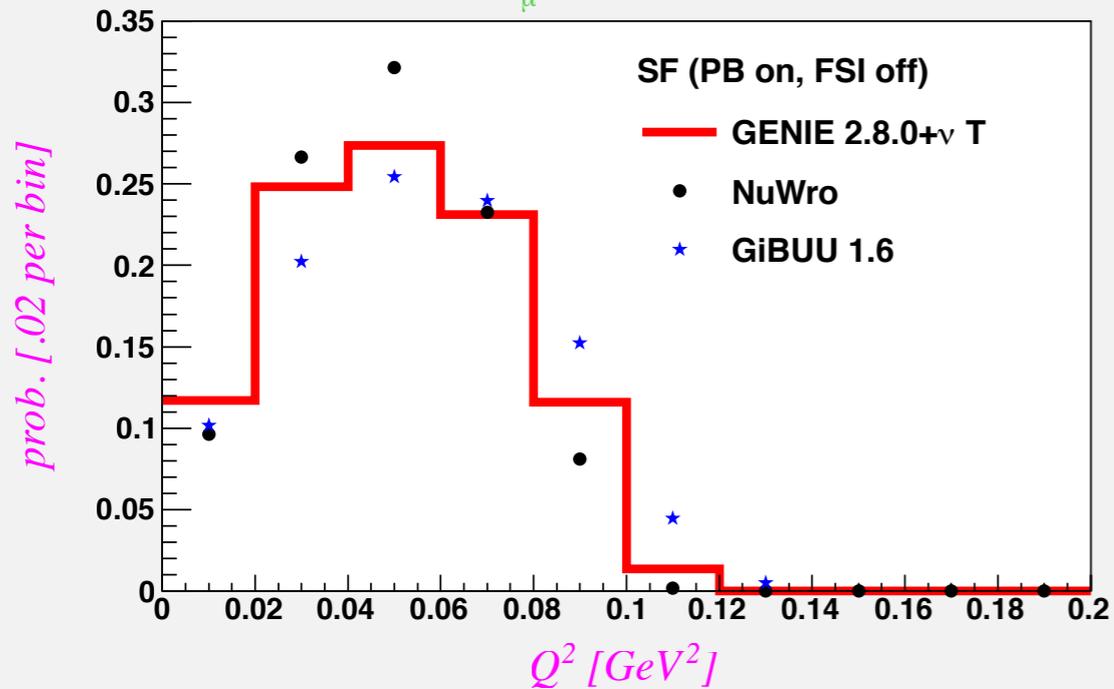
very good agreement between simulation and theoretical calculation. however, Ar is now an approximation and more calculations are needed

Neutrino Cross-Section

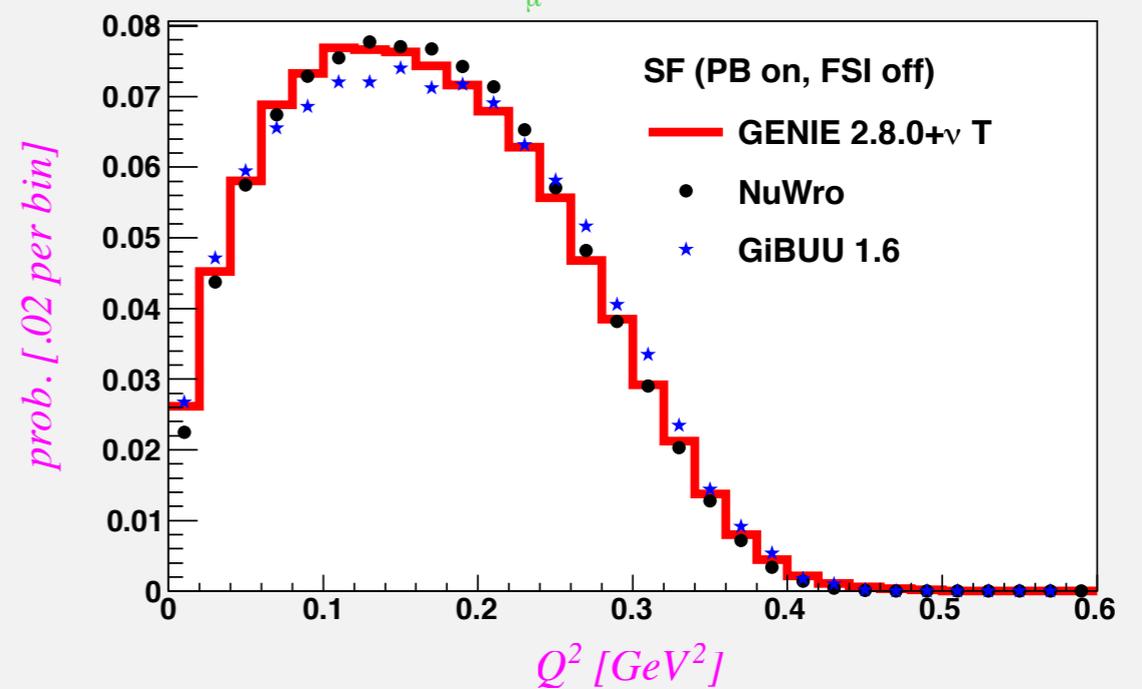
**GENIE vs. GiBUU vs. NuWro
vs. O. Benhar's cal.**

Neutrino Cross-Section

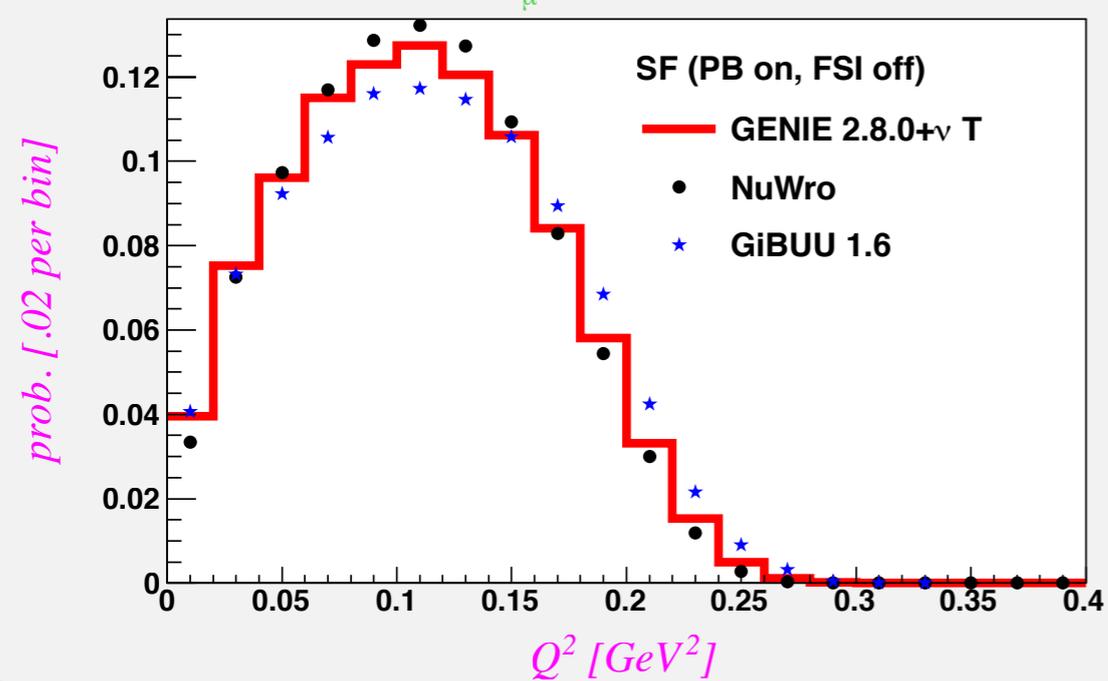
Q^2 on ^{12}C at $E_{\nu_\mu} = 0.2$ GeV - SF (PB)



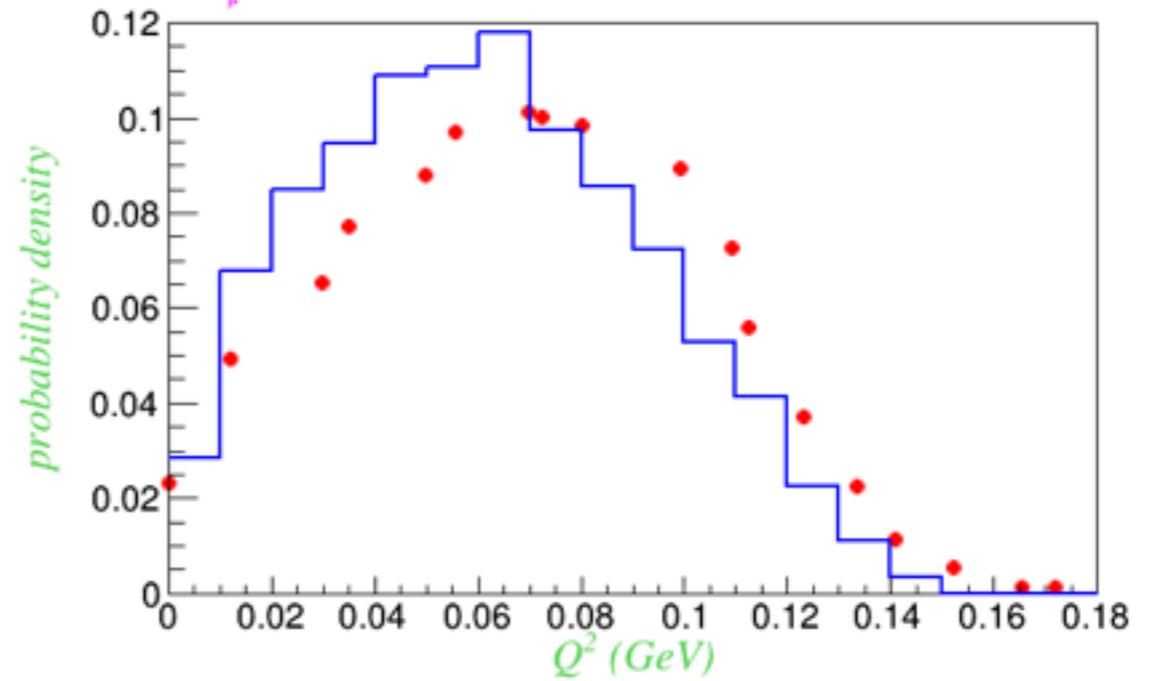
Q^2 on ^{12}C at $E_{\nu_\mu} = 0.4$ GeV - SF (PB)



