

NuWro: π production

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Outline

- NuWro π production dilemma
- some comparisons with the data
- a general description of the model
- more details (only if there is time and interest)

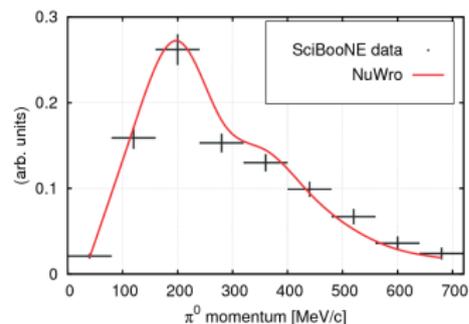
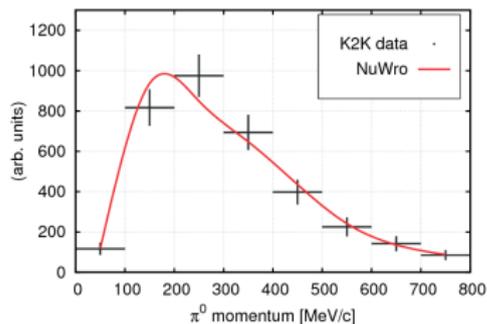
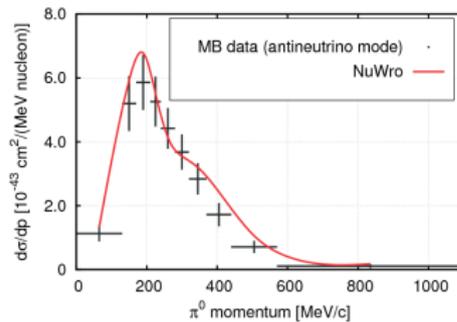
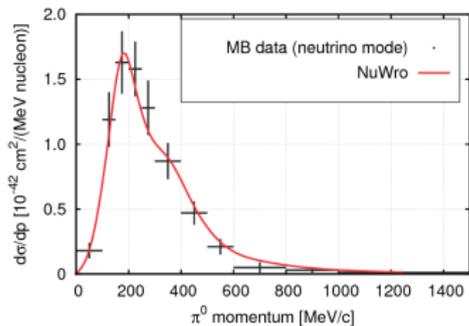


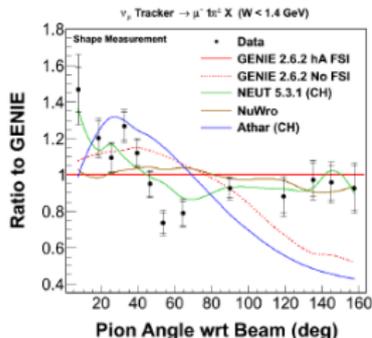
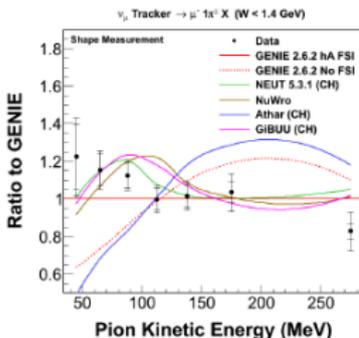
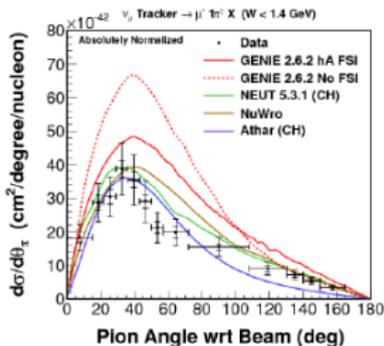
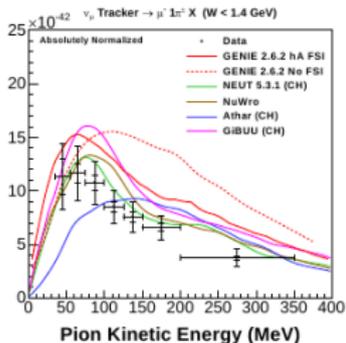
NuWro π production dilemma

- we know the current model is not sophisticated
- but it gives rather good agreement with the data
- RES/DIS transition region requires a lot of work.