Q^2 on ^{12}C at $E_{\nu_\mu} = 0.3$ GeV - SF (PB)

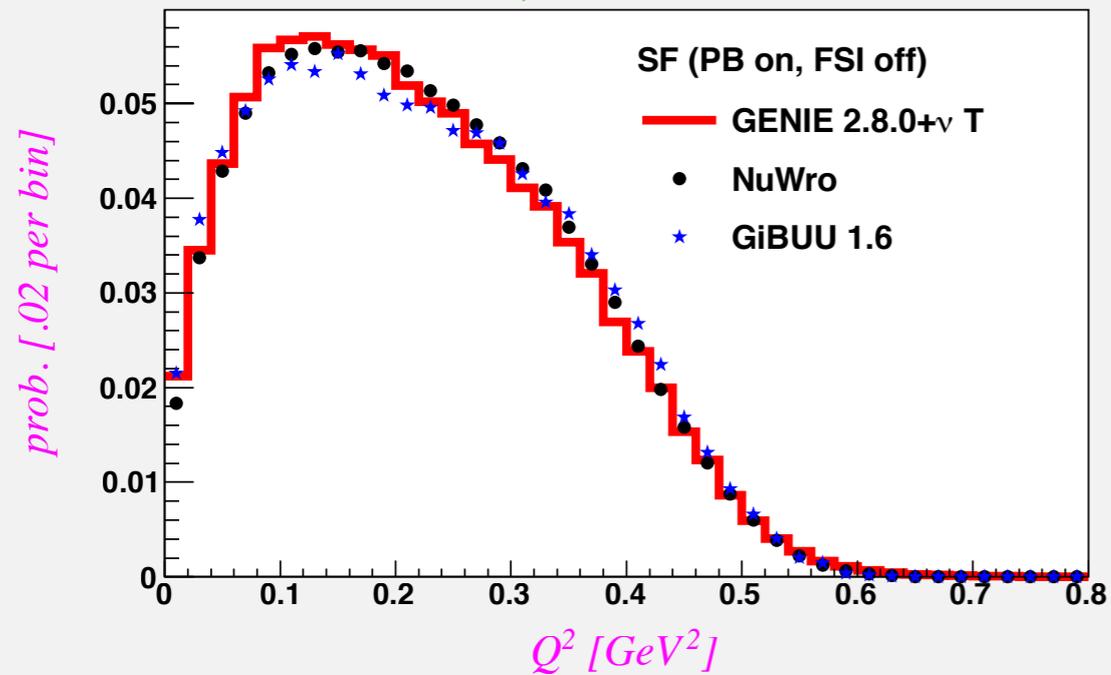


true $Q^2(E_{\nu_\mu} = 0.225$ GeV): GENIE-solid blue line, GiBUU-red dot

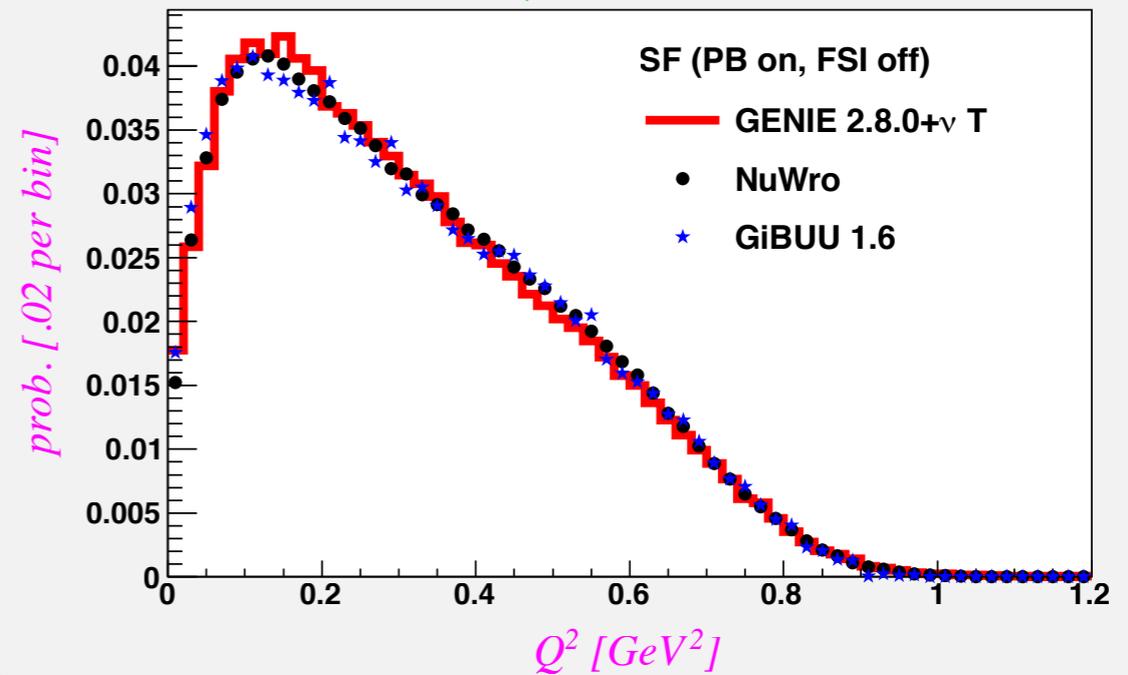


Neutrino Cross-Section

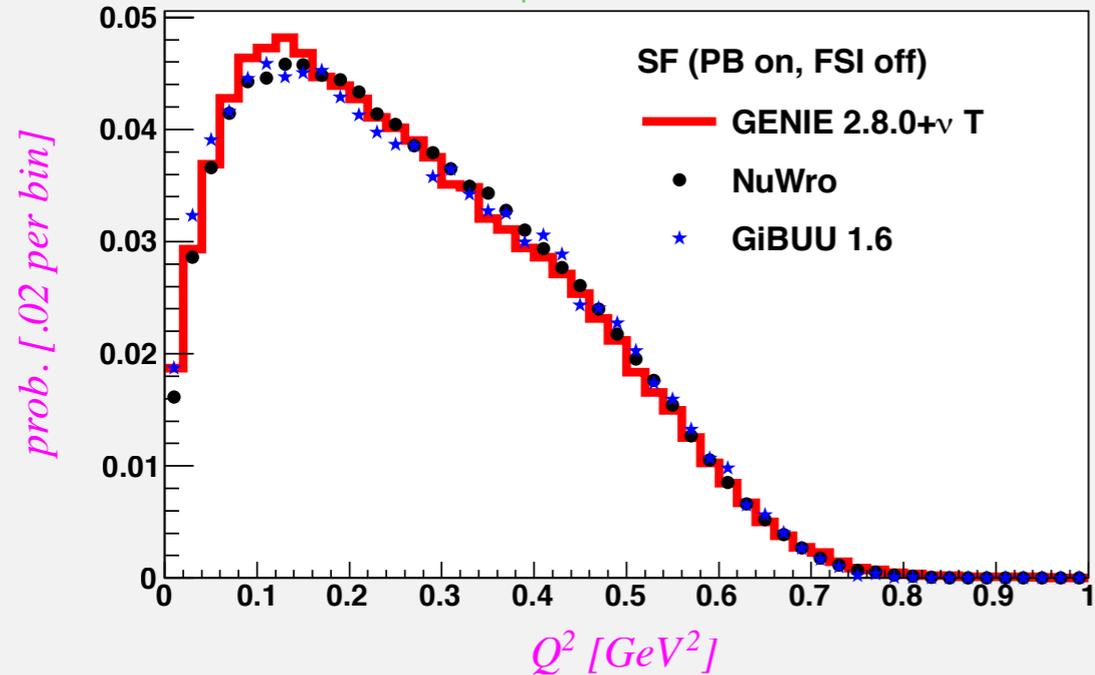
Q^2 on ^{12}C at $E_{\nu_\mu} = 0.5$ GeV - SF (PB)



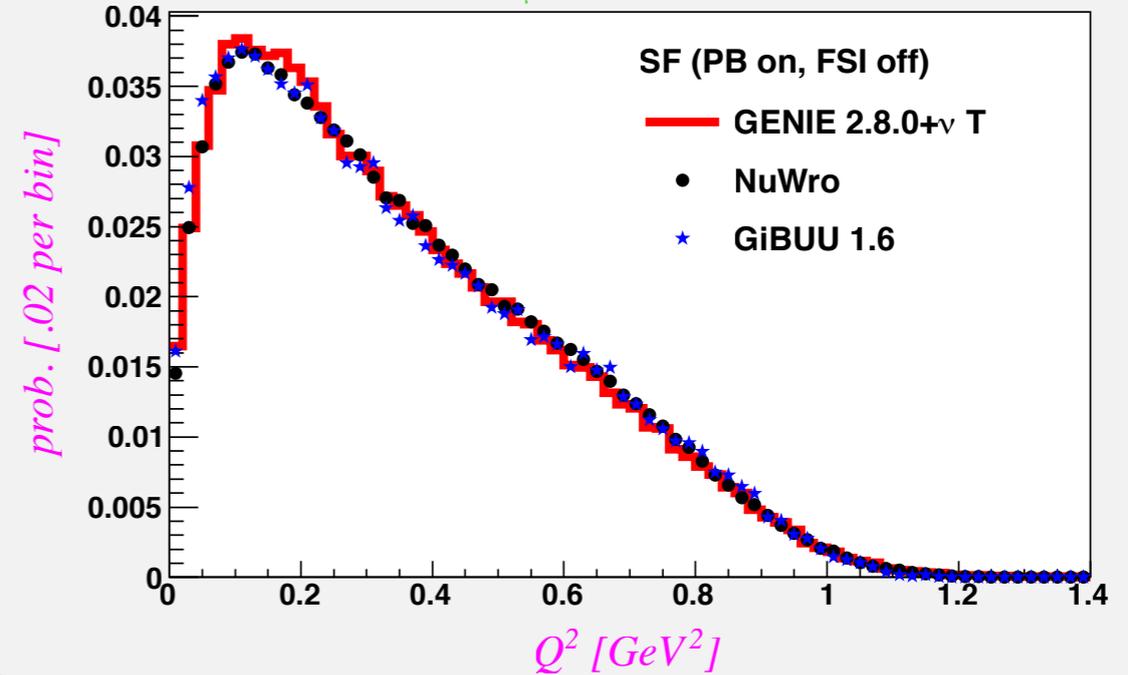
Q^2 on ^{12}C at $E_{\nu_\mu} = 0.7$ GeV - SF (PB)



Q^2 on ^{12}C at $E_{\nu_\mu} = 0.6$ GeV - SF (PB)

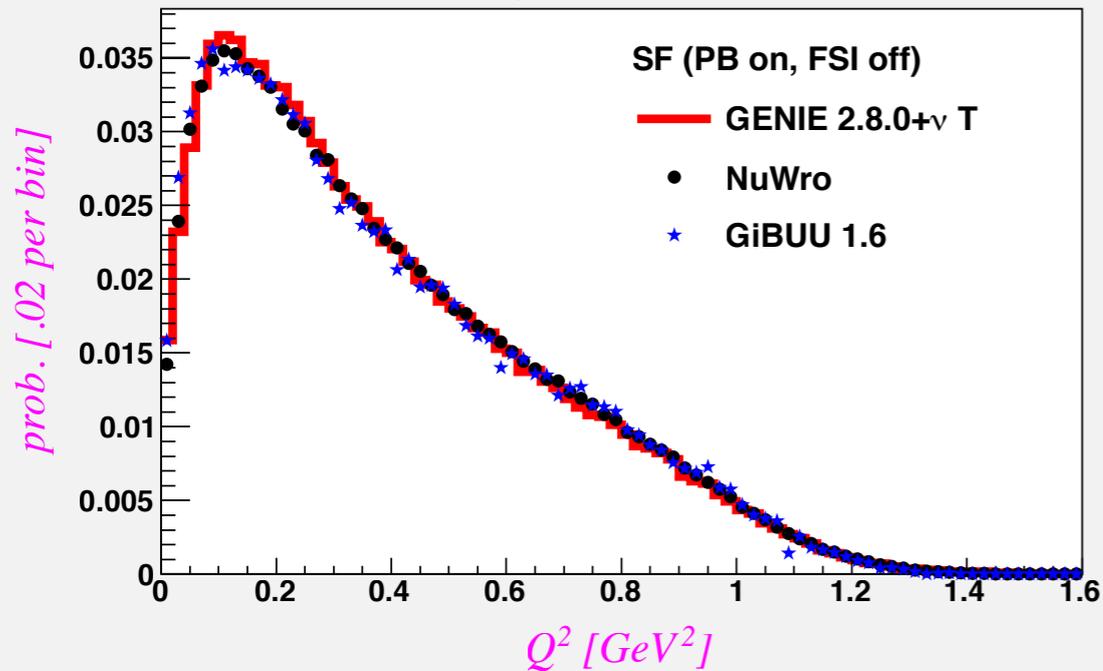


Q^2 on ^{12}C at $E_{\nu_\mu} = 0.8$ GeV - SF (PB)

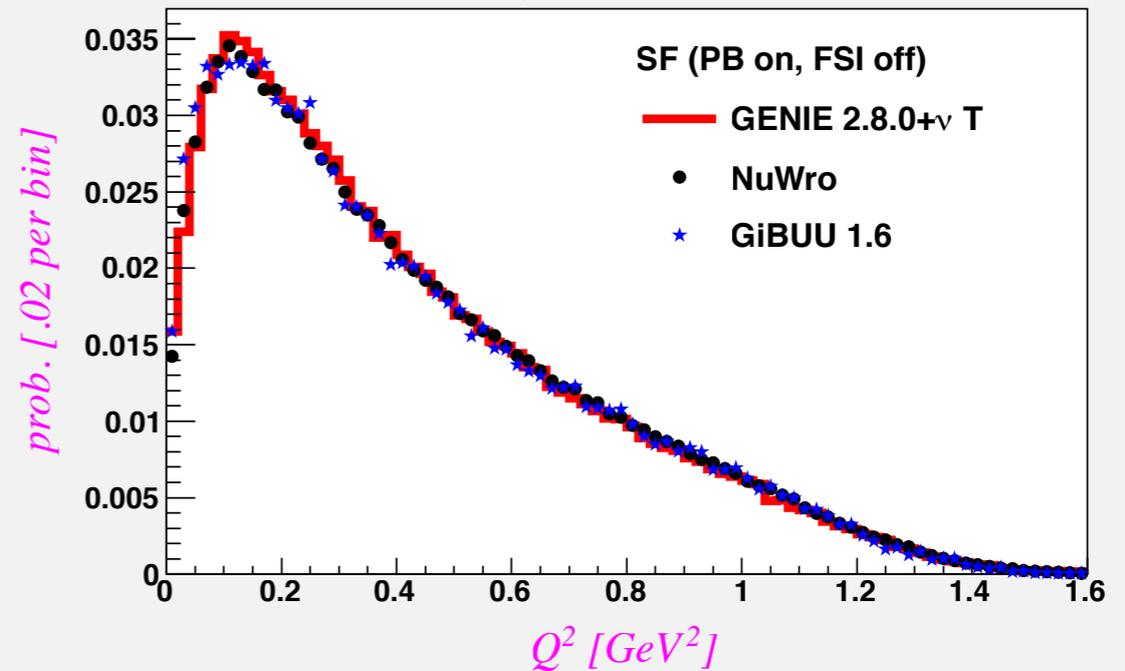


Neutrino Cross-Section

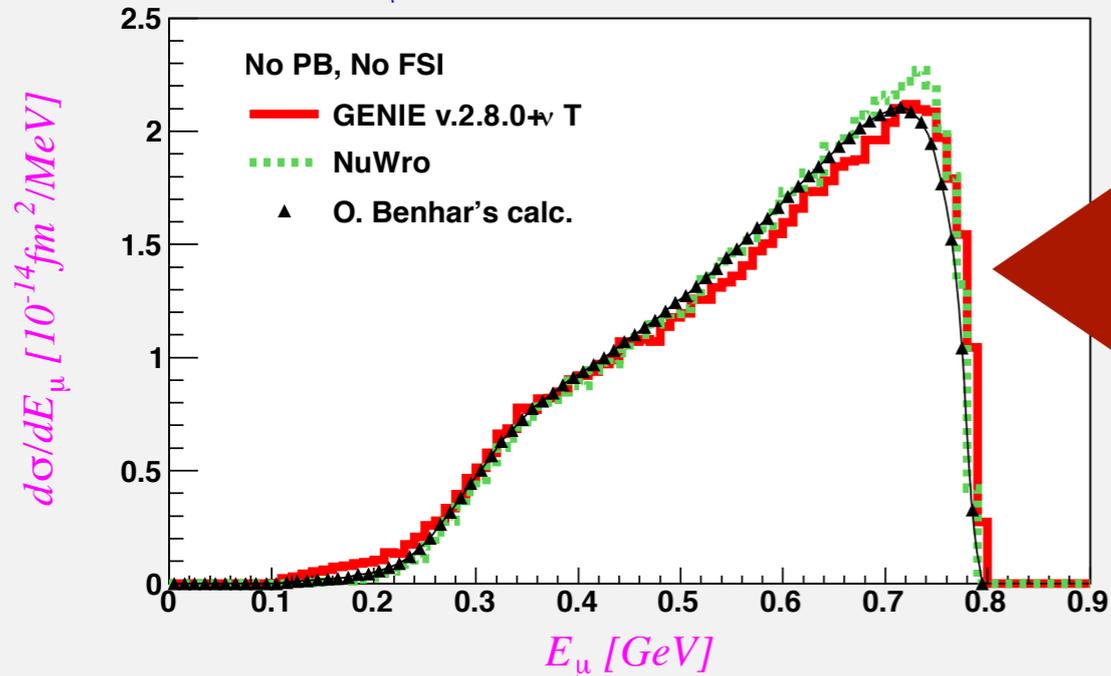
Q^2 on ^{12}C at $E_{\nu\mu} = 0.9 \text{ GeV}$ - SF (PB)



Q^2 on ^{12}C at $E_{\nu\mu} = 1.0 \text{ GeV}$ - SF (PB)



E_μ on ^{12}C at $E_{\nu\mu} = 0.8 \text{ GeV}$ - SF (no PB, no FSI)



besides silencing FSI,
turning off PB, too.
compare simulated results
to the theoretical calculation

Q^2 (with PB on) is quite similar in RFGM and SF. You see the similarity of Q^2 within GENIE, GiBUU and NuWro. But, this similarity cannot exactly tell you which nuclear model you used to compute Q^2 .

However, if you look at E_{μ} . The difference in the nuclear model option reveals (because it influences the phase space, $(|q|, w)$, at the interaction vertex). That is, the shape of E_{μ} reflects which nuclear model you apply to computing your cross-section. We have seen that E_{μ} from GiBUU is very close to the one derived from RFGM in GENIE and NuWro.

That implies NO SF in GiBUU.

**Does the nuclear model
influence the extracted
neutrino oscillating
parameters?**

Using GLoBES analysis to “quantify” the answer by feeding one toy model

this toy model is developed by adapting T2K flux and near detector’s efficiency. Note: this is just a toy model used to simplify the simulation loading. this simulation is NOT exclusively for T2K experiment.