A possible strategy: to implement a better (from theorist point of view) model and to keep two options.



Comparisons. $\text{NC}\pi^0$ production.

Comparisons. MINERvA CC π^+ data

A disclaimer: no fine tuning was done to arrive at this agreement.



RES@NuWro current model

NuWro definition of RES and DIS is different wrt other MCs.

- RES means $W \leq 1.6$ GeV (W is invariant hadronic mass)
- DIS means $W > 1.6$ GeV
- RES is dominated by Δ excitation
- RES contains a contribution from 2π production
- DIS also contains single pion production (SPP) events
- DIS uses PYTHIA fragmentation routines to produce final states – nothing is done *by hand*
- DIS code works also for $W \leq 1.6$ GeV and is used to model non-resonant background to SPP.



RES@NuWro more details

NuWro reproduces the following cross section

$$\frac{d\sigma^{SPP}}{dW} = \frac{d\sigma^{\Delta}}{dW} (1 - \alpha(W)) + \frac{d\sigma^{DIS}}{dW} F^{SPP}(W)\alpha(W)$$

with

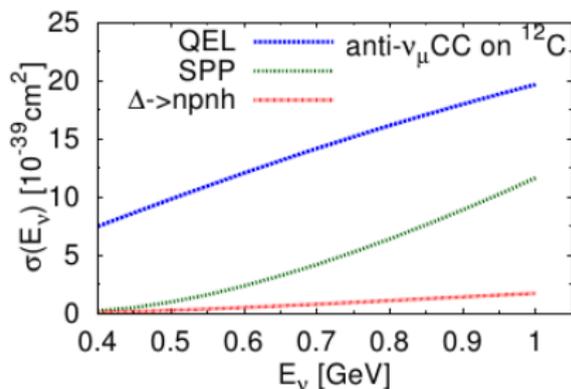
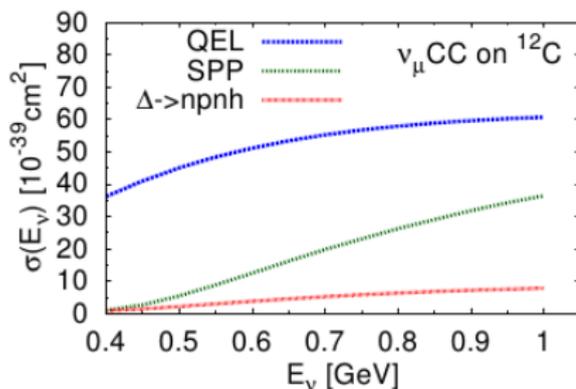
$$\begin{aligned} \alpha(W) = & \Theta(W_{min} - W) \frac{W - W_{th}}{W_{min} - W_{th}} \alpha_0 \\ & + \Theta(W_{max} - W) \Theta(W - W_{min}) \frac{W - W_{min} + \alpha_0(W_{max} - W)}{W_{max} - W_{min}} \\ & + \Theta(W - W_{max}) \end{aligned}$$

$W_{th} = M + m_{\pi}$, W_{min} and W_{max} define Δ - DIS transition region; default values are $W_{min} = 1.3$ GeV, $W_{max} = 1.6$ GeV.



Nuclear effects

- Fermi motion
- Pauli blocking
- approximate treatment of Δ in-medium selfenergy by subtracting a fraction of pionless decays evaluated after theoretical computations:

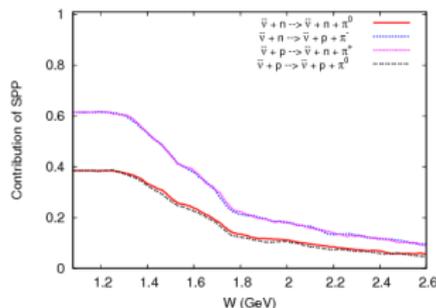
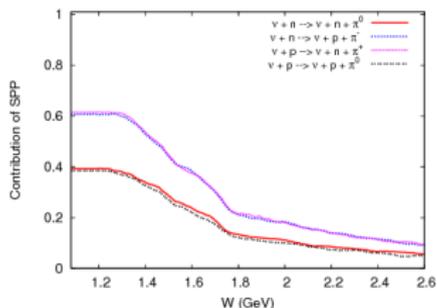
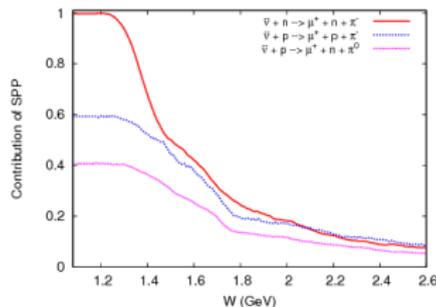
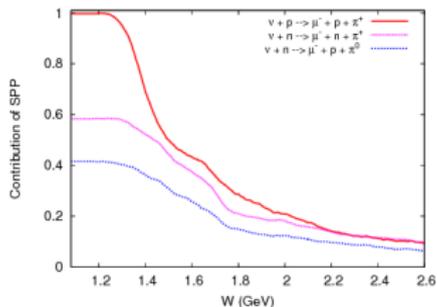


Back-up slides (more details)



RES@NuWro one pion functions

$F^{SPP}(W)$ are *one pion functions*. They are defined as probabilities of single π final state in the overall cross section – as given by PYTHIA.



NuWro calculates them at the beginning of every run. It takes ~ 10 seconds.



Nonresonant background parameters

kanal:	$\nu p \rightarrow \mu^- p \pi^+$	$\nu n \rightarrow \mu^- n \pi^+$	$\nu n \rightarrow \mu^- p \pi^0$
α_0	0.0	0.2	0.3
kanal:	$\bar{\nu} n \rightarrow \mu^+ n \pi^-$	$\bar{\nu} p \rightarrow \mu^+ p \pi^-$	$\bar{\nu} p \rightarrow \mu^+ n \pi^0$
α_0	0.0	0.2	0.3

It is consistent with the M_A , $C_A^5(0)$ values obtained from fitting the ANL and BNL data within a model with no background in the Δ^{++} channel.



$N - \Delta$ transition matrix element:

$$\langle \Delta^{++}(p') | V_\mu | N(p) \rangle = \sqrt{3} \bar{\Psi}_\lambda(p') \left[g_\mu^\lambda \left(\frac{C_3^V}{M} \gamma_\nu + \frac{C_4^V}{M^2} p'_\nu + \frac{C_5^V}{M^2} p_\nu \right) q^\nu - q^\lambda \left(\frac{C_3^V}{M} \gamma_\mu + \frac{C_4^V}{M^2} p'_\mu + \frac{C_5^V}{M^2} p_\mu \right) \right] \gamma_5 u(p)$$

$$\langle \Delta^{++}(p') | A_\mu | N(p) \rangle = \sqrt{3} \bar{\Psi}_\lambda(p') \left[g_\mu^\lambda \left(\gamma_\nu \frac{C_3^A}{M} + \frac{C_4^A}{M^2} p'_\nu \right) q^\nu - q^\lambda \left(\frac{C_3^A}{M} \gamma_\mu + \frac{C_4^A}{M^2} p'_\mu \right) + g_\mu^\lambda C_5^A + \frac{q^\lambda q_\mu}{M^2} C_6^A \right] u(p).$$

$\Psi_\mu(p')$ is the Rarita-Schwinger field, and $u(p)$ is the Dirac spinor.

C_3^V , C_4^V , C_5^V known from pion electroproduction due to CVC.