**O. Lalakulich, U. Mosel, and K. Gallmeister,
Phys.Rev. C86, 054606 (2012), 1208.3678.**

**P. Coloma and P. Huber
Phys.Rev. Lett.111, 221802 (2013)**

Experimental Setup - Simulation

- Ideal and perfect near detector (^{12}C or ^{16}O), 1 km, 1kton
- Far detector at 295 km, 22.5 kton
 - **Oxygen**
 - Carbon (RFG and SF)
- Use T2K flux, peak at 0.6 GeV, 750kW, 5 years running
- Use SK reconstruction efficiency as function of energy
- Use migration matrices produced by **GENIE 2.8.0+ ν T**

Migration Matrix is reconstructed energies as a function of true energies

- Muon neutrino disappearance only -> fit to atmospheric parameters

Go beyond simple case

P. Coloma, P. Huber, C.-M. Jen and C. Mariani

Phys. Rev. D 89, 073015 (2014)

- Use different nuclear models - RFG and SF - and evaluate effects on neutrino oscillation parameters
- Use one neutrino generator (GiBUU) to simulate the nuclear effects and use another neutrino generator (GENIE) to extract the oscillation parameters
- In a real experiment the “real” effects from data will be used in the oscillation analysis together with “some” simulation of nuclear effects
- Neutrino generators are “enough” different to help understanding what will be the effect of different nuclear models on neutrino oscillation analyses

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GLOBES Fit

C.-M. Jen,¹ A. Ankowski,² O. Benhar,^{1,*} A.P. Furmanski,³ L. N. Kalousis,¹ and C. Mariani¹

hep-ex/1402.6651v2

- Neglecting all FSI and multinucleon contributions, we can compute the number of events as:

$$N_i^{QE} = \sigma_{QE}(E_i)\phi(E_i)P_{\mu\mu}(E_i)$$

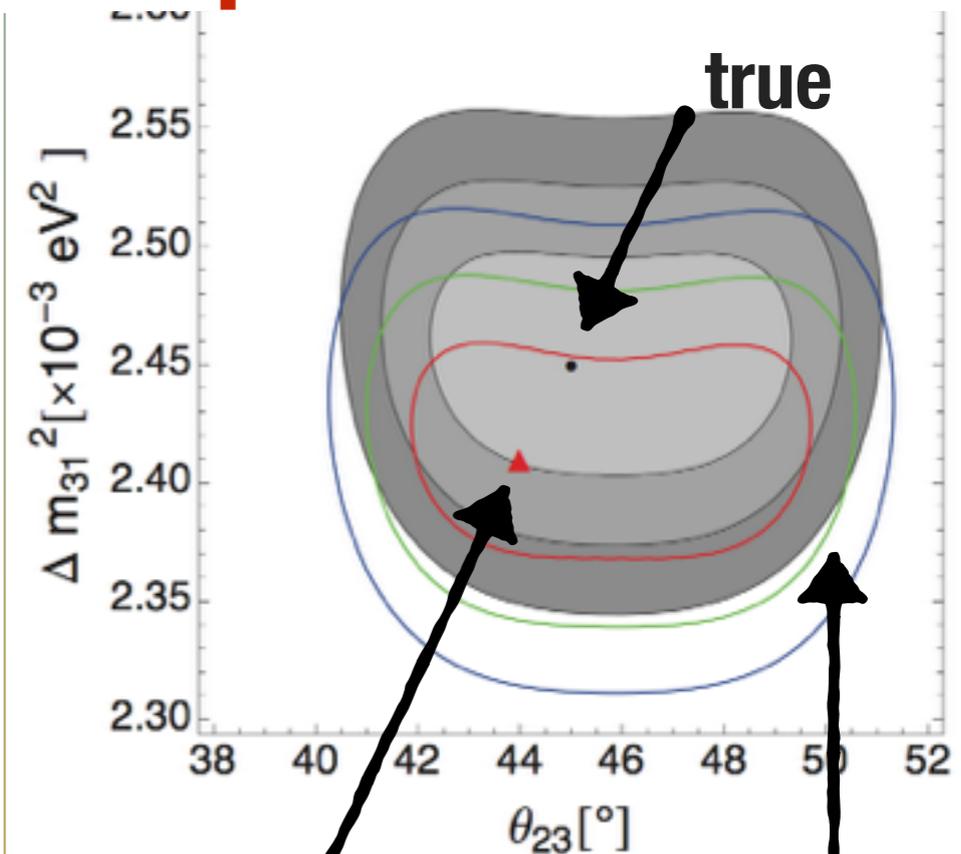
- However, in practice we will observe a different distribution at the detector, given by:

$$N_i^{QE-like} = \sum_j M_{ij}^{QE} N_j^{QE} + \sum_{non-QE} \sum_j M_{ij}^{non-QE} N_j^{non-QE}$$

- However, an intermediate situation would most likely take place:

$$N_i^{test}(\alpha) = \alpha N_i^{QE} + (1 - \alpha) N_i^{QE-like}$$

Coloma and Huber, 1307.1243 [hep-ph]



SF - reconstructed from the true QE dynamics

1, 2 and 3σ allowed regions

- **the event distribution is a convolution of cross-section, flux, detector efficiency, oscillation probability and migration matrix**
- **different nuclear models consider different nuclear effects in treating nucleon's kinematics**
- **as a result, event distributions are different for different nuclear models**

Chun-Min (Mindy) Jen, Center for Neutrino Physics, Virginia Tech

Summary of results

Input “true” Values

$$\begin{aligned} \theta_{12} &= 33.2^\circ & \Delta m_{21}^2 &= 7.64 \times 10^{-5} \text{ eV}^2 \\ \theta_{13} &= 9^\circ & \Delta m_{31}^2 &= 2.45 \times 10^{-3} \text{ eV}^2 \\ \theta_{23} &= 45^\circ & \delta &= 0^\circ \end{aligned}$$

Fitted Values

True	Fitted	$\theta_{23,min}$	$\Delta m_{31,min}^2 [\text{eV}^2]$	χ_{min}^2	σ_a
GENIE (^{16}O)	GENIE (^{12}C)	44°	2.49×10^{-3}	2.28	–
GiBUU (^{16}O)	GENIE (^{16}O)	41.75°	2.69×10^{-3}	47.64	–
		47°	2.55×10^{-3}	20.95	5%
GiBUU (^{16}O)	GiBUU (^{16}O) w/o MEC	42.5°	2.44×10^{-3}	22.38	–
GENIE (^{16}O)	GENIE (^{16}O) w/o MEC	44.5°	2.36×10^{-3}	19.54	–

Summary of results cont'd

Input “true” Values

$$\begin{aligned}\theta_{12} &= 33.2^\circ & \Delta m_{21}^2 &= 7.64 \times 10^{-5} \text{ eV}^2 \\ \theta_{13} &= 9^\circ & \Delta m_{31}^2 &= 2.45 \times 10^{-3} \text{ eV}^2 \\ \theta_{23} &= 45^\circ & \delta &= 0^\circ\end{aligned}$$

Fitted Values

True	Fitted	$\theta_{23,min}$	$\Delta m_{31,min}^2 [\text{eV}^2]$
RFGM _{2.8.0+νT}	RFGM _{2.8.0}	45.7 deg	2.45×10^{-3}
SF _{2.8.0+νT}	RFGM _{2.8.0+νT}	44 deg	2.41×10^{-3}
SF _{2.8.0+νT}	RFGM _{2.8.0}	44.5 deg	2.41×10^{-3}

Conclusions

- due to the lack of knowledge in Argon structure functions, taking electron data at JLab is needed.
- the systematics uncertainty of nuclear models for extracted oscillating parameters can be more exactly determined.

Acknowledgement :

**A. Ankowski, O. Benhar, P. Coloma, D. Day, S. Dytman,
D. Higinbotham, P. Huber, C. Mariani**

BACKUP

Chun-Min (Mindy) Jen, Center for Neutrino Physics, Virginia Tech

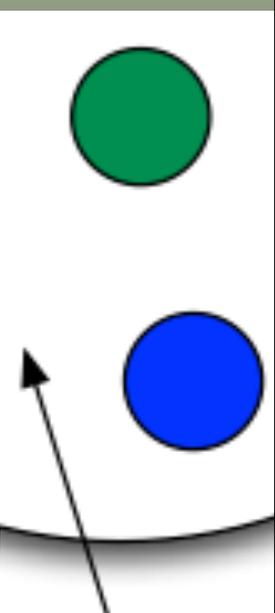
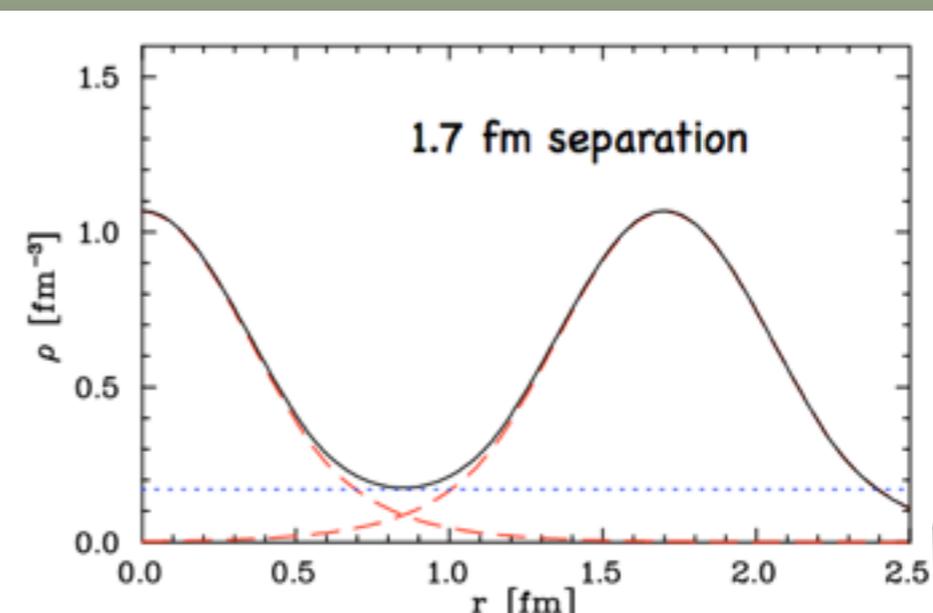
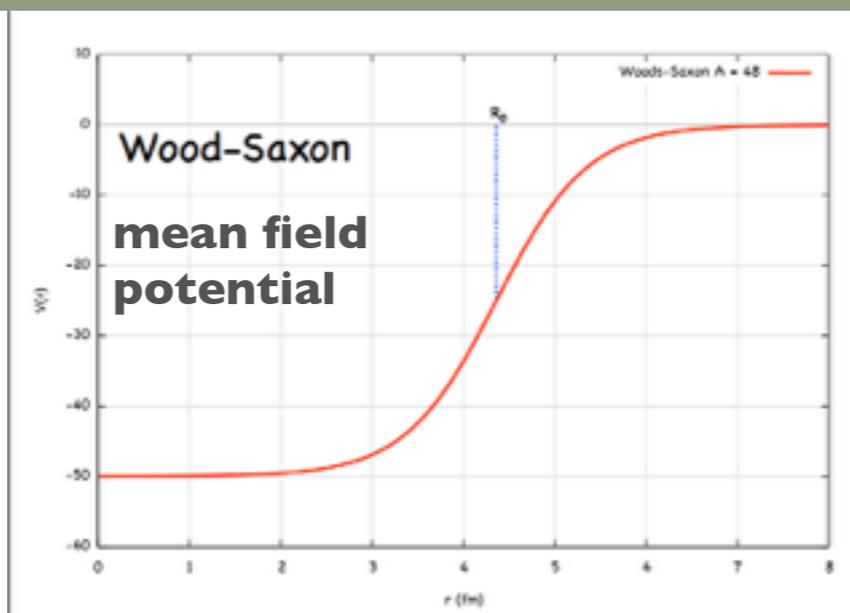
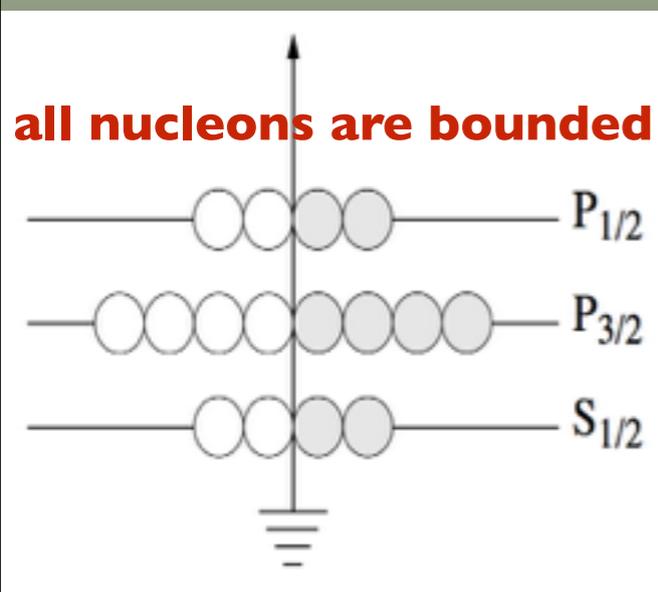
NUCLEAR MODEL

STANDARD SHELL MODEL

INDEPENDENT PARTICLE SHELL MODEL (IPSM)

0th-order (the most naive model - Fermi Gas Model) :

no N-N correlation; all nucleons sitting on bound states are regarded as quasi-free particles



$$E_{miss}/\text{binding} = \omega - T_p - T_B$$

the well-depth is determined by being adjusted to re-produce the measured E_{binding} or E_{miss}

average volume (number) density = $0.16 \text{ GeV}/\text{fm}^3$

- ❖ the energy of each shell is a delta function
- ❖ all nucleons feel the same force acting on them as a result of a mean field potential
- ❖ absence of position correlation in the ground state wave function between each pair of nucleons

courtesy of D. Day

Chun-Min (Mindy) Jen, Center for Neutrino Physics, Virginia Tech

momentum density $n(k) \leftrightarrow$ charge (\sim proton) density $\rho_{ch}(r) \text{ (fm}^{-3}\text{)}$

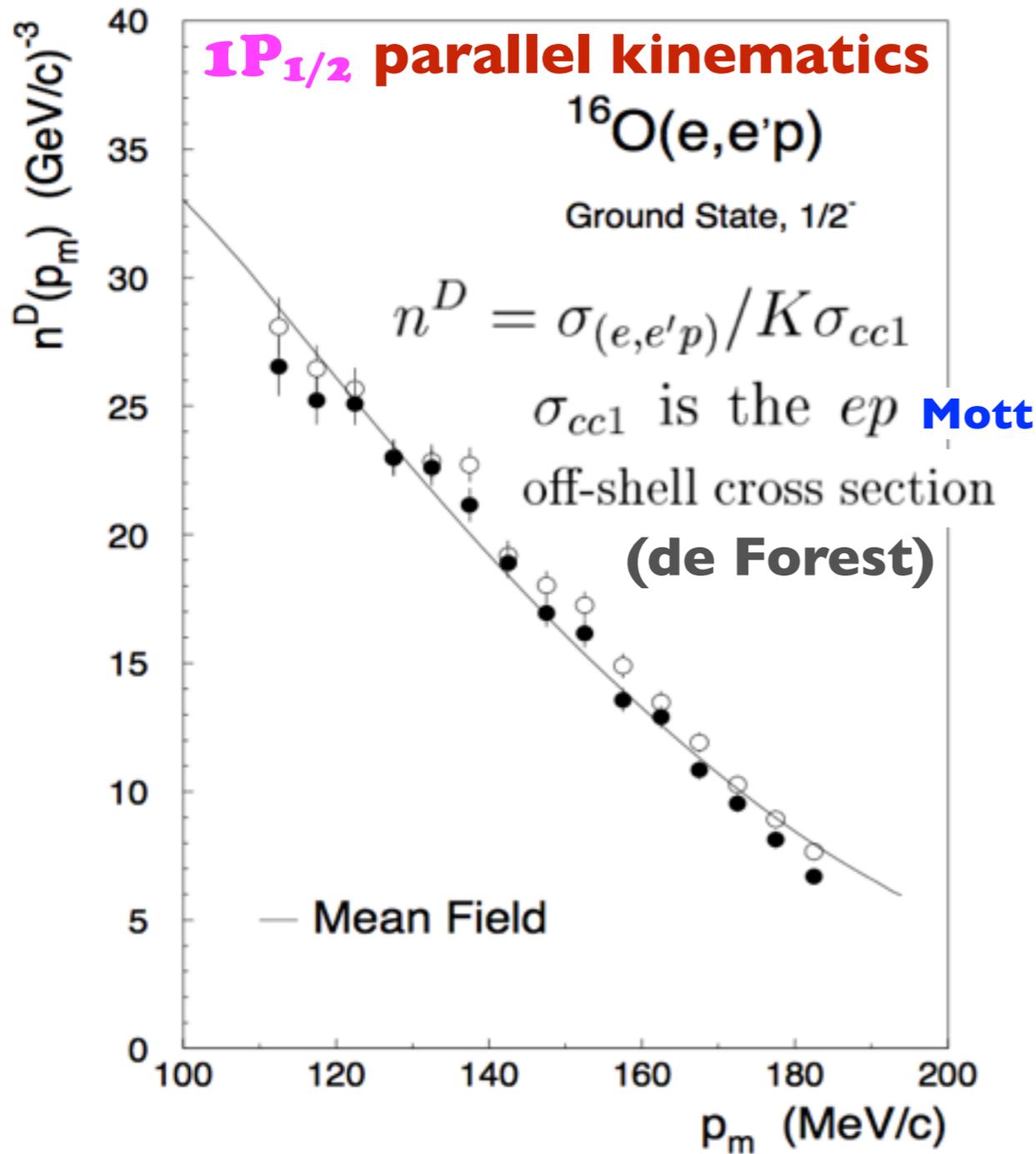


Figure 1-10: ¹⁶O(e, e'p) distorted momentum distribution for the 1p_{1/2} state measured at Mainz [15]. The kinetic energy is \sim 93 MeV. The curve is a DWIA calculation which uses a Woods-Saxon potential with parameters fit from the NIKHEF data [16], and the Schwandt optical potential [10] for final state interactions.

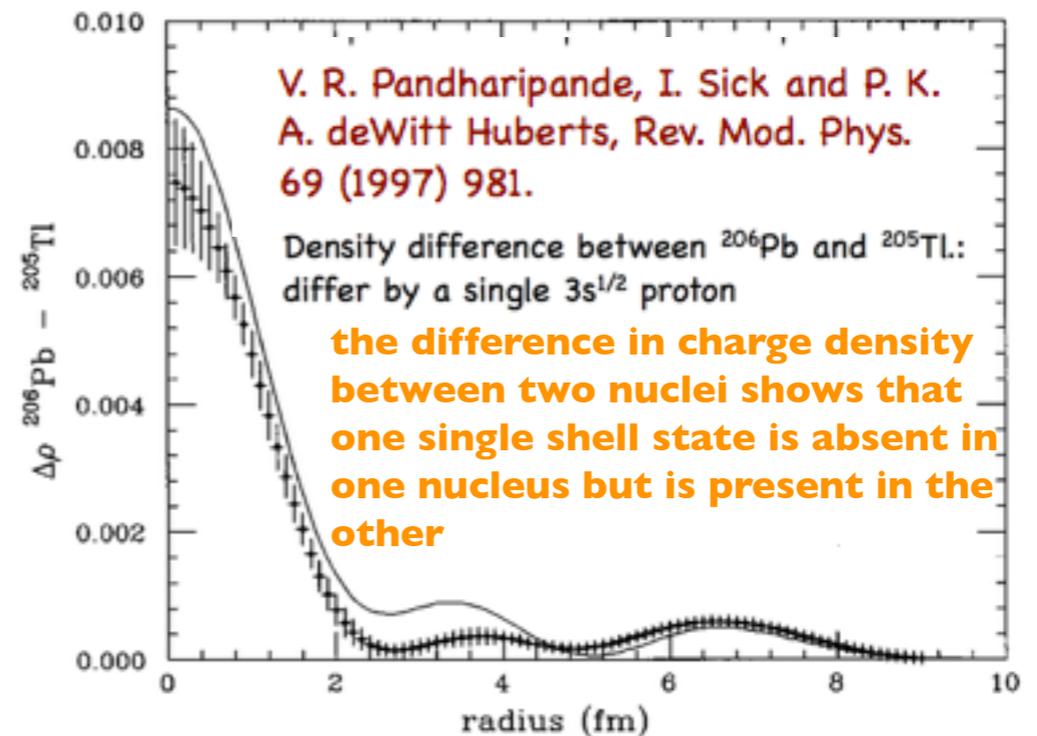
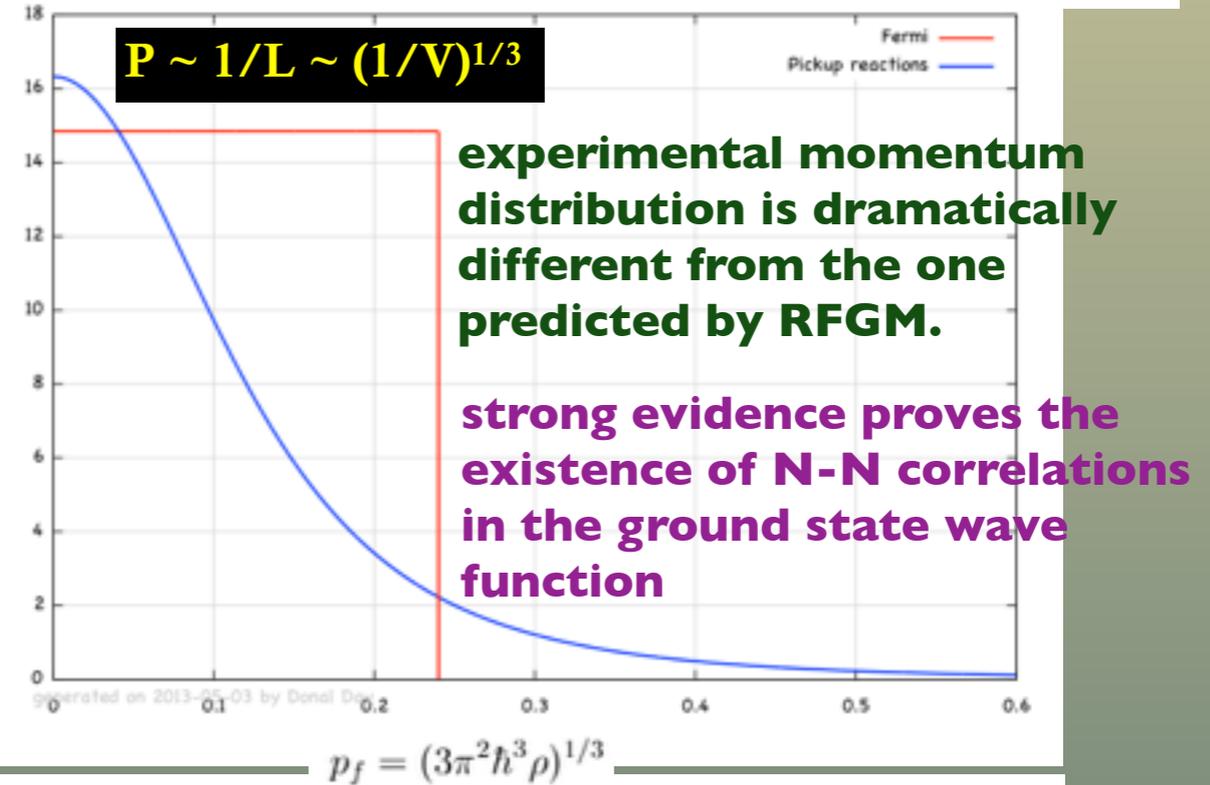