Axial part:

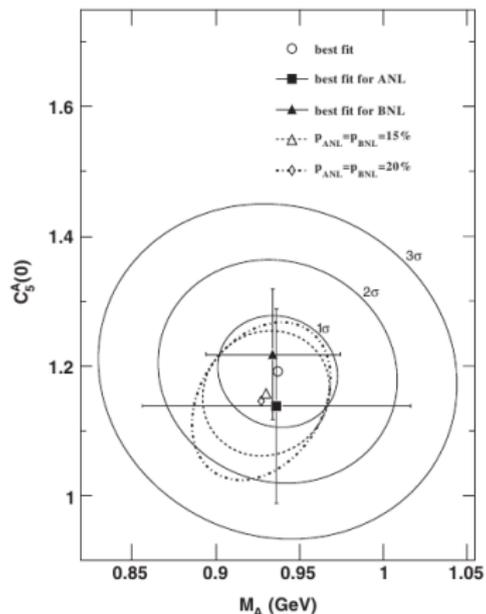
- typically one sets $C_3^A(Q^2) = 0$;
- Adler model suggests $C_4^A(Q^2) = -C_5^A(Q^2)/4$
- PCAC implies $C_6^A(Q^2) = \frac{M^2}{m_\pi^2 + Q^2} C_5^A(Q^2)$
- $C_5^A(0)$
 - is either evaluated from the *off-diagonal Goldberger-Treiman relation*

$$C_5^A(0) = \frac{g_{\pi N\Delta} f_\pi}{\sqrt{6} M} \simeq 1.15,$$

- or is treated as a free parameter
- typically one assumes $C_5^A(Q^2) = C_5^A(0) \left(1 + \frac{Q^2}{M_A^2}\right)^{-2}$.



Values of $C_5^A(0)$ and M_A .



- in order to extract their values overall normalization uncertainty, deuteron nuclear effects, nonresonant background contribution (Nieves et al) should be included in the analysis
- a tension between ANL and BNL pion production data disappear
- on the left, results of simultaneous fit to both data sets

K.M. Graczyk, D. Kietczewska, P. Przewłocki, JTS, PRD80 093001 (2009)



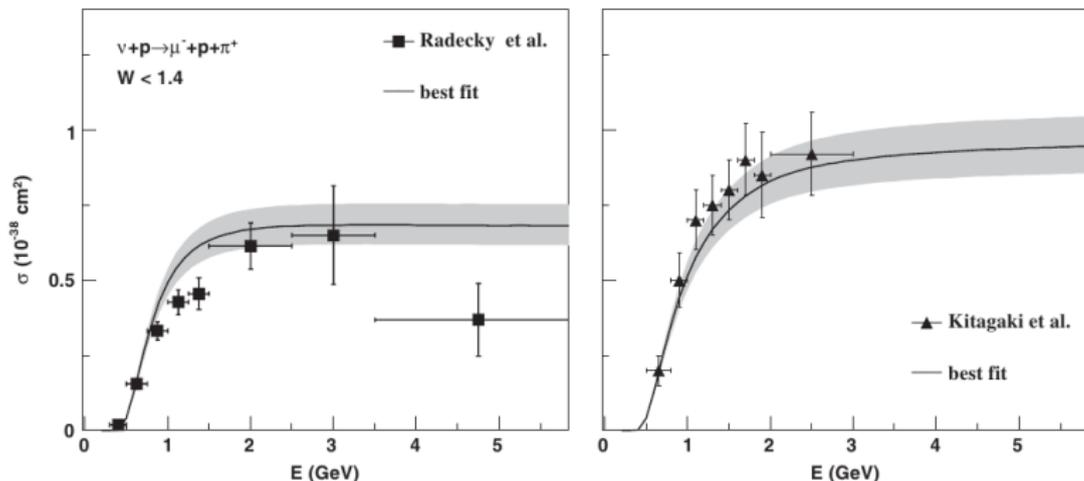
Values of $C_5^A(0)$ and M_A .

FIG. 5. Total cross section for $\nu + p \rightarrow \mu^- + p + \pi^+$. In the left panel the ANL data [5] with the cut $W = 1.4$ are shown (black squares), while the right panel presents the BNL data [42] (without cuts in W)—black triangles. The overall normalization error is not plotted. The best fit curves were obtained with a corresponding cut in W . The theoretical curves were obtained with dipole parametrization Eq. (32) with $M_A = 0.94 \text{ GeV}$ and $C_5^A(0) = 1.19$. The shaded areas denote the 1σ uncertainties of the best fit. The theoretical curves are not modified by the deuteron correction effect.