Figure 2: Charge density difference between ²⁰⁶Pb and ²⁰⁵Tl. Experiment vs. mean field calculation. Figure borrowed from ref. [2]

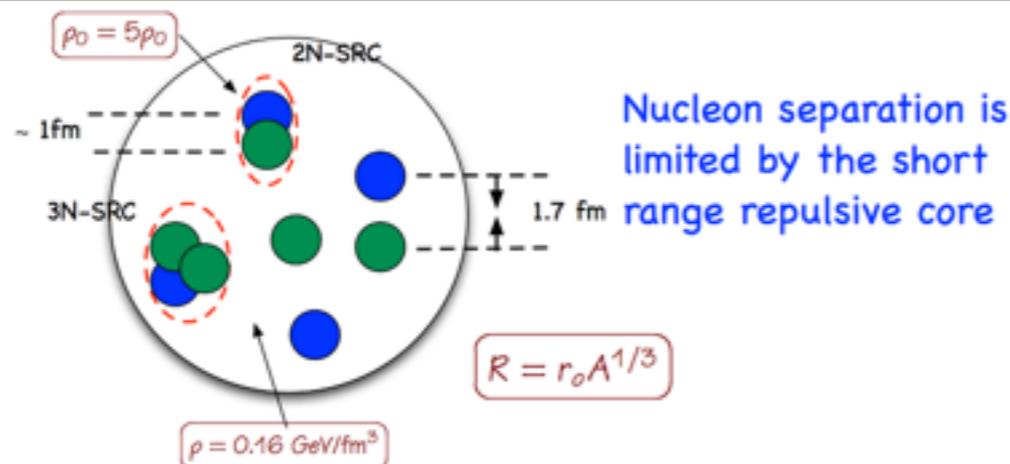
NUCLEAR MODEL

STANDARD —> MODIFIED SHELL MODEL

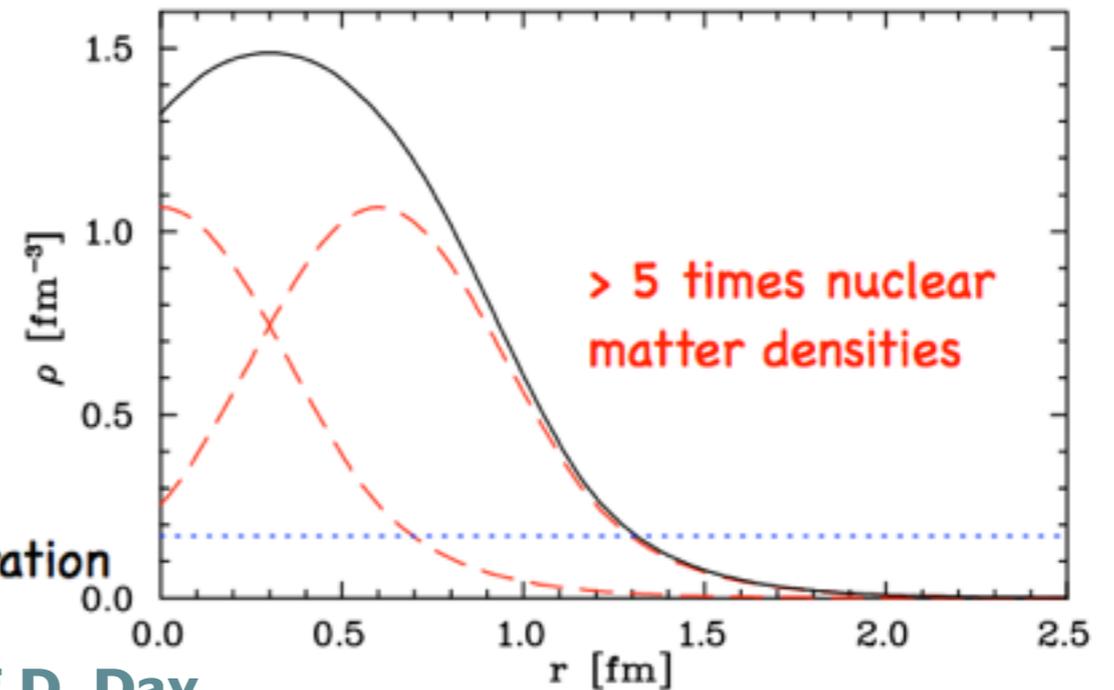
THE NATURE OF N-N CORRELATIONS (QUALITATIVE)

Short Range Correlations

JLab $^{12}\text{C}(e,e'pN)$ experiment



Determined by N-N potential



courtesy of D. Day

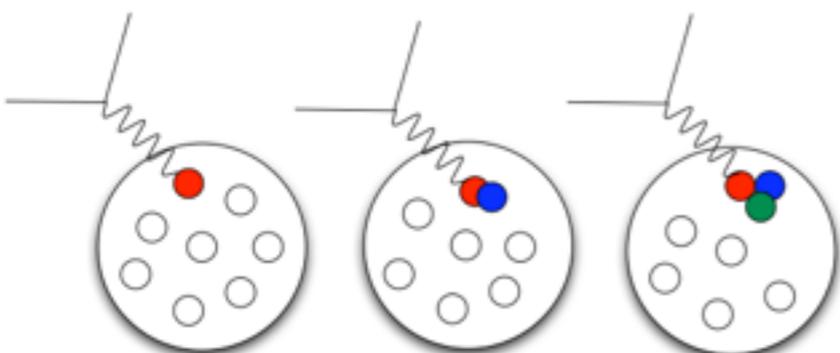
1. N-N (position) correlation is formed by the nucleon charge density distribution and leads to the individual shell structure for each specific nucleus (different A, different Z)
2. N-N correlation causes the overlap between adjacent shells and thus produces the strong short-range repulsive force
3. N-N correlation force is universal for all nuclei (how do we know? - see the next slide)
4. N-N correlation force is quite similar to the type of force acting on quasi-free nucleons

NUCLEAR MODEL

STANDARD —> MODIFIED SHELL MODEL

WHAT IS SPECTROSCOPIC FACTOR?

(QUANTITATIVE DESCRIPTION OF N-N INTERACTIONS)



$$Z_n = \int \frac{d^3k}{(2\pi)^3} |\hat{\chi}_n(\mathbf{k})|^2$$

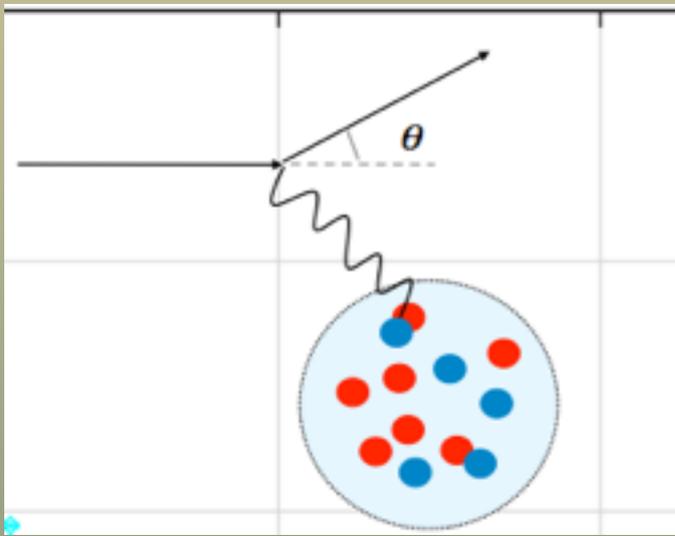
spectroscopic factor is extracted by taking the ratio of the experimental cross-section to the theoretical one.

$$\chi_n(\mathbf{r}_1) = \int d^3r_2 \dots d^3r_A \Psi_n^{A-1}(\mathbf{r}_2 \dots \mathbf{r}_A)^\dagger \Psi_0^A(\mathbf{r}_1 \dots \mathbf{r}_A)$$

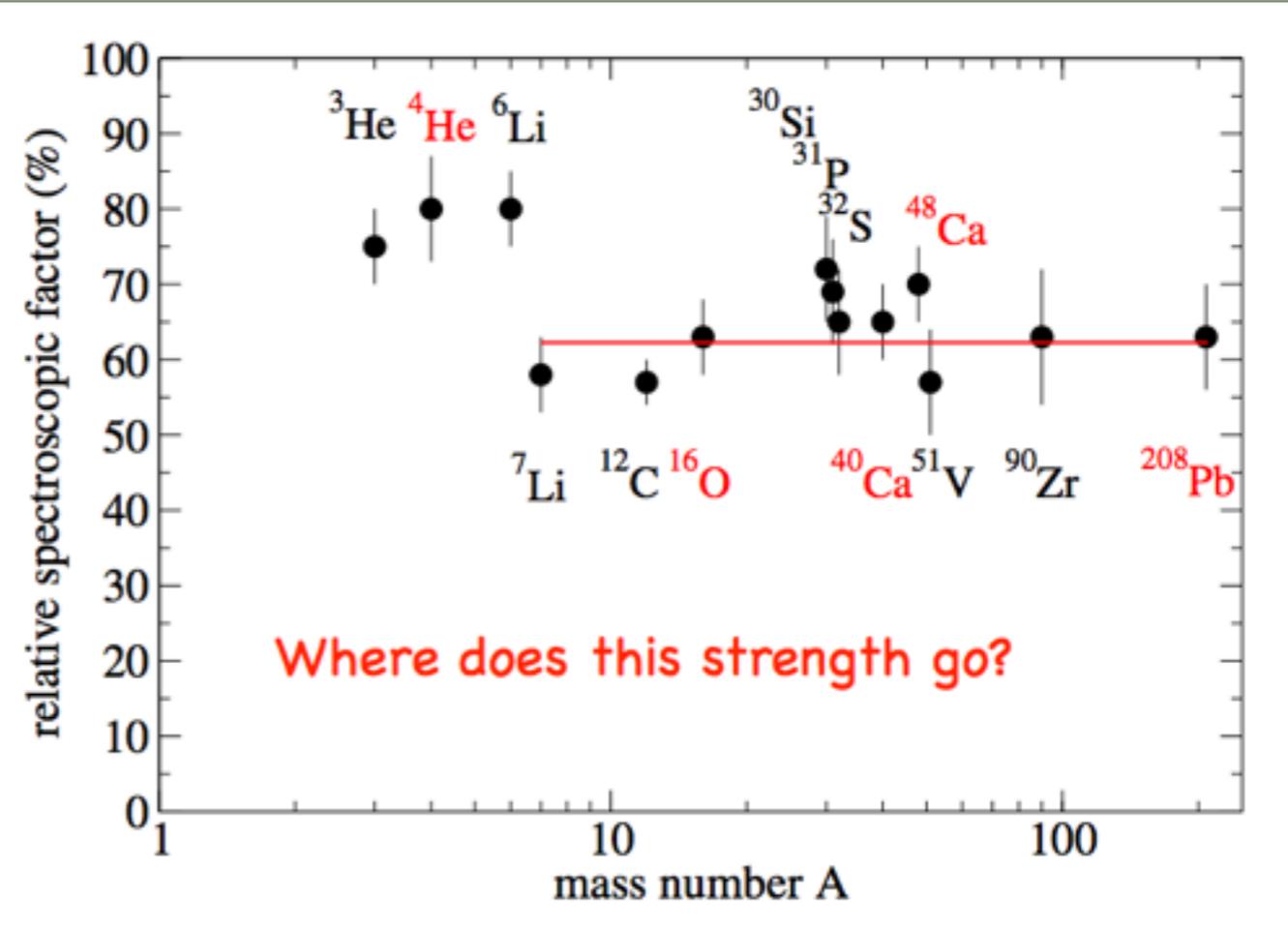
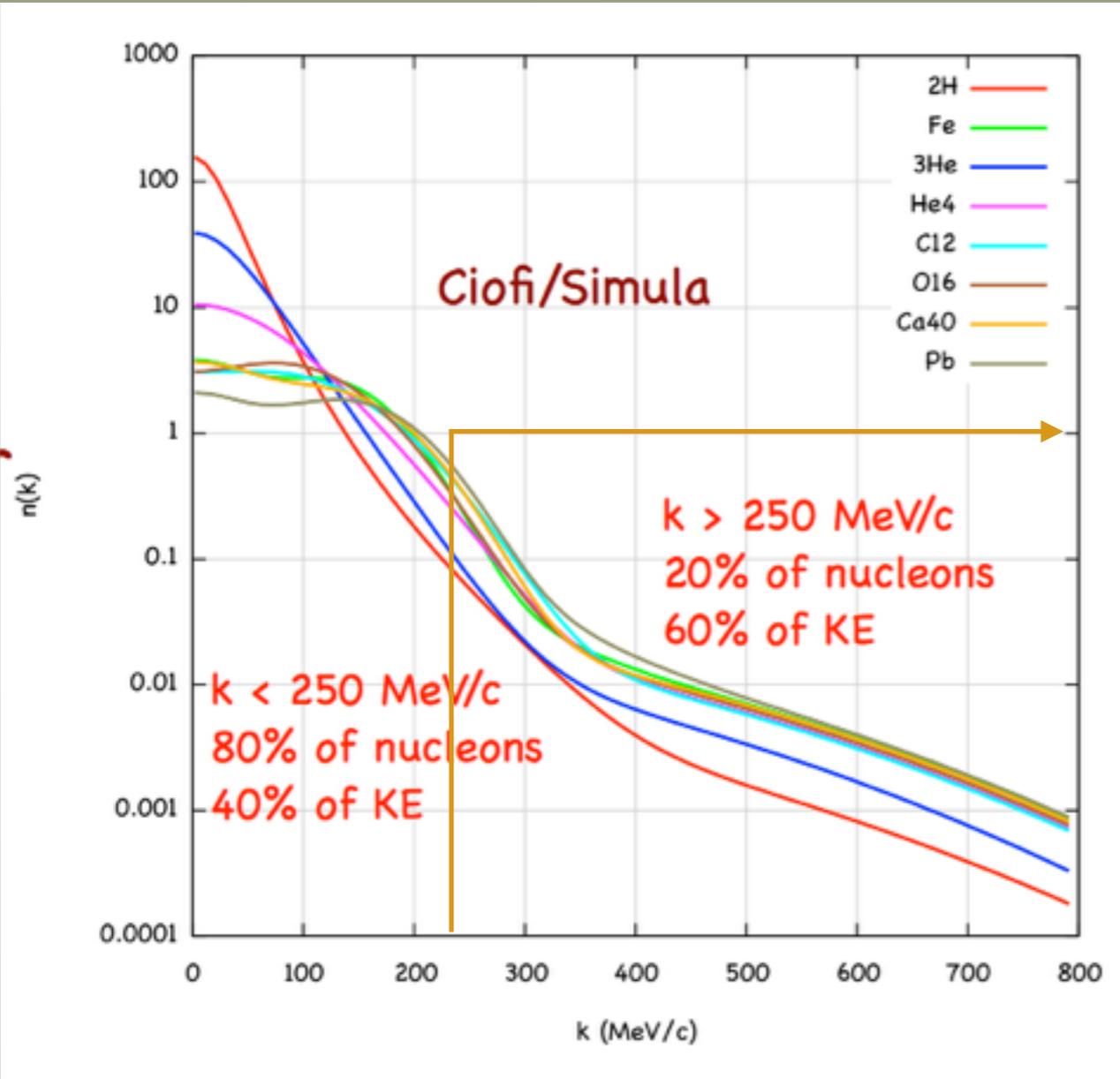
final-state (one-hole) initial-state

courtesy of O. Benhar

- ✦ **spectroscopic factor** tells you the number of bound-state (valence orbital - near Fermi sea) nucleons interacting with the incoming beam particles
- ✦ **spectroscopic factor** reflects the evidence of presence of short-range N-N correlations; the stronger N-N correlations; the more reduction the spectroscopic factor is (no N-N, $Z_n = 1$)
- ✦ **spectroscopic factor** also manifests the existence of long-range N-N correlations, leading to 2p2h
- ✦ **spectroscopic factor** is not the same as the occupation number, for the spectroscopic factor is determined by integrating the probability of knocking out "one" bound-state nucleon associated with one quantum number and meanwhile leaving the residual system with an excitation energy over the E_{miss} of bound states. the occupation number instead tells you the total number of nucleons from both bound and continuous states, so it's always larger than the spectroscopic factor.



shapes of tail structures above Fermi sea are nearly the same for different nuclei \longleftrightarrow
N-N short-range correlation effect is universal for all nuclei (spectroscopic factor is similar for light/medium/heavy nuclei)



Take ^{40}Ca - proton separation energy

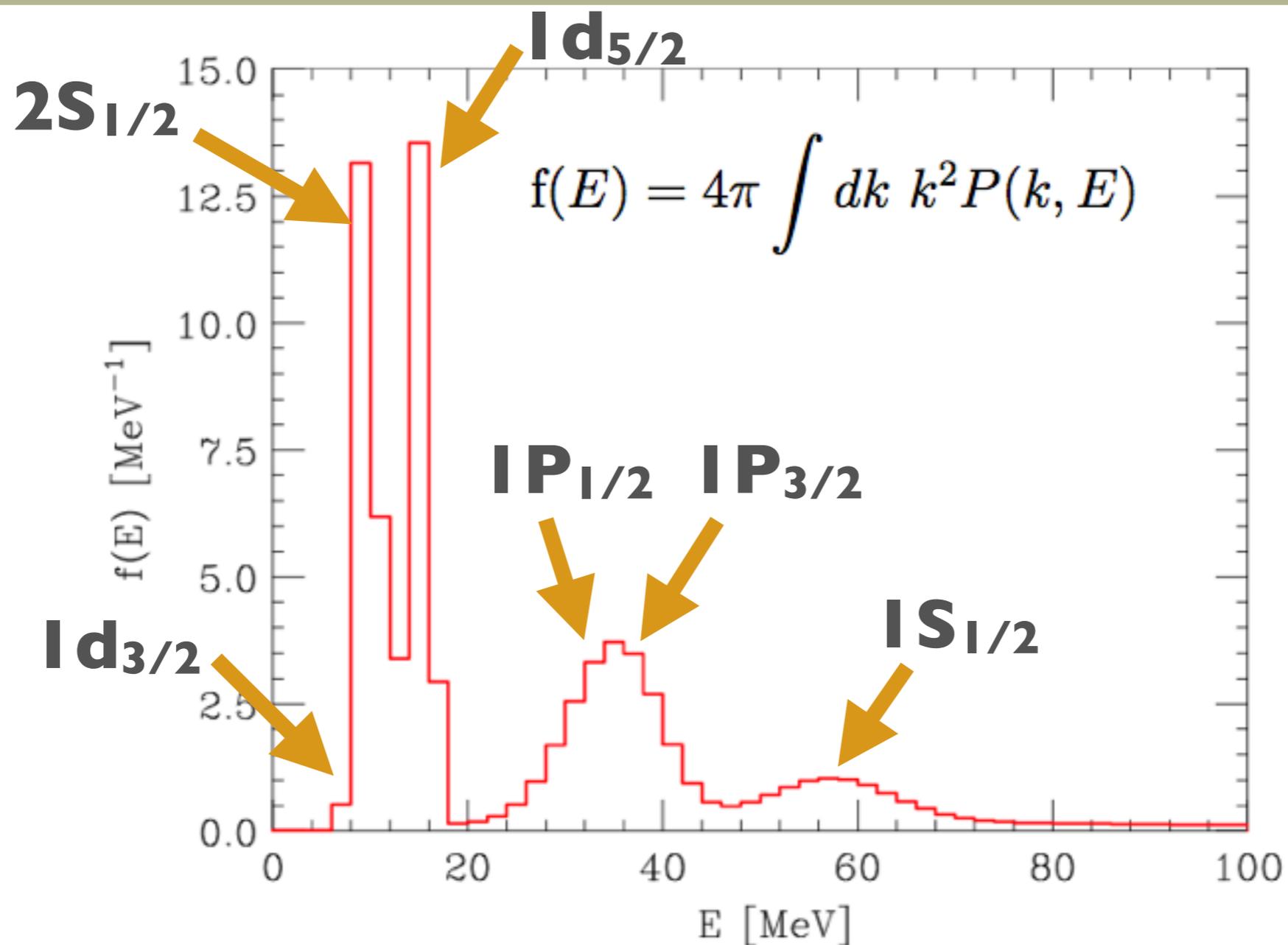


FIG. 2: Proton removal energy distribution in the $^{40}_{20}\text{Ca}$ ground state, obtained from Eq.(18) using the model spectral function of Ref. [13]. courtesy of O. Benhar

Take ^{40}Ca Structure Functions - proton's momentum distribution (bound states only)

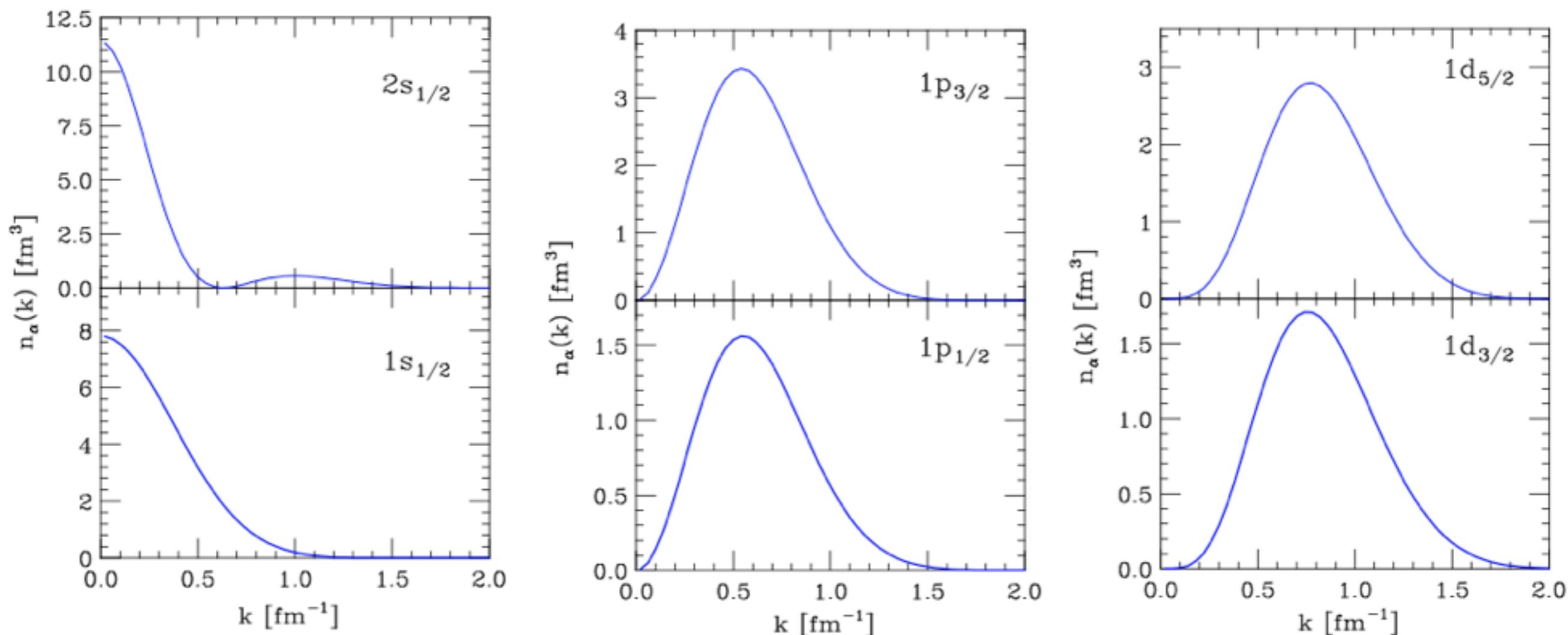


FIG. 3: Momentum distributions of the shell model orbits occupied by protons in the $^{40}_{20}\text{Ca}$ ground state. The results have been obtained using the Woods-Saxon potential reported in Ref. [16].

courtesy of O. Benhar

Improving the accuracy of neutrino energy reconstruction in charged-current quasielastic scattering off nuclear targets

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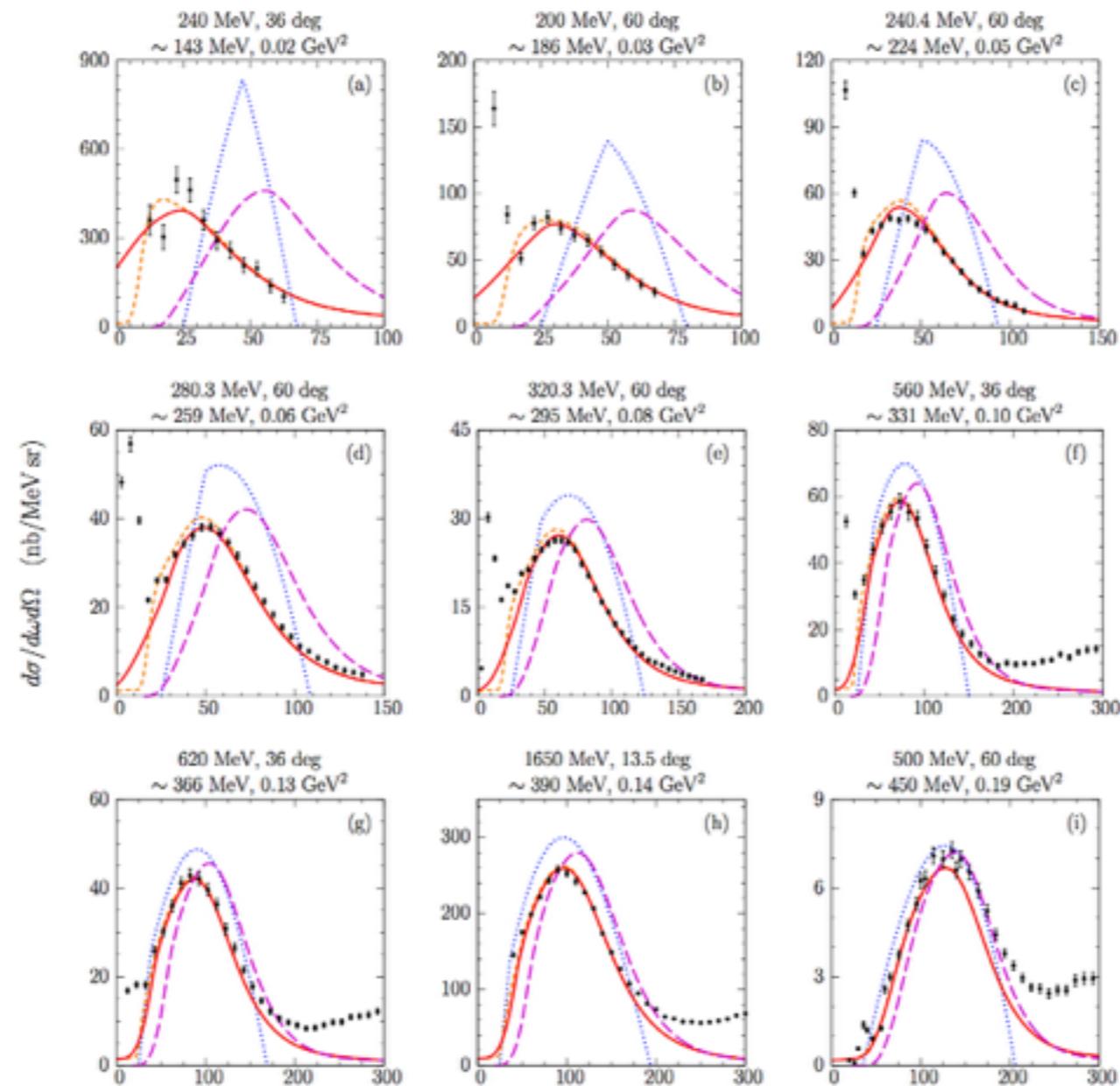


FIG. 2. (color online). Double differential electron-carbon cross sections, $d\sigma/d\omega d\Omega$. The results obtained with Pauli blocking accounted for in the local-density (solid lines) and step-function (short-dashed lines) approximations are compared to the experimental data of Refs. [15–17]. The IA (long-dashed lines) and RFG calculations (dotted lines) are also shown, for reference. The panels are labeled according to beam energy, scattering angle, and values of $|\mathbf{q}|$ and Q^2 at the quasielastic peak.